Vadalog:

Introduction, Extensions and Business Applications

Emanuel Sallinger

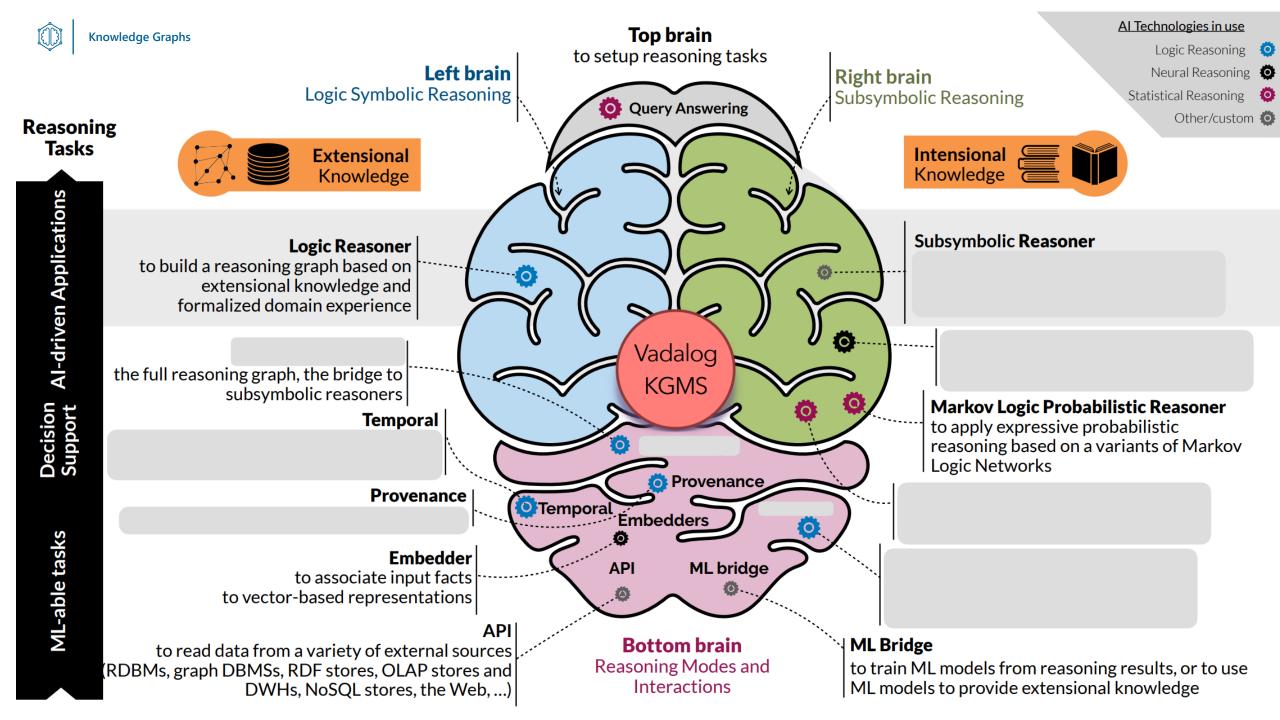




Knowledge Graph Lab



The 18th Reasoning Web Summer School Declarative Al 30 September 2022



AMW 2016

LANGUAGE

Data Wrangling for Big Data: Towards a Lingua Franca for Data Wrangling

2016–2019 Selected Highlights



LOGIC

Swift Logic for Big Data and Knowledge Graphs



The VADA Architecture for Cost-Effective Data Wrangling

MEDI 2018

DATA SCIENCE

Data Science with Vadalog: Bridging Machine Learning and Reasoning

VLDB2018 -

SYSTEM

The Vadalog System: Datalogbased Reasoning for Knowledge Graphs



2019 -

PROJECT ARCHITECTURE

VADA: an architecture for end user informed data preparation



SPACE EFFICIENCY

The Space-Efficient
Core of Vadalog



ENTERPRISE AI

Knowledge Graphs and Enterprise AI: The Promise of an Enabling Technology

Datalog 2.0 2019

RECOMMENDER SYSTEMS

Feature Engineering and Explainability with Vadalog: A Recommender Systems Application

COVID-19: LOCKDOWN

COVID-19 and Company Knowledge Graphs: Assessing Golden Powers and Economic Impact of Selective Lockdown via AI Reasoning

ENTERPRISE AI IN PRACTICE

Weaving Enterprise Knowledge Graphs: The Case of Company Ownership Graphs

Declarative AI 2020

COVID-19: TAKEOVERS

Reasoning on Company Takeovers during the COVID-19 Crisis with Knowledge Graphs

Declarative AI 2020

PROBABILISTIC

Reasoning Under Uncertainty in Knowledge Graphs

Declarative AI 2020

MONEY LAUNDERING

Rule-based Anti-Money Laundering in Financial Intelligence Units: Experience and Vision



KNOWLEDGE GRAPHS

Knowledge Graphs: The Layered Perspective



BOOK

Knowledge Graphs and Big Data Processing



KG EMBEDDINGS

Reasoning in Knowledge Graphs:
An Embeddings Spotlight

2021

Selected Highlights



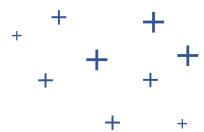
CONFIDENTIALITY

Financial Data Exchange with Statistical Confidentiality: A Reasoning-based Approach



COMPANY CONTROL

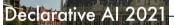
Distributed Company Control in Company Shareholding Graphs



Declarative Al 2021

TEMPORAL

Monotonic Aggregation for Temporal Datalog



HARMFUL JOINS

Eliminating Harmful Joins in Warded Datalog+/-.

Declarative Al 2021

INDUSTRIAL BLOCKCHAIN

Rule-based Blockchain Knowledge Graphs: Declarative AI for Solving Industrial Blockchain Challenges



JOINS

Traversing Knowledge Graphs with Good Old (and New) Joins



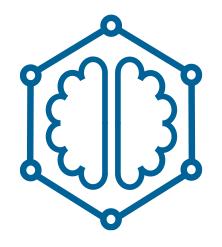
HYBRID AI

Augmenting Logic-based Knowledge Graphs: The Case of Company Graphs



BLOCKCHAIN VISION

Blockchains as Knowledge Graphs
- Blockchains for Knowledge
Graphs



Knowledge Graphs People and Groups

Emanuel Sallinger



Prof. Dr.

Emanuel Sallinger





Knowledge Graph Lab



University of **Oxford**





Knowledge Graph Lab

Formally:

Vienna Science and Technology Fund (WWTF)
Vienna Research Group (VRG) on
Scalable Reasoning in Knowledge Graphs (VRG18-013)





Institute of Logic and Computation



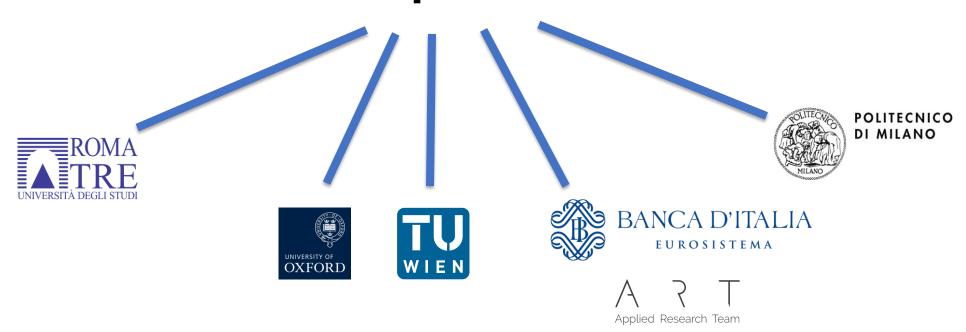






Center for Al and ML SIG Knowledge Graphs

Joint Knowledge Graph Labs





VADAValue-Added Data















Banking and Finance











SIEMENS

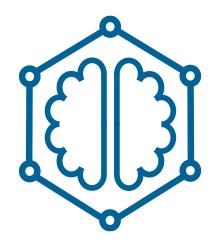
Logistics





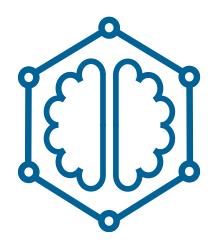
... and more





Knowledge Graphs People and Group

Emanuel Sallinger



Knowledge Graphs

Motivation

Emanuel Sallinger

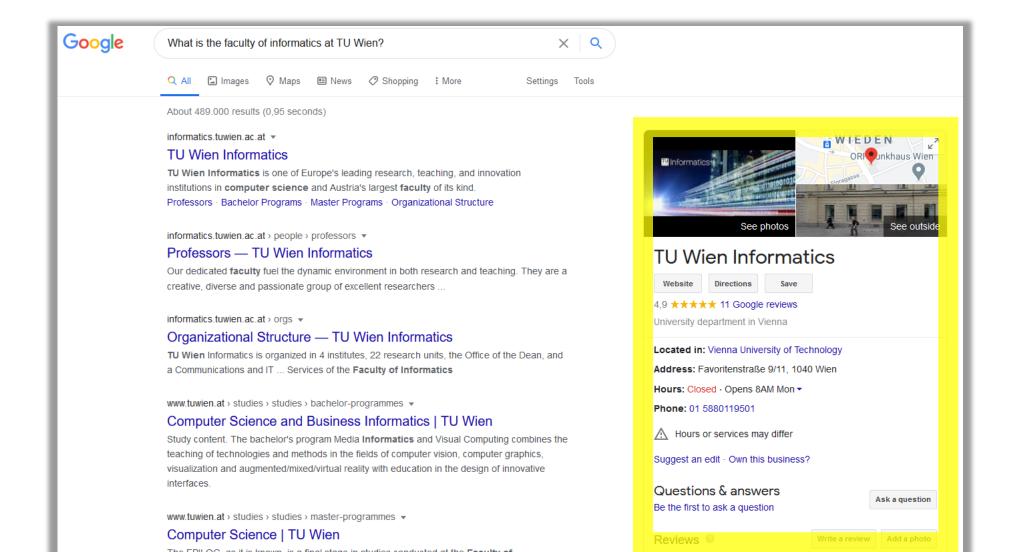


Motivation

- 1. The **technology** used by Google and others
- 2. A meeting place of **databases**, **data science** and **Artificial Intelligence** research
- 3. A **skillset** to solve fascinating problems

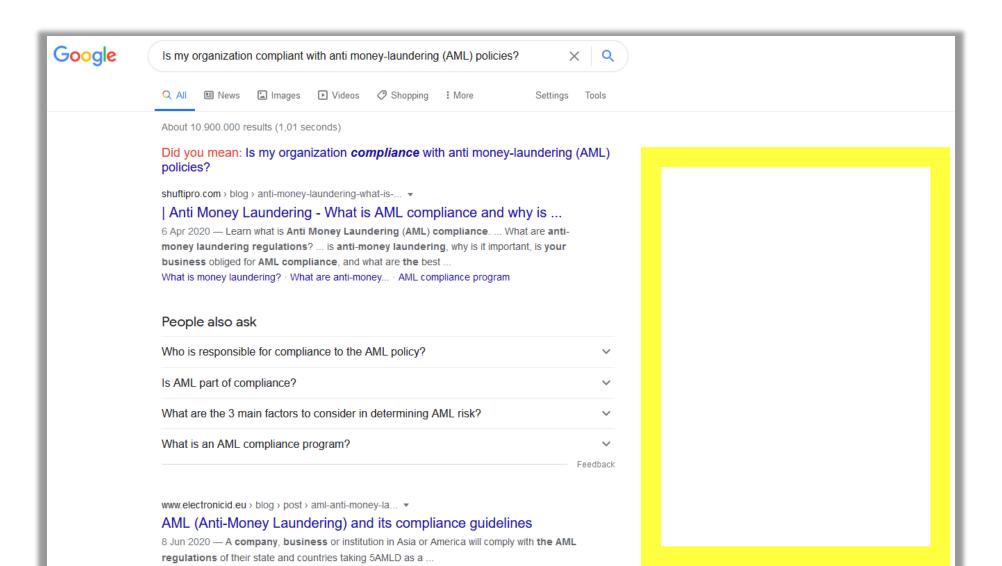


"What is the faculty of informatics at TU Wien"?





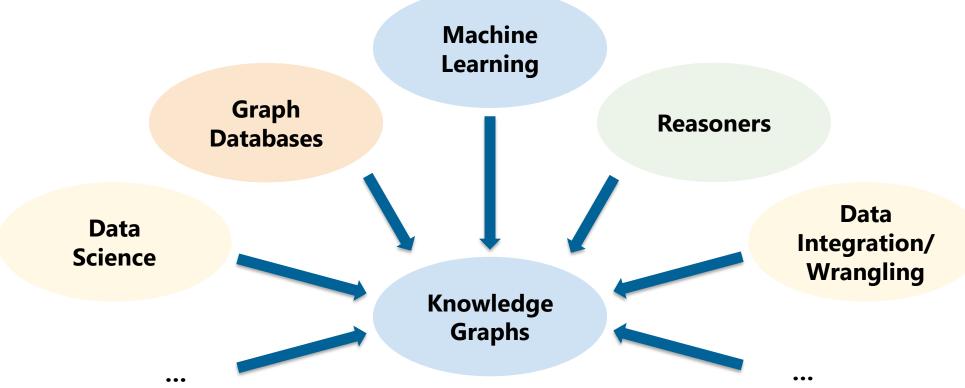
"Is my organization compliant with anti money-laundering (AML) policies?"





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Graph

Databases

Knowledge Graphs



Reasoners

Graph

Databases

Knowledge Graphs



Reasoners



expressive power

Knowledge Graphs

Graph Databases



Reasoners

expressive power

Knowledge Graphs

scalability

Graph Databases



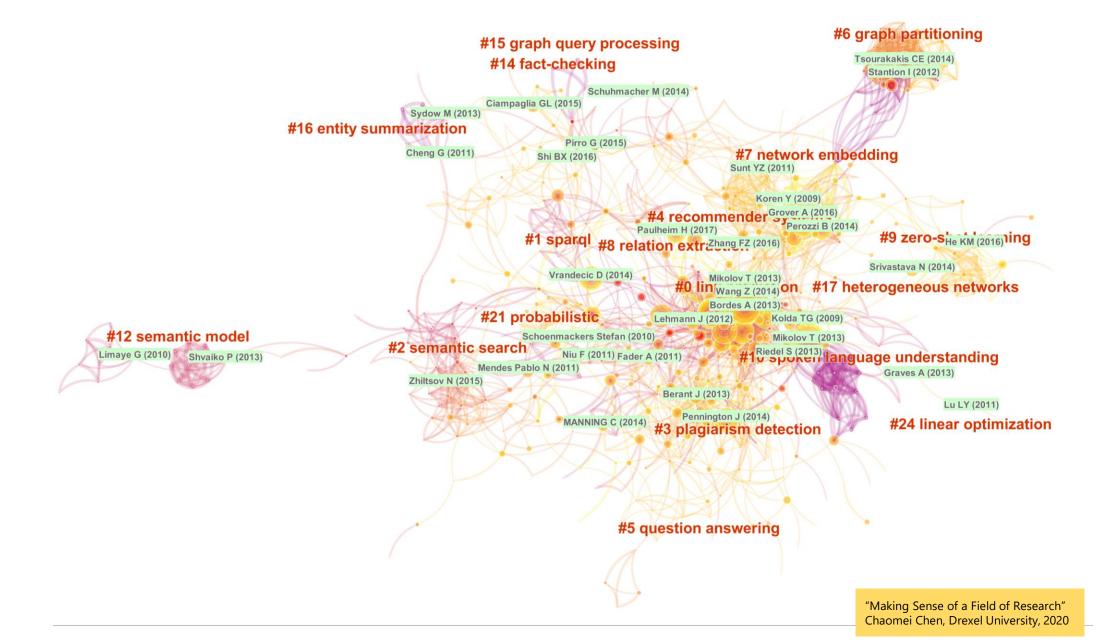
Reasoners

Dauphin Y (2014) Heck L (2012) #11 text analysis

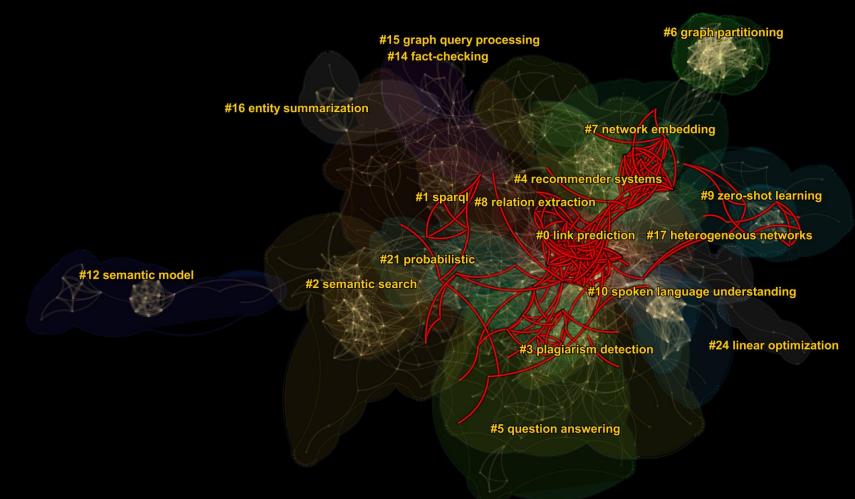
Gorlitz O (2011) #19 text analysis Chein M (2009) #12 text analysis Baker Collin (2008) Hakkani-Tur D (2013) **#5 text analysis** Favre B (2007) Agrawal R (2009) #6 structured knowledge-based search Mottin D (2014) Elbassuoni S (2009) #32 query by example Sunt YZ (2011) #1 ant colony optimisation Pound J (2010) Hoffart J (2013) Bizer C (2009) #4 convolution residual network #40 information extraction Bizer C (2009) #3 fuzzy cognitive maps Schultz A (2012) Vrandecic D (2014) Isele R (2013) Yih WT (2015) Pennington J (2014) #48 disambiguation of interpretations Berant J (2013) Wang Z (2014) #0 knowledge representation #33 text analysis Bordes A (2013) Lin Y (2015) Wang Z (2014) Suchanek FM (2007) Etzioni O (2008) Socher Richard (2013) #10 text analysis Mikolov T (2013) Auer S (2007) #23 link-prediction Nyhan B (2013) #2 text analysis Bollacker Kurt (2008) Fleischhacker D (2014) Mikolov T (2013) Schmachtenberg M (2014) #53 text analysis

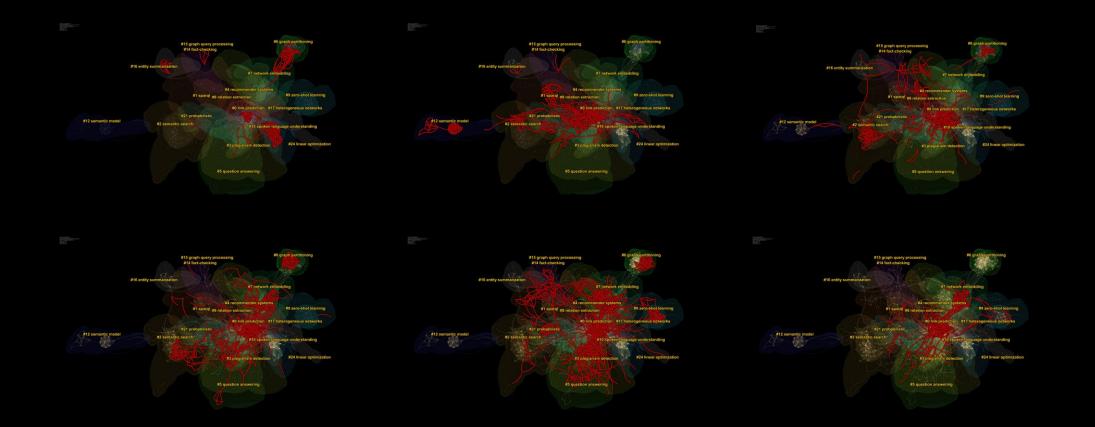
#39 relation

"Making Sense of a Field of Research" Chaomei Chen, Drexel University, 2020









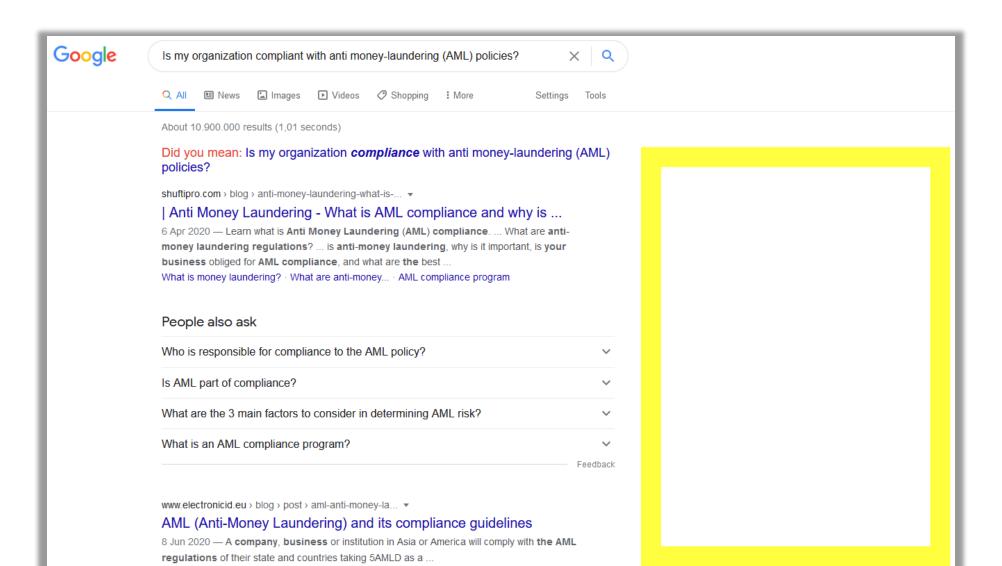


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FINANCIAL TIMES

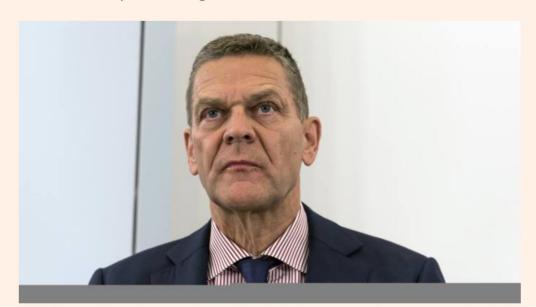
Danske Bank AS

+ Add to myFT

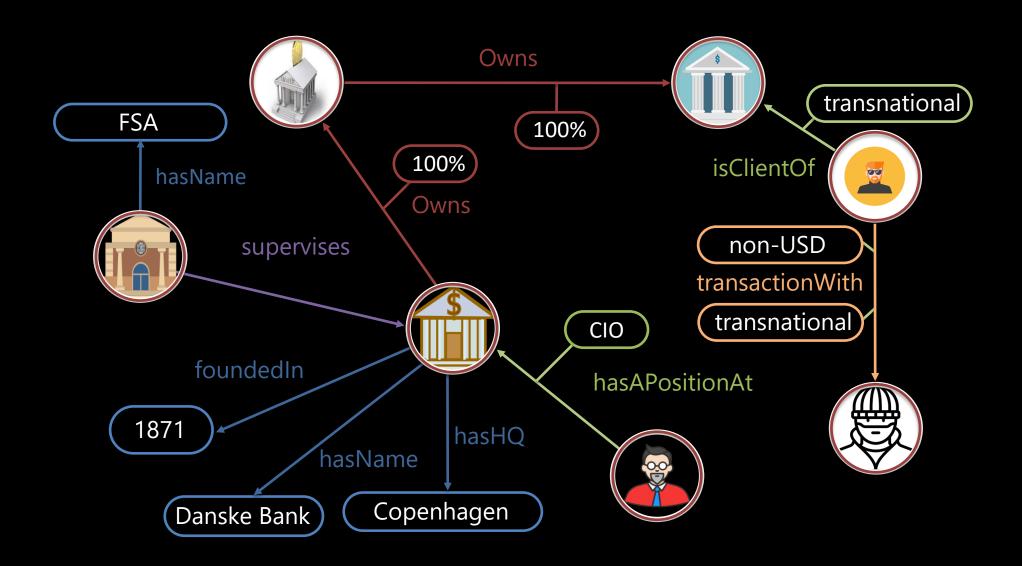
Danske Bank chairman ousted by main shareholder after scandal

Maersk family brings in new blood to stabilise lender in wake of €200bn money laundering

€200bn money laundering



Ole Andersen will step down as chairman of Danske Bank at an extraordinary general meeting in the next few weeks © Bloomberg





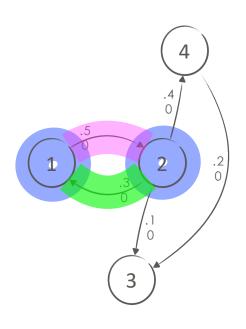


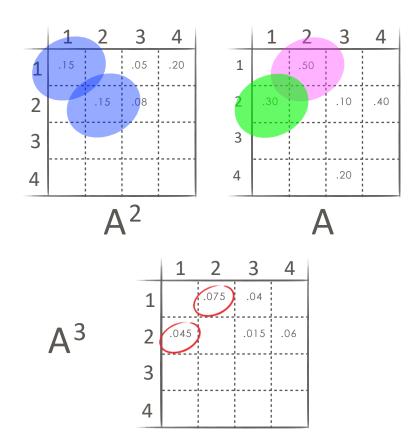






"Integrated Ownership"







Facebook KG Social graph with people, places, things



Amazon PG knowledge graph of all products



Factual Businesses & places



Wolfram KB World facts + mathematics



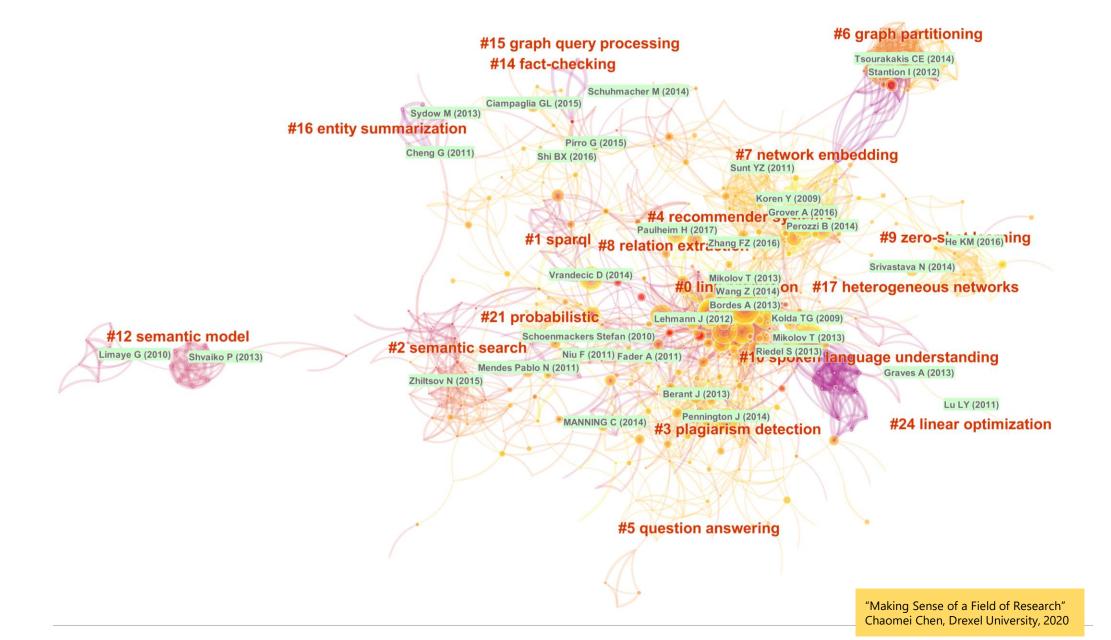
RIT People, skills, recruiting



Commercial Banks Customers, Companies, Risks, ...



Rating Agencies Companies, Evaluations, Risks, ...





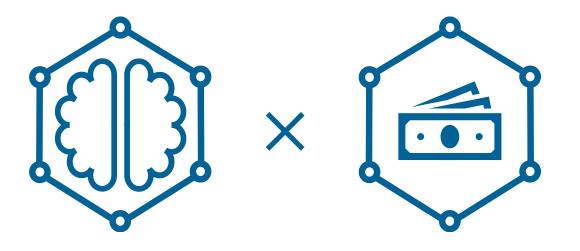
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Knowledge Graphs

Motivation



Overview Representations

With Financial KGs as a Running Example

Representations



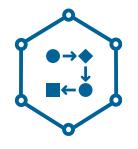
KG EmbeddingsWidely-applied, large family of ML models



Logical Knowledge in KGs Highly expressive, diverse family of logical models.



Graph Neural NetworksUsing the KG structure
as a neural network.



Data ModelsOverview of data models in different communities

FINANCIAL TIMES

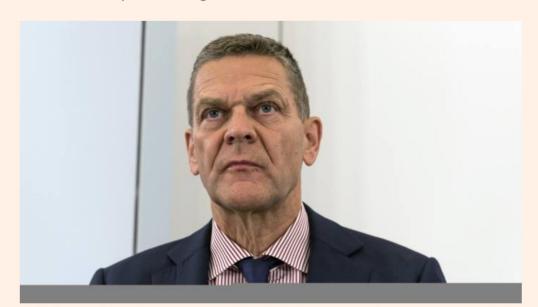
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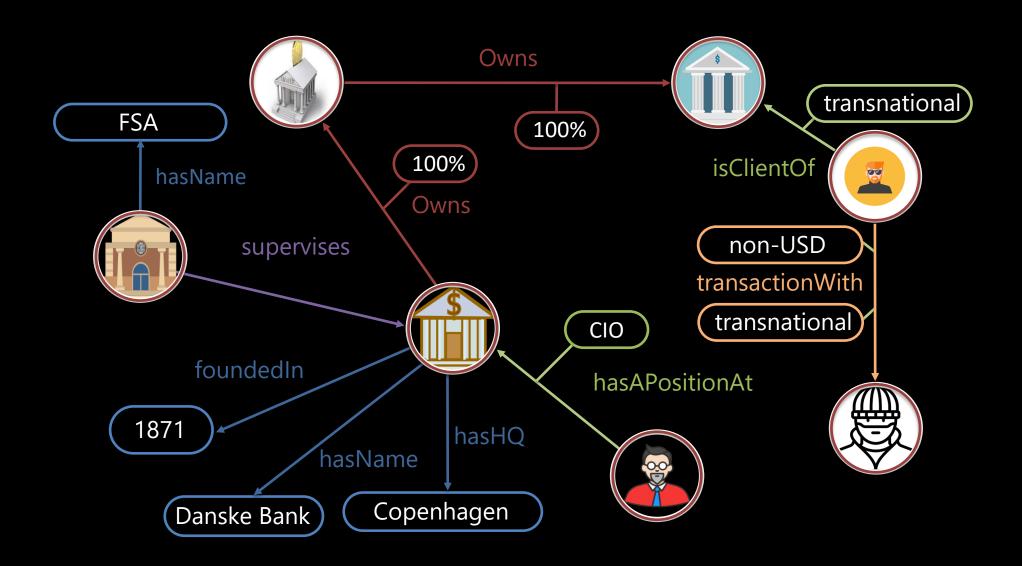
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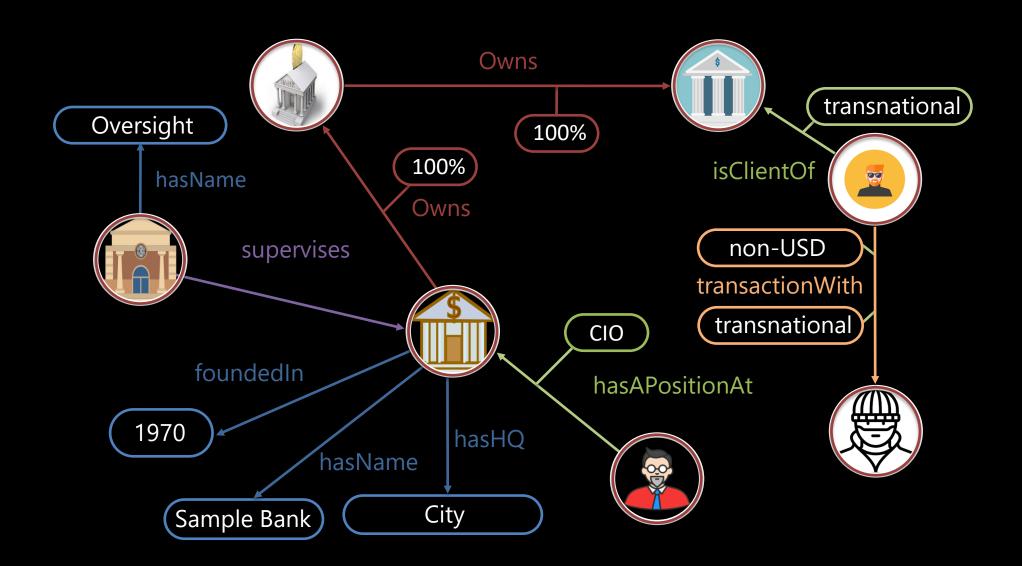
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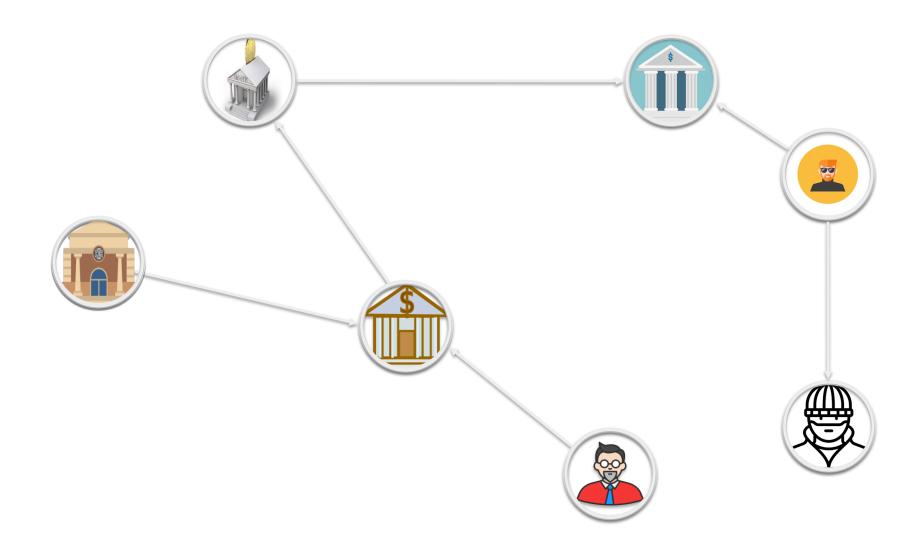


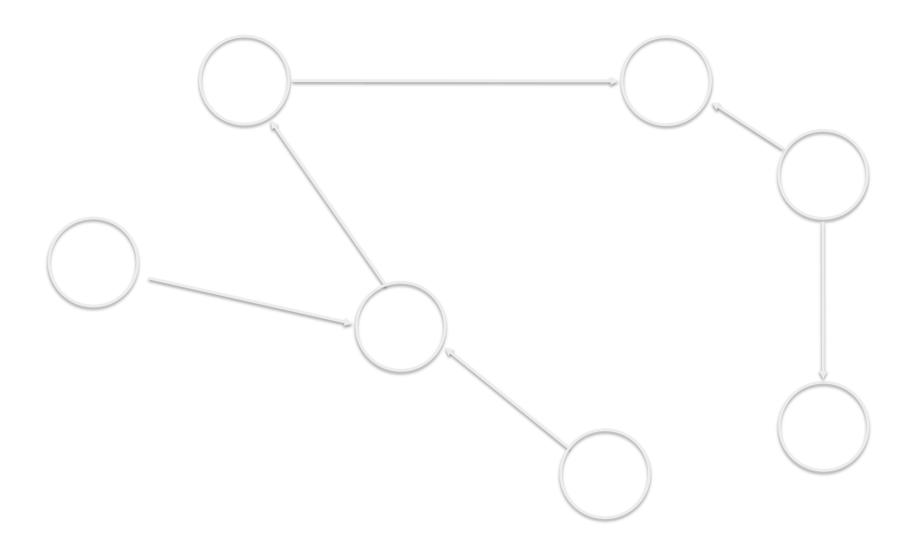
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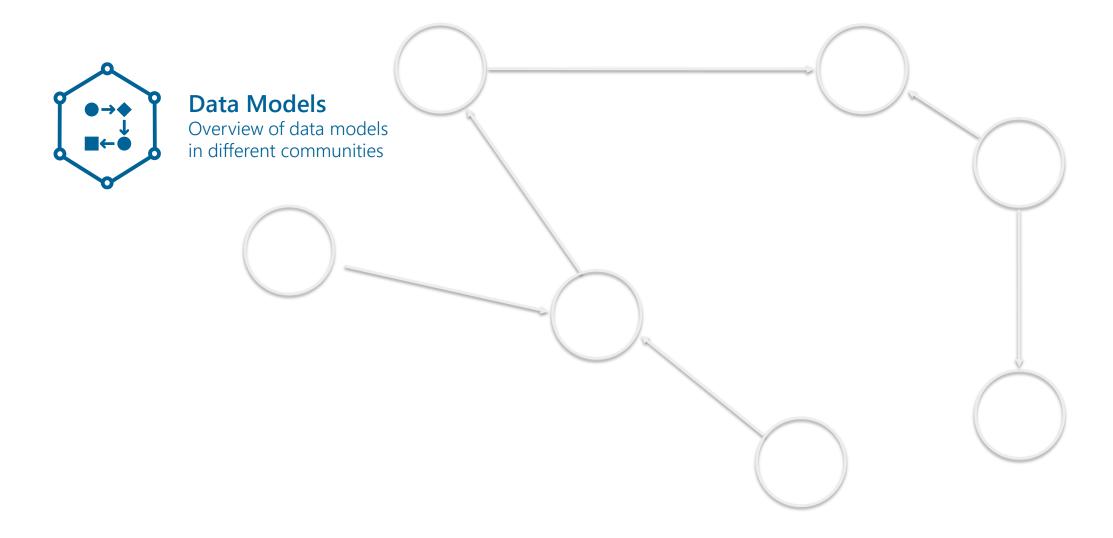


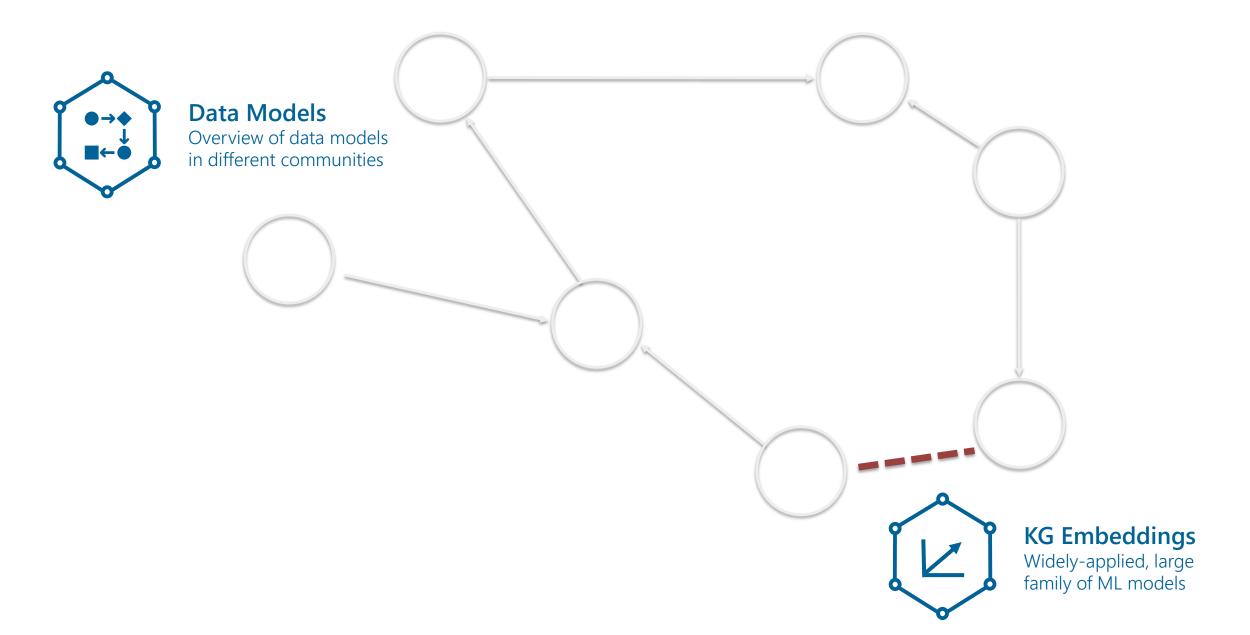


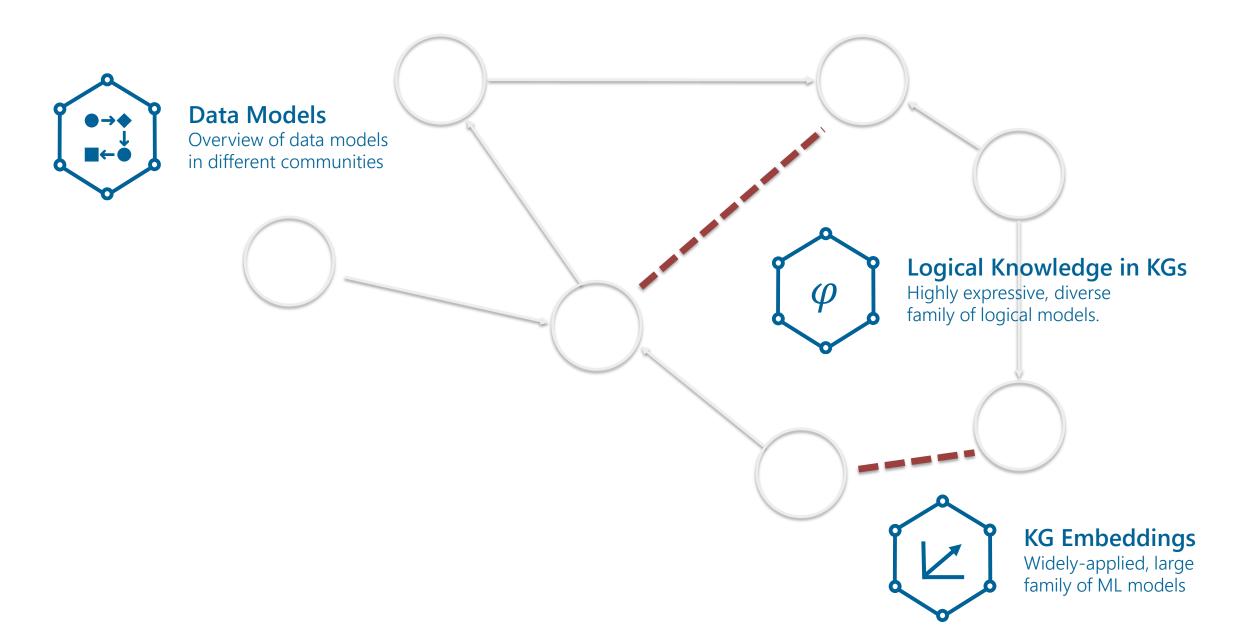


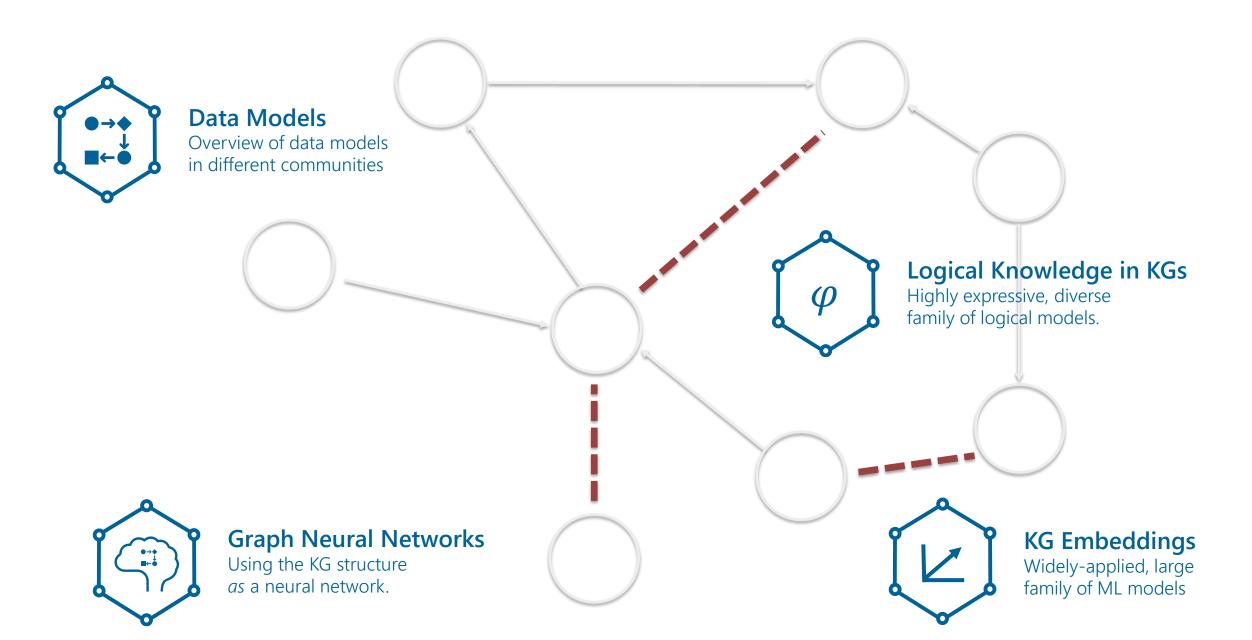












Representations



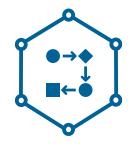
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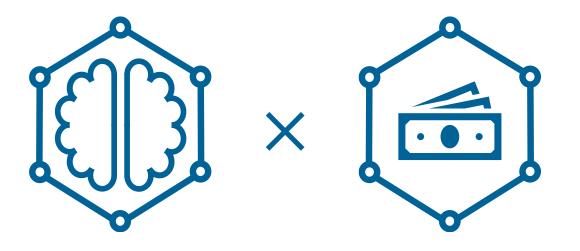
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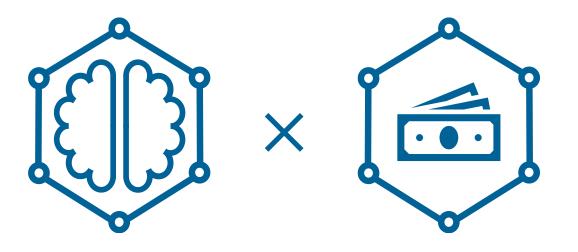


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Overview Representations

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Overview

Systems

With Financial KGs as a Running Example

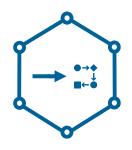
Systems



ArchitecturesThe big picture of building IT architectures for KGs



Scalable ReasoningMaking use of the knowledge in the KG

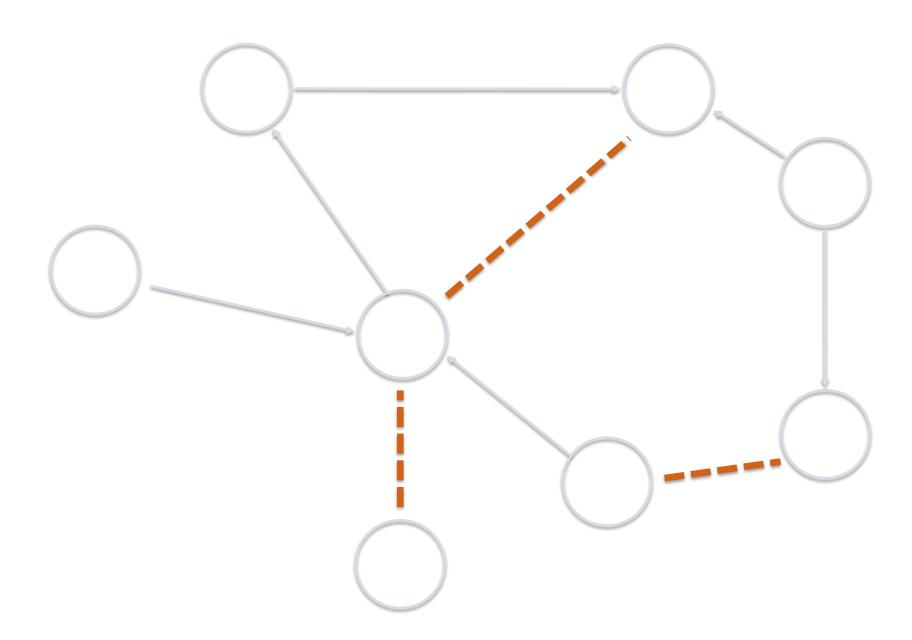


KG CreationHow to create a KG from heterogeneous data?

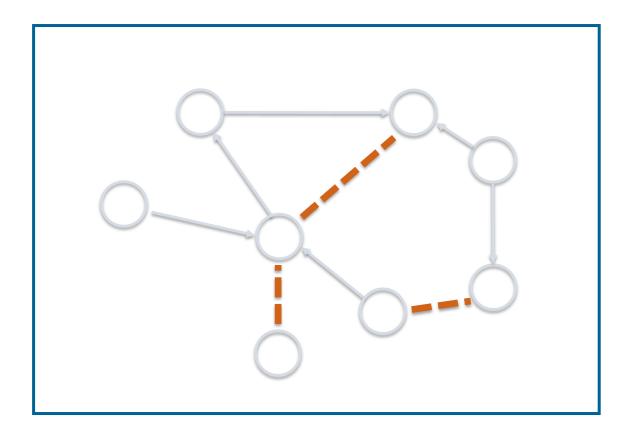


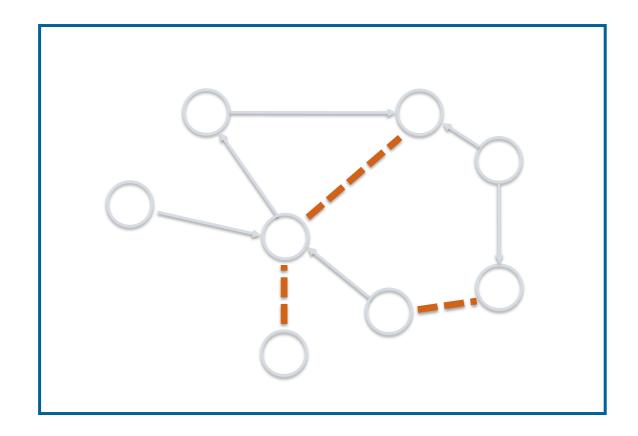
KG EvolutionHow to update, correct and complete a KG?





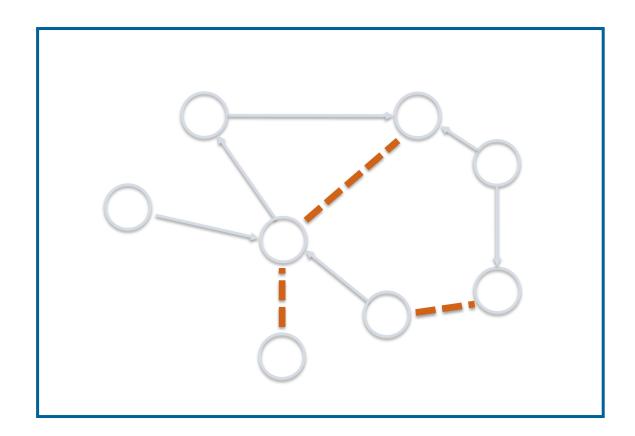








Architectures
The big picture of building
IT architectures for KGs

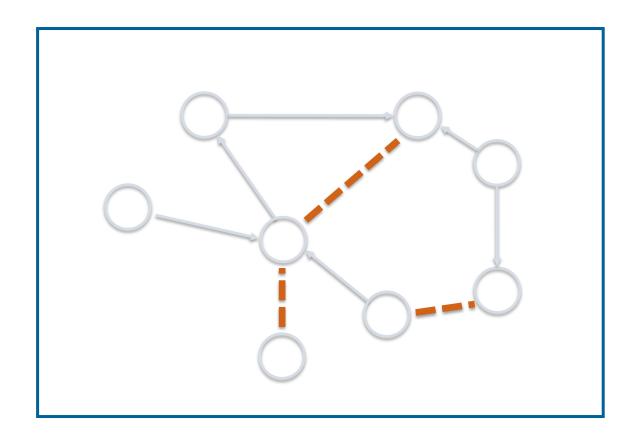




The big picture of building IT architectures for KGs



The example graph





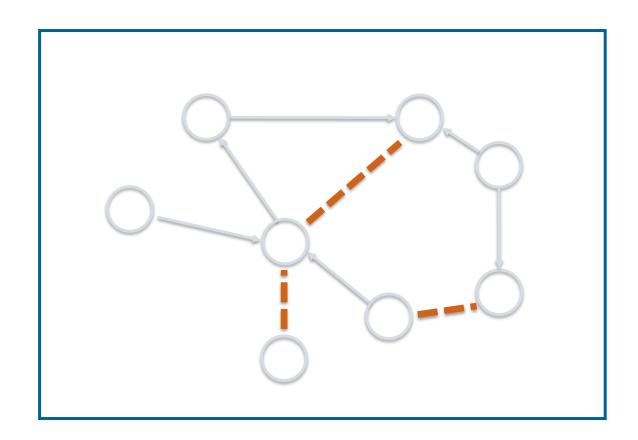
The big picture of building IT architectures for KGs



The example graph



Millions of companies





The big picture of building IT architectures for KGs



The example graph

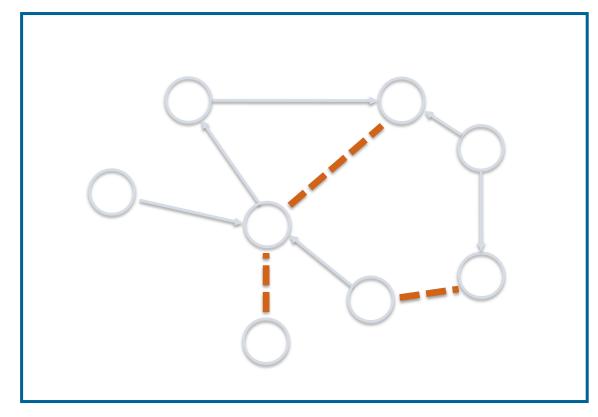


Millions of companies



10.000+ TPS(transactions per second)







The big picture of building IT architectures for KGs



The example graph

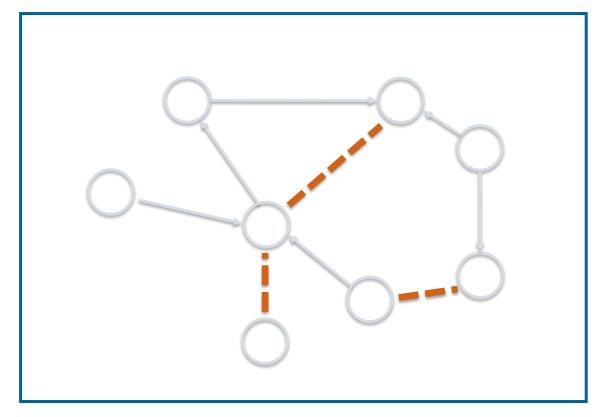


Millions of companies



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ArchitecturesThe big picture of building

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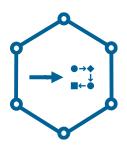
Millions of companies

10.000+ TPS (transactions per second)

Scal Makin

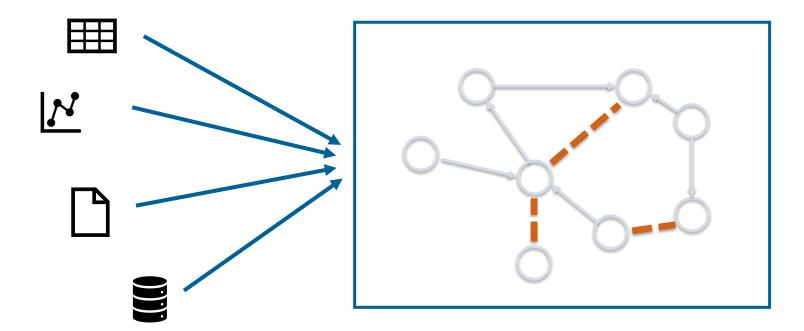
Scalable Reasoning

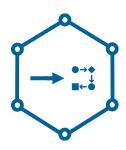
Making use of the knowledge in the KG



KG Creation

How to create a KG from heterogeneous data?





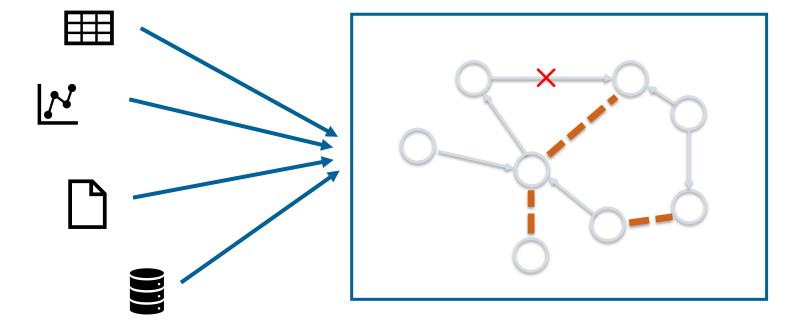
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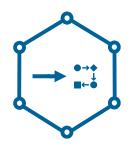
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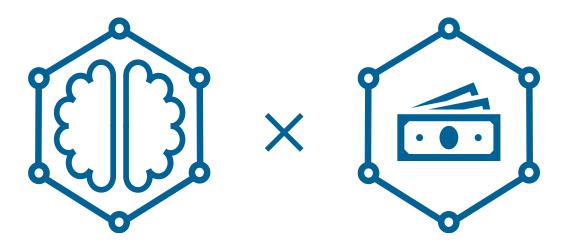
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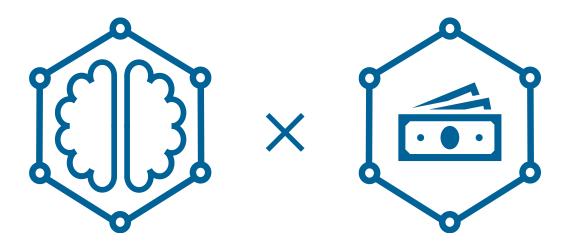
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Overview Applications

With Financial KGs as a Running Example

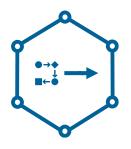
Applications



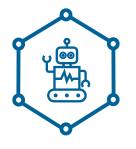
Real-World ApplicationsOverview of diverse applications



Financial KGs
Concrete applications in finance and economics



ServicesWhich service to provide based on KGs?



Connections.. between KGs, Al, ML and Data Science.

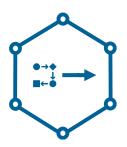
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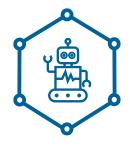
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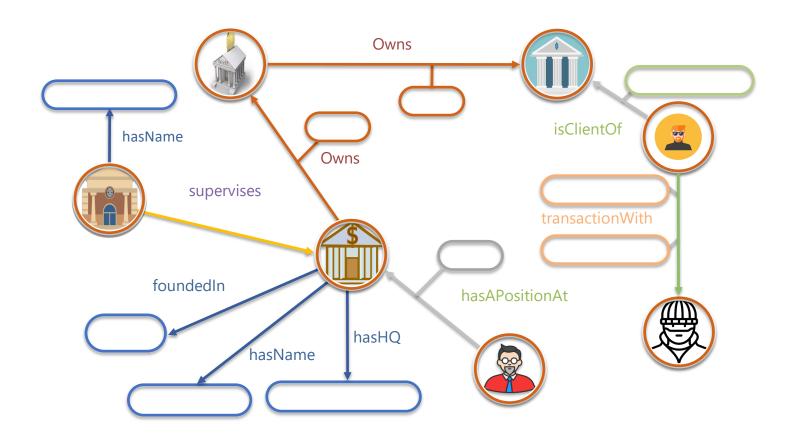
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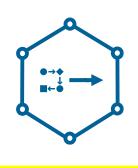
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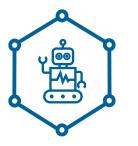
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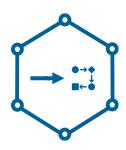
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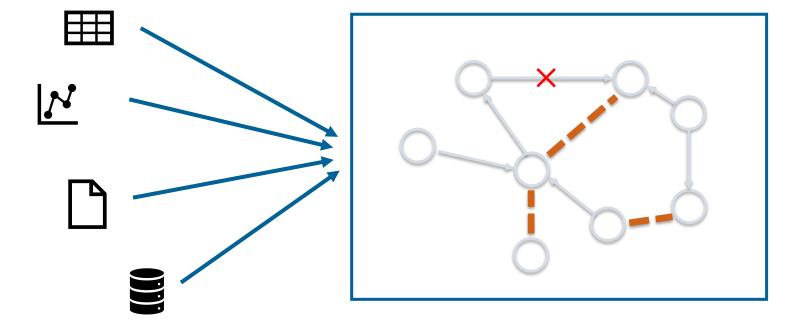
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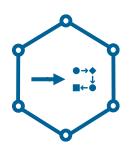
How to create a KG from heterogeneous data?



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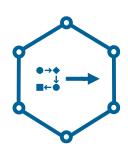
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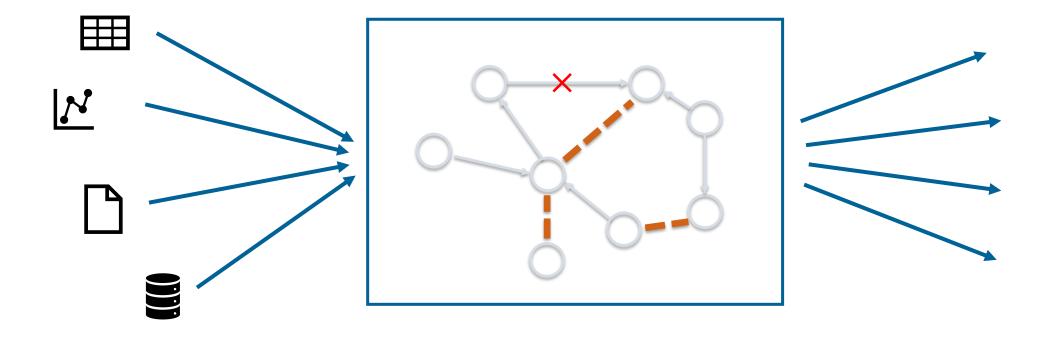
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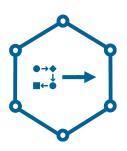
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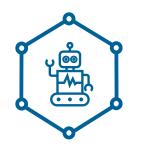
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Data Science

Artificial Intelligence

Knowledge Graphs

Machine Learning

Neural Networks

Deep Learning

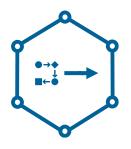
Applications



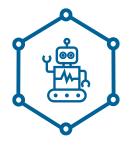
Real-World ApplicationsOverview of diverse applications



Financial KGs
Concrete applications in finance and economics



ServicesWhich service to provide based on KGs?

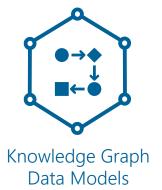


Connections.. between KGs, Al, ML and Data Science.

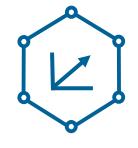


Representations









Knowledge Graph Embeddings



Logical Knowledge



Graph Neural Networks

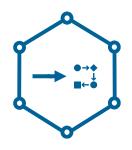
Systems



ArchitecturesThe big picture of building IT architectures for KGs



Scalable ReasoningMaking use of the knowledge in the KG



KG CreationHow to create a KG from heterogeneous data?



KG EvolutionHow to update, correct and complete a KG?

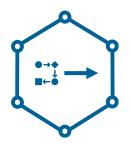
Applications



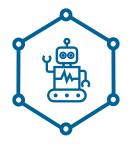
Real-World ApplicationsOverview of diverse applications



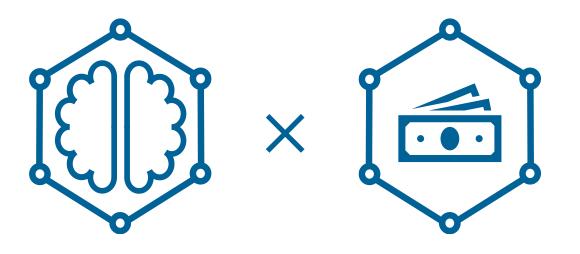
Financial KGs
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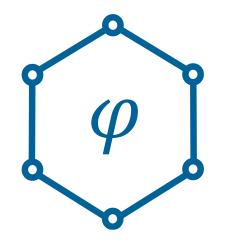
Connections.. between KGs, Al, ML and Data Science.



Overview Applications

With Financial KGs as a Running Example

Emanuel Sallinger



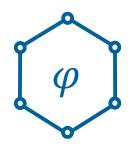
Logical Knowledge in KGs

Emanuel Sallinger

Representations



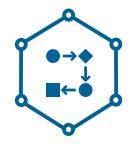
KG EmbeddingsWidely-applied, large family of ML models



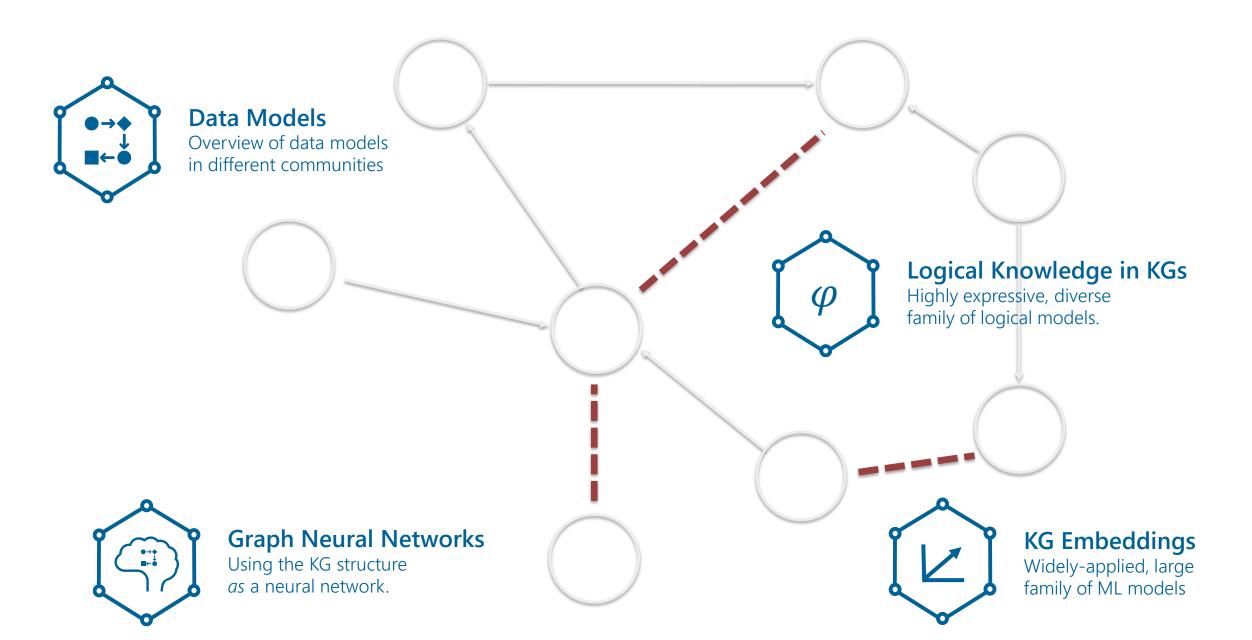
Logical Knowledge in KGs Highly expressive, diverse family of logical models.

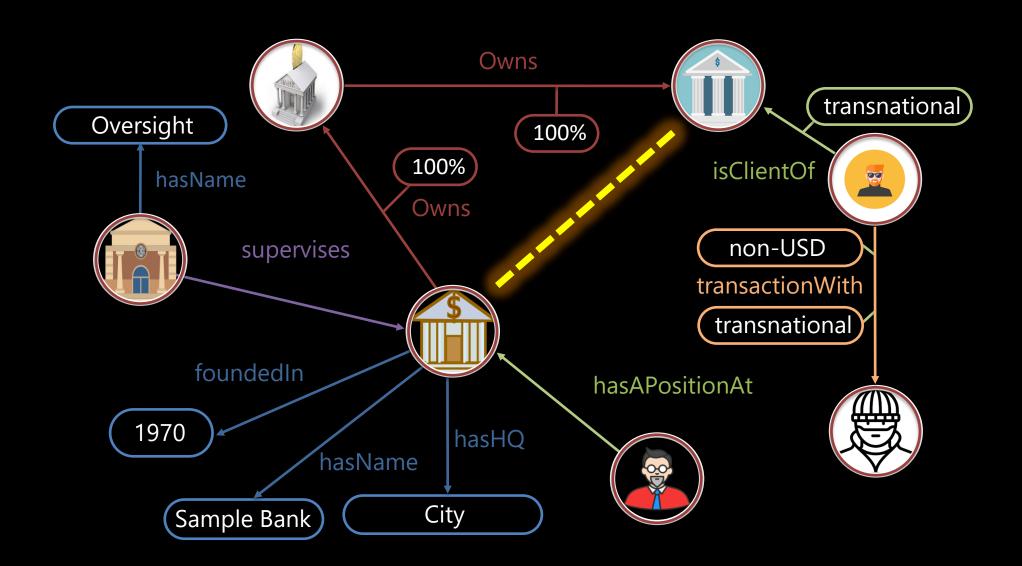


Graph Neural NetworksUsing the KG structure
as a neural network.



Data ModelsOverview of data models in different communities







Representations









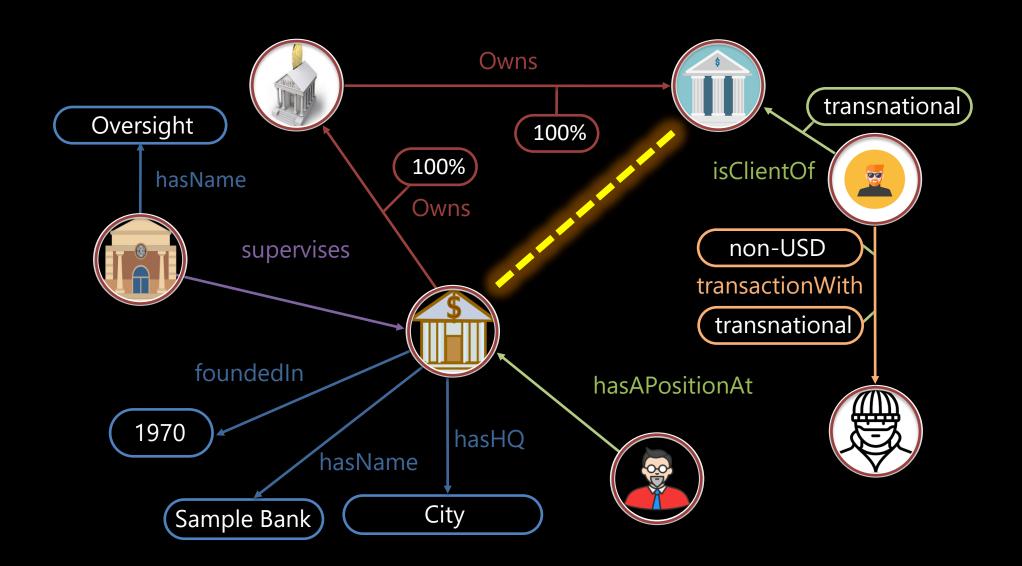
Knowledge Graph Embeddings



Logical Knowledge

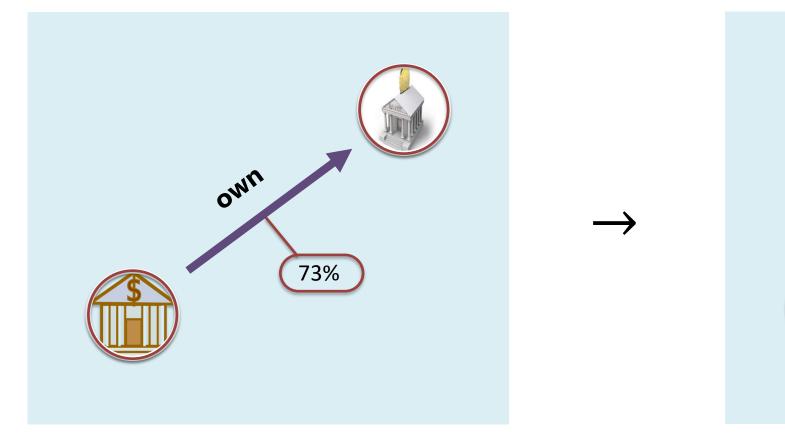


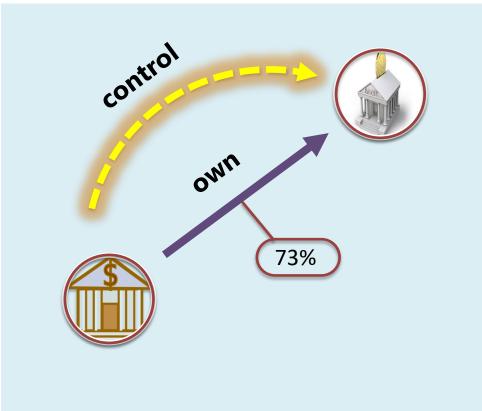
Graph Neural Networks



First-order Logic

 $\forall x, y \ (own(x, y, w), w > 0.5 \rightarrow control(x, y))$





Datalog

control(X,Y) :- own(X,Y,W), W > 0.5.

SQL

SELECT x,y INTO control FROM company WHERE w > 0.5

Relational Calculus

$$control = \{(x, y) \mid own(x, y, w), w > 0.5 \}$$

Relational Algebra

$$control = \sigma_{w>0.5} \ own$$

```
x controls y if x directly holds over 50% of y
```

Cypher (Graph DBs)

```
MATCH (x:Company) -[o:OWN]-> (y:Company)]
WHERE o.w > 0.5
CREATE (x) -[:CONTROL]-> (y)
```

.. Cypher

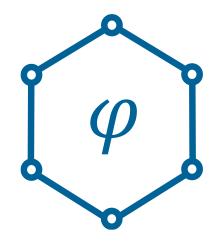
SPARQL

Datalog

SQL

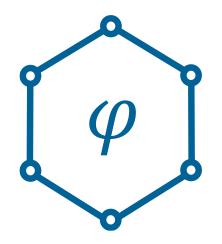
First-order Logic

Relational Algebra



Logical Knowledge in KGs

Emanuel Sallinger



Logical Knowledge in KGs

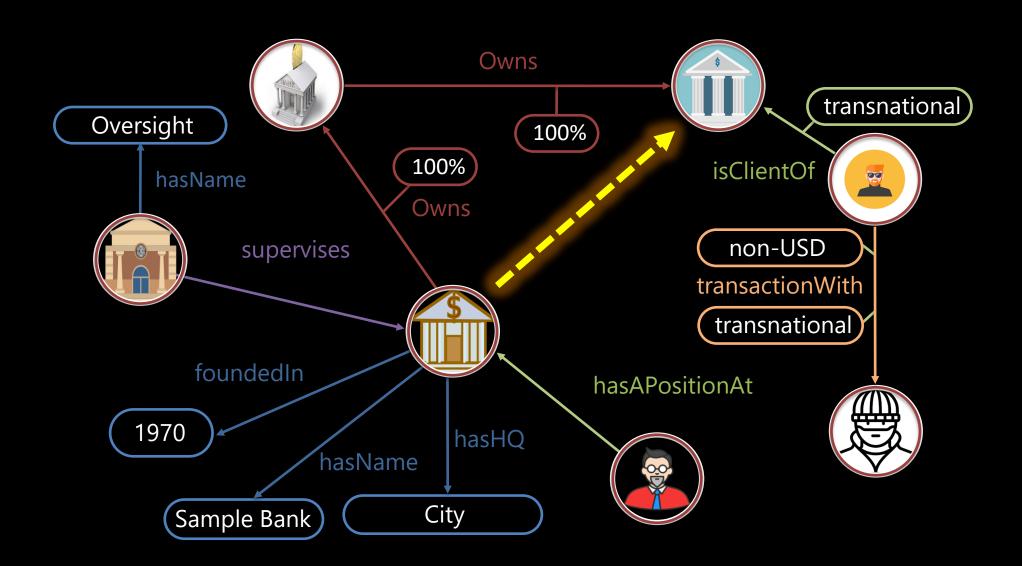
Challenges: Recursion and Creation

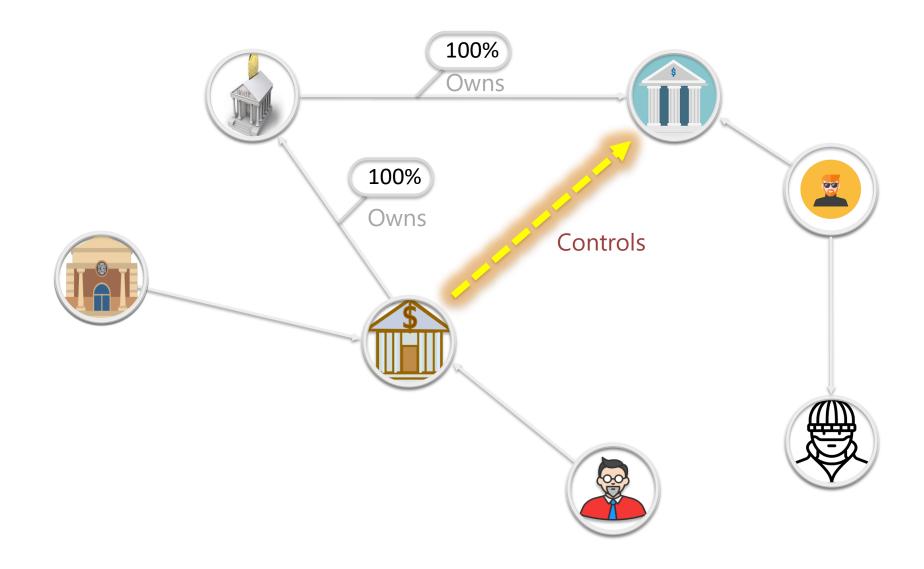
Emanuel Sallinger

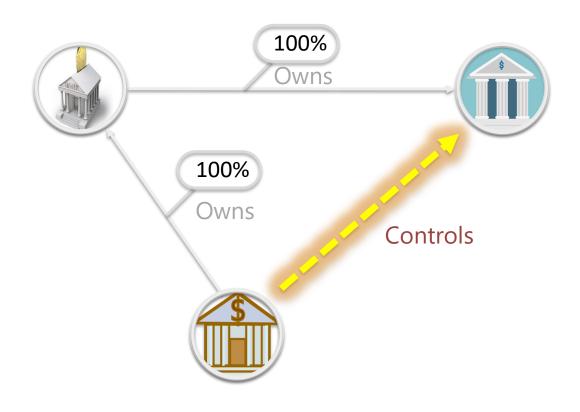


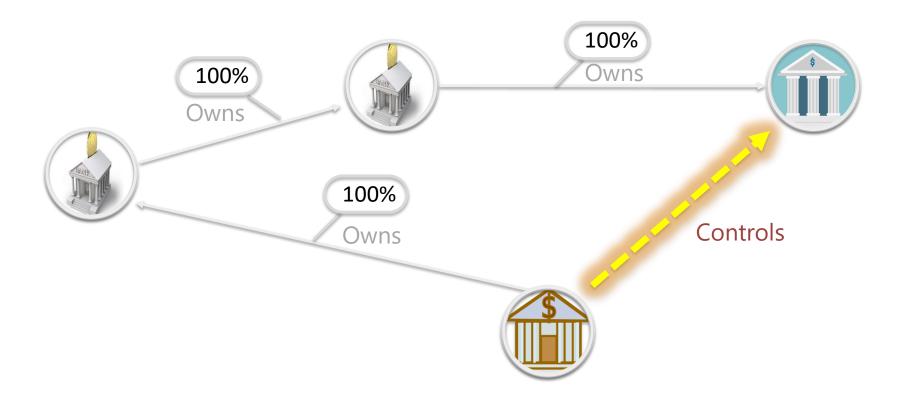
Main Challenges

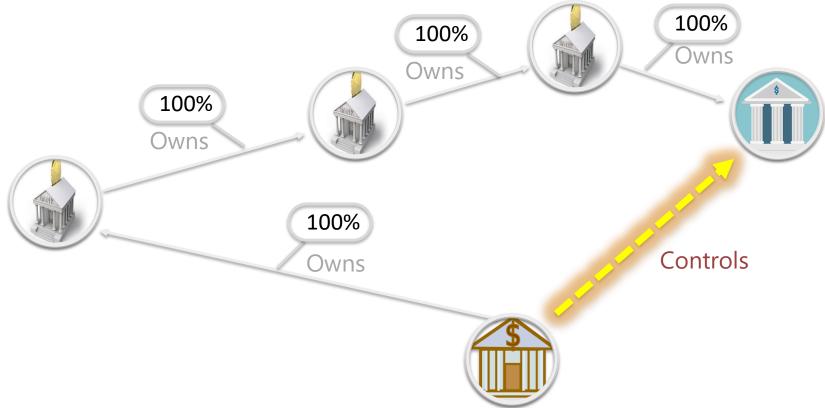
- 1. **Recursion**unlimited graph exploration
- 2. **Object Creation** *exploring unknown parts of the KG*

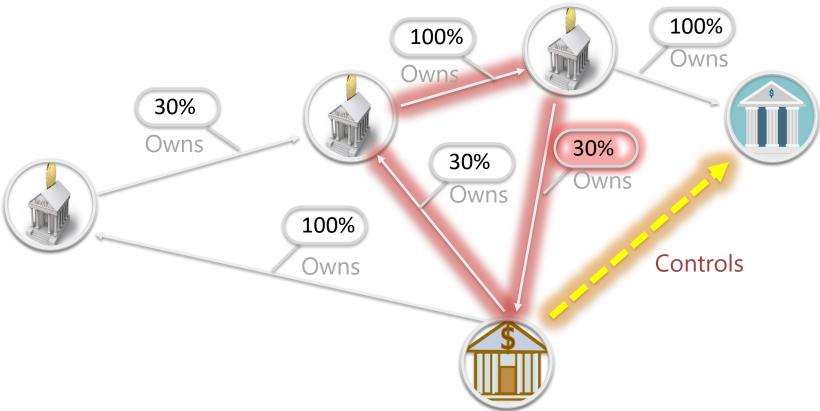




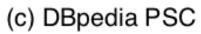


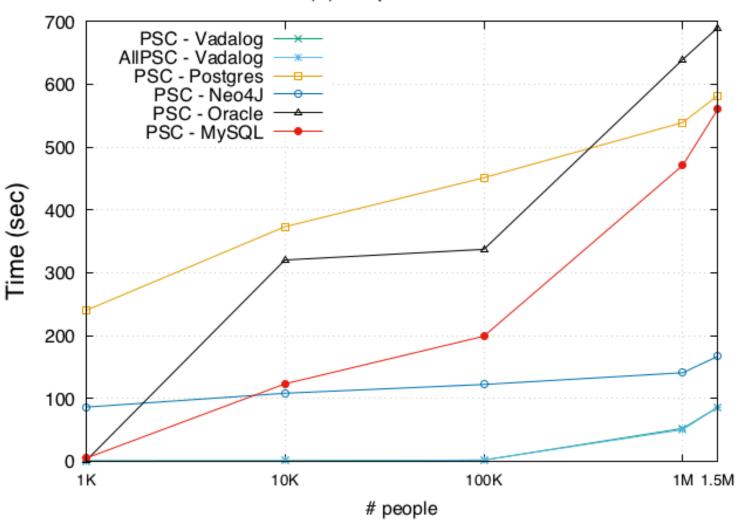






x controls a set S of companies that jointly control y

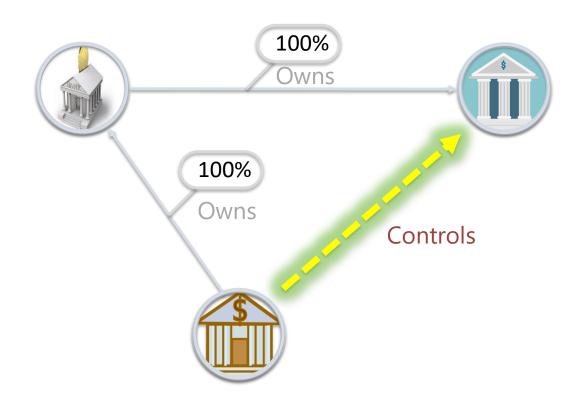


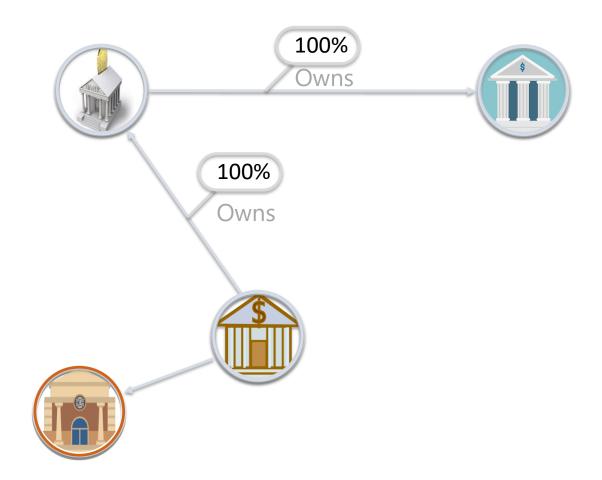


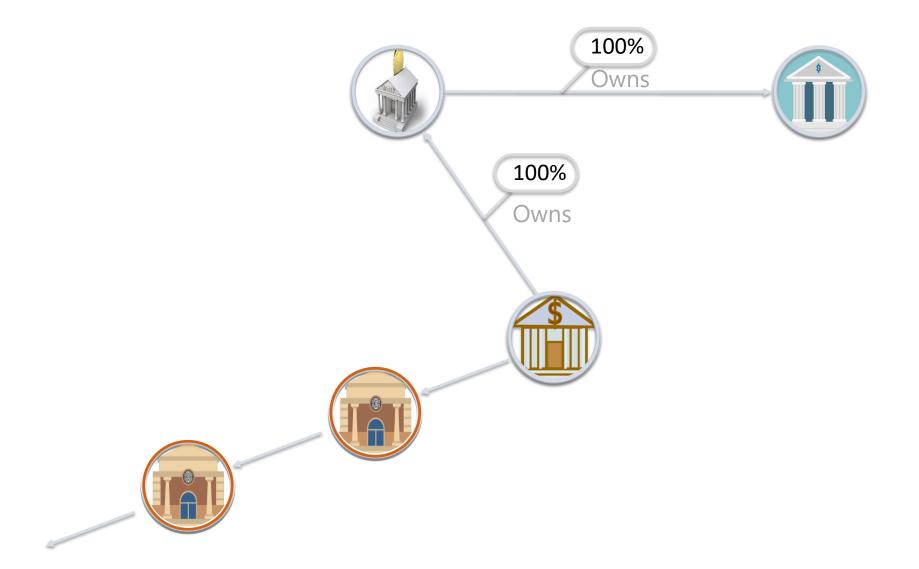


Main Challenges

- 1. **Recursion**unlimited graph exploration
- 2. **Object Creation** *exploring unknown parts of the KG*







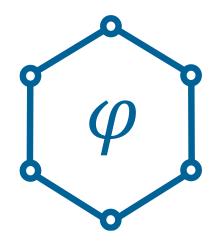
x controls y if x directly holds over 50% of y, or x controls a set S of companies that jointly control y



Main Challenges

- 1. **Recursion**unlimited graph exploration
- 2. **Object Creation** *exploring unknown parts of the KG*

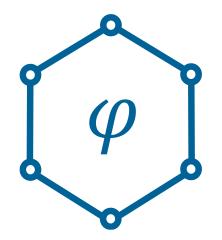
Query answering under recursive Datalog with object creation (existential quantification) is undecidable.



Logical Knowledge in KGs

Challenges: Recursion and Creation

Emanuel Sallinger



Logical Knowledge in KGs

Recursion in Datalog

Primer

Emanuel Sallinger

SQL

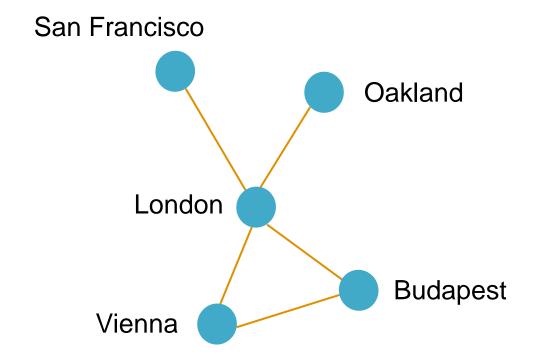
```
WITH RECURSIVE temp AS (
    SELECT * FROM flight
UNION ALL
    SELECT t.Origin, f.Destination
    FROM temp t, flight f
    WHERE t.Destination = f.Origin
)
```

SELECT * INTO connection FROM temp

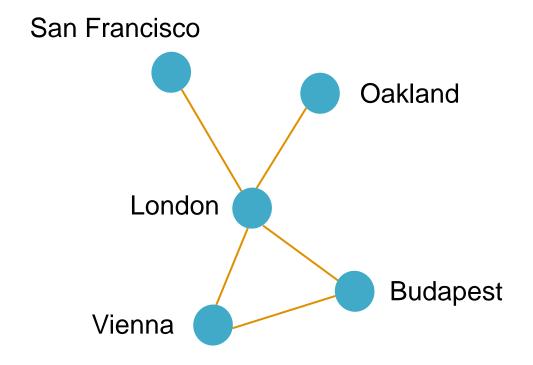
Datalog

```
connection(X,Y) :- flight(X,Y,_).
connection(X,Z) :- connection(Y,Z), flight(X,Y,_).
```

San Francisco Oakland London Budapest



IATA	City
VIE	Vienna
LHR	London
LGW	London
BUD	Budapest
OAK	Oakland
SFO	San Francisco



Origin	Destination	Airline
VIE	LHR	ВА
LHR	SFO	ВА
LGW	OAK	DI
BUD	VIE	OS

IATA	City
VIE	Vienna
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SFO	San Francisco



airport

city

IATA	City	
VIE	Vienna	
LHR	London	
SFO	San Francisco	



City
Vienna
London
San Francisco





SQL

SELECT City INTO city FROM airport





SQL

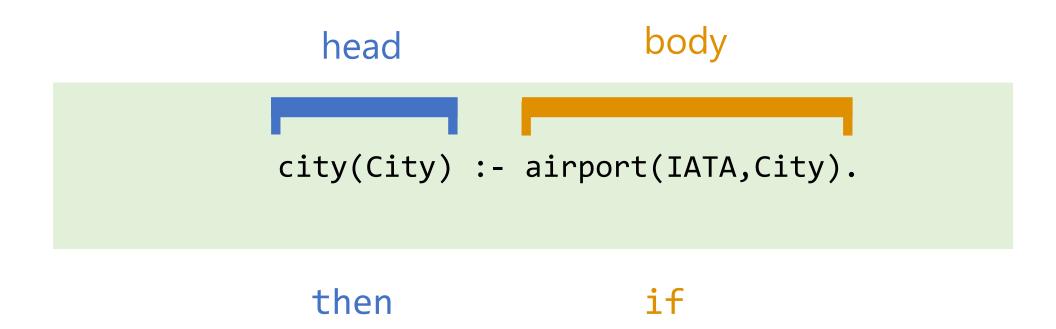
SELECT City INTO city FROM airport

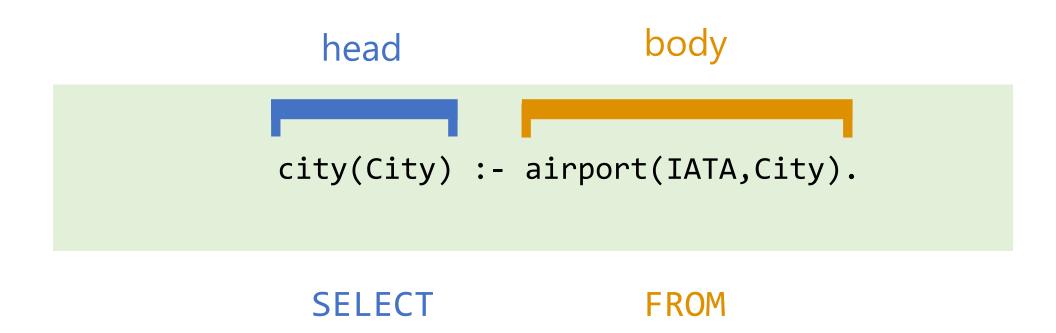
Datalog

city(City) :- airport(IATA,City).

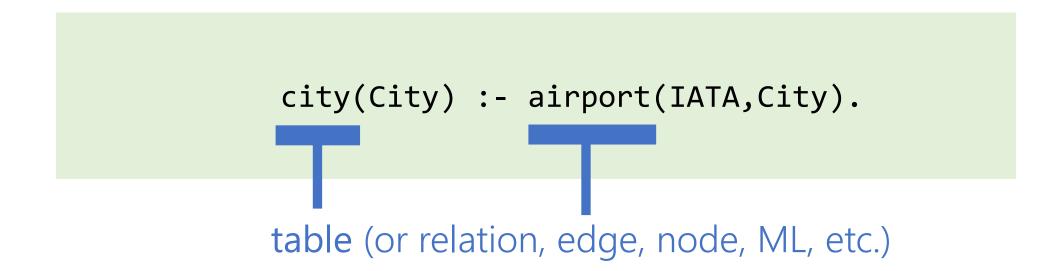
city(City) :- airport(IATA,City).

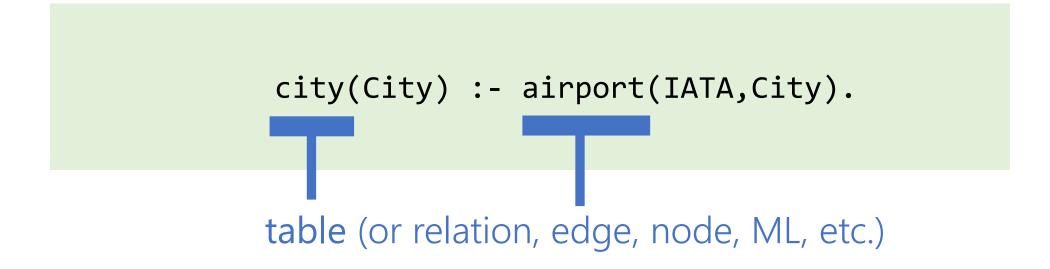




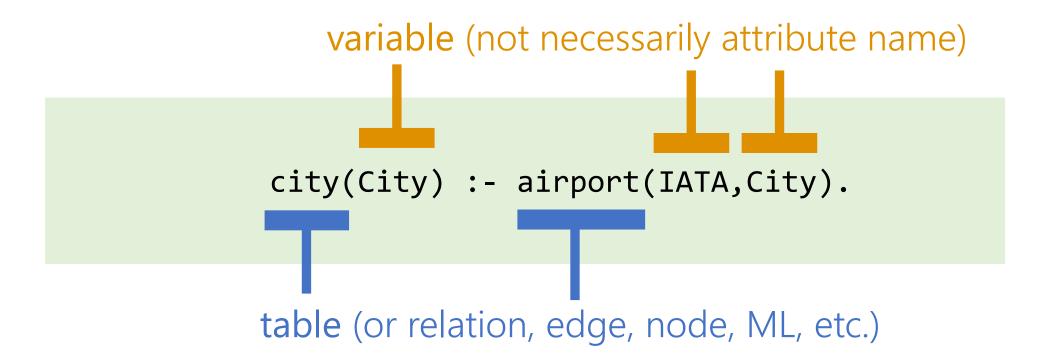


city(City) :- airport(IATA,City).



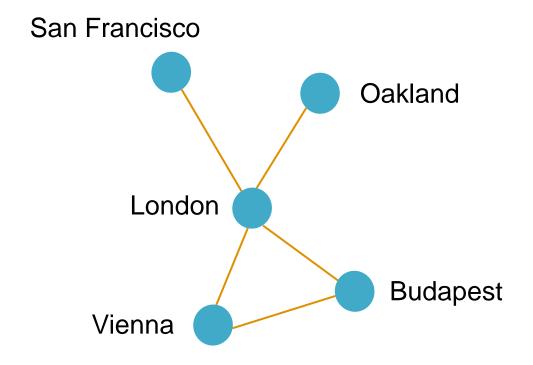


SELECT City INTO city FROM airport



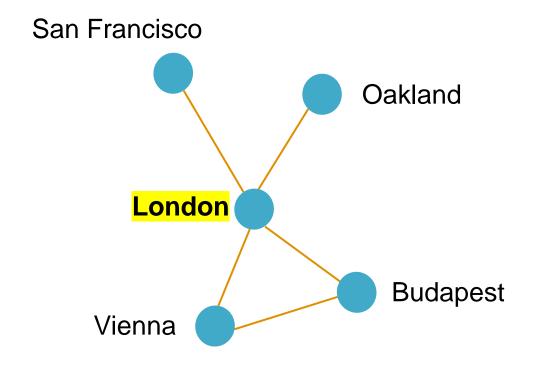
SELECT City INTO city FROM airport

city(X) :- airport(X , Y). table (or relation, edge, node, ML, etc.)



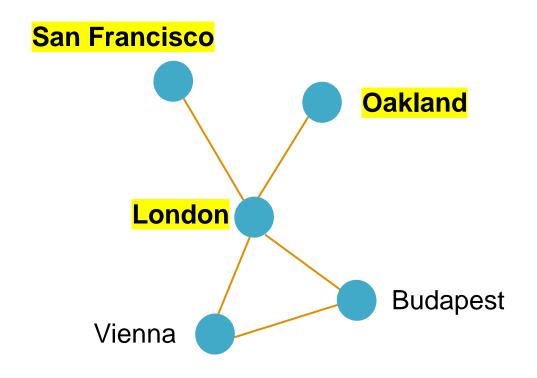
Origin	Destination	Airline
VIE	LHR	ВА
LHR	SFO	ВА
LGW	OAK	DI
BUD	VIE	OS

IATA	City
VIE	Vienna
LHR	London
LGW	London
BUD	Budapest
OAK	Oakland
SFO	San Francisco



Origin	Destination	Airline
VIE	LHR	ВА
LHR	SFO	ВА
LGW	OAK	DI
BUD	VIE	OS

IATA	City	
VIE	Vienna	
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Origin	Destination	Airline
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SFO	San Francisco	

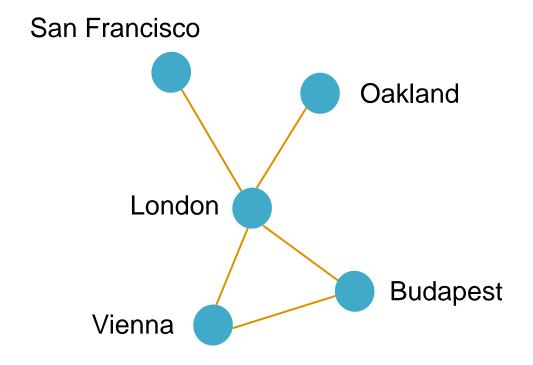
join

```
dest(D) :- flight(L,D,A), airport(L,"London").
```

```
SELECT f.Destination INTO dest
FROM flight f, airport a
WHERE f.Origin = a.IATA AND a.City = "London"
```

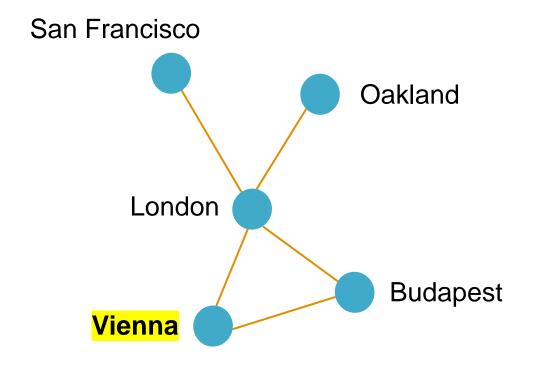
join

```
SELECT f.Destination INTO dest
FROM flight f, airport a
WHERE f.Origin = a.IATA AND a.City = "London"
```



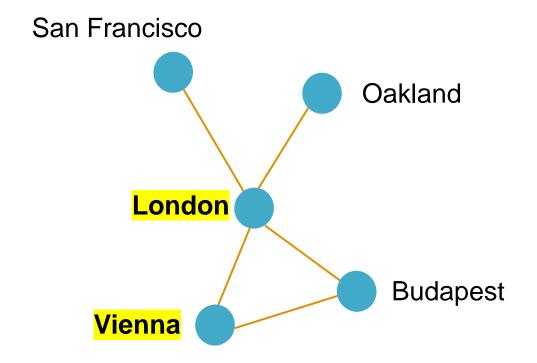
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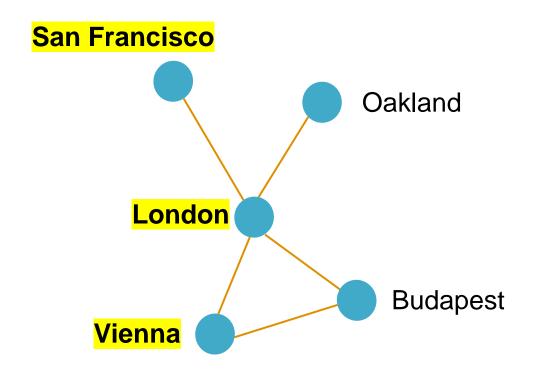
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Origin	Destination	Airline
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Origin	Destination	Airline
<mark>VIE</mark>	<mark>LHR</mark>	ВА
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LGW	OAK	DI
BUD	VIE	OS

IATA	City
VIE	Vienna
LHR	London
LGW	London
BUD	Budapest
OAK	Oakland
SFO	San Francisco

SQL

```
WITH RECURSIVE temp AS (
   SELECT * FROM flight
UNION ALL
   SELECT t.Origin, f.Destination
   FROM temp t, flight f
   WHERE t.Destination = f.Origin
SELECT * INTO connection FROM temp
```

Datalog

```
connection(X,Y) :- flight(X,Y,_).
connection(X,Z) :- connection(Y,Z), flight(X,Y, ).
```

Syntax of Datalog

A datalog rule is an expression of the form

$$R_1(x_1) : -R_2(x_2), ..., R_n(x_n).$$

where R_i are relation names and x_i are lists of variable names.

- Each variable in x_1 must occur in at least one of x_2, \dots, x_n .
- A datalog programme is a finite set of datalog rules.





Semantics of Datalog

- Various semantics are possible:
 - Model-theoretic semantics
 - Fixpoint semantics
 - Proof-theoretic semantics
- Important tool: The "chase" procedure
 - Informally, starting with a database and applying rules to generate new tuples.

• More than we can cover here. For the interested:



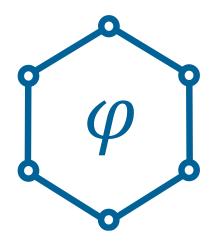
Datalog

```
connection(X,Y) :- flight(X,Y,_).
connection(X,Z) :- connection(Y,Z), flight(X,Y,_).
```

First-order Logic

```
\forall X, Y, U \ (connection(X, Y) \leftarrow flight(X, Y, U))
\forall X, Y, Z, U \ connection(X, Z) \leftarrow connection(Y, Z) \land flight(X, Y, U)
```

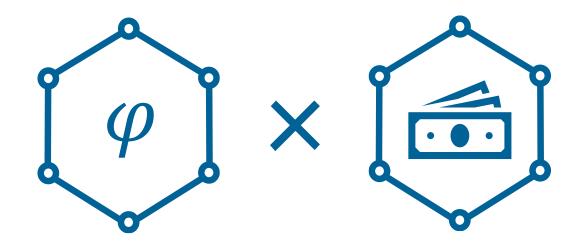




Logical Knowledge in KGs Recursion in Datalog

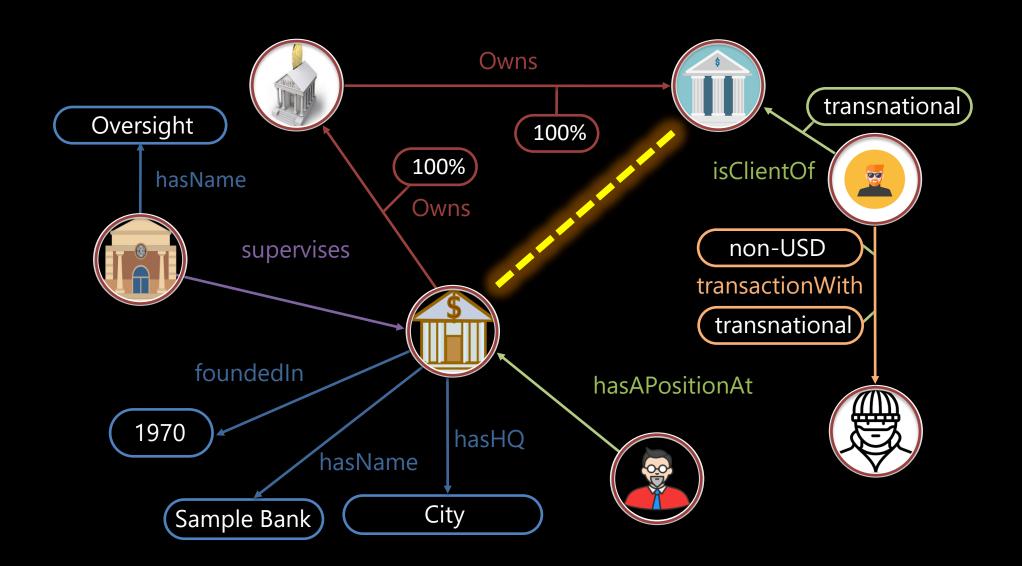
Primer

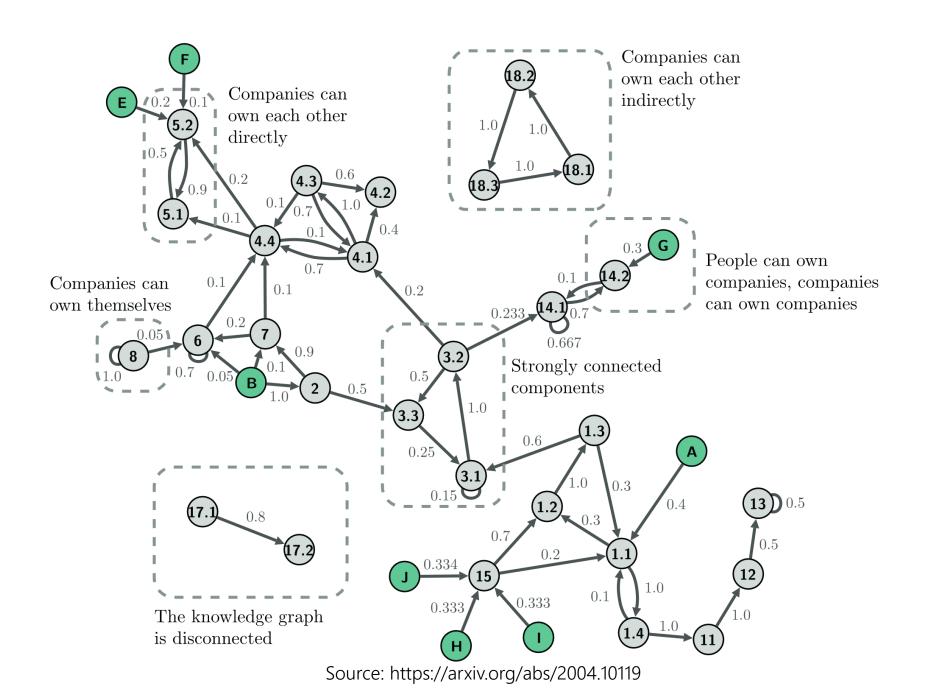
Emanuel Sallinger

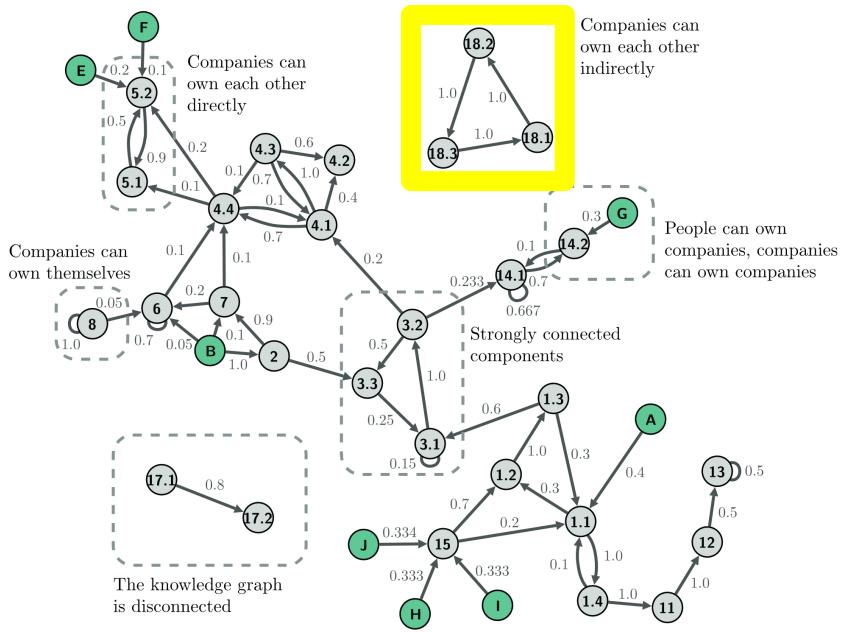


Logical Knowledge in KGs Recursion in the Real World

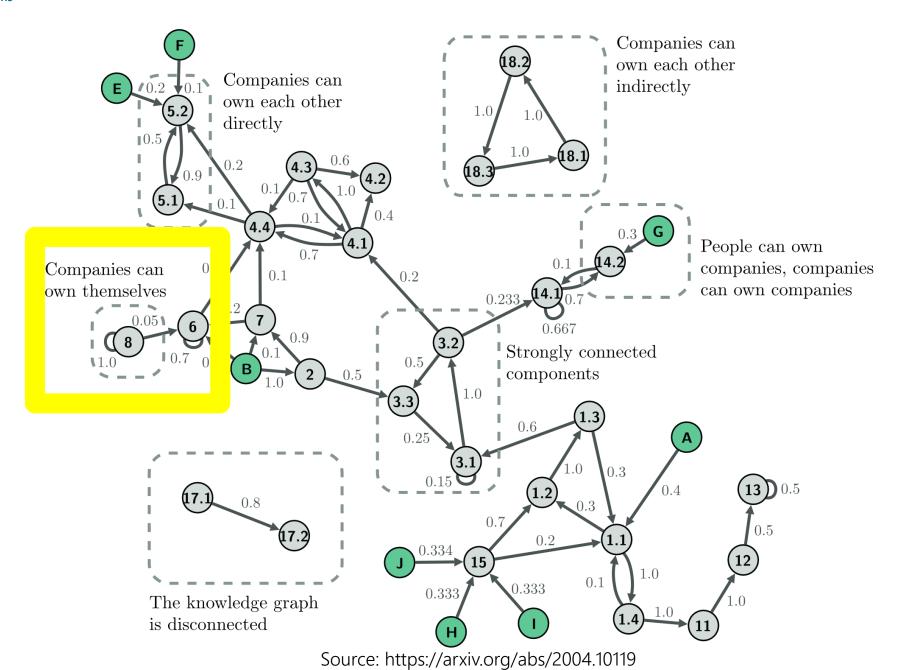
Emanuel Sallinger

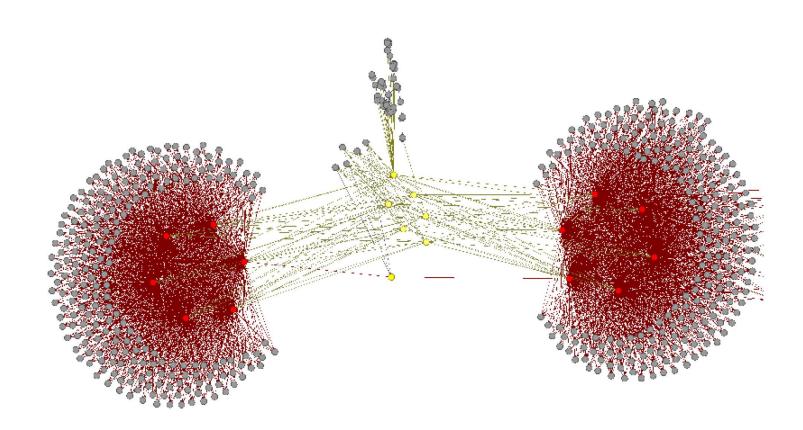


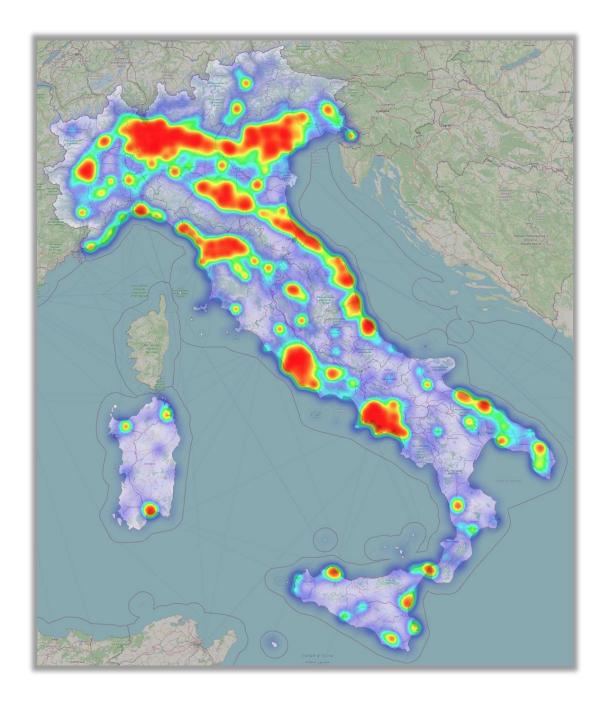




Source: https://arxiv.org/abs/2004.10119

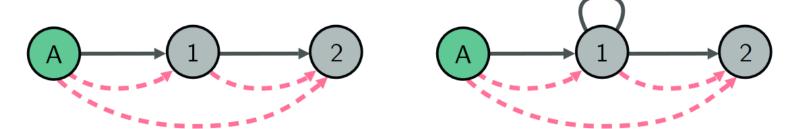






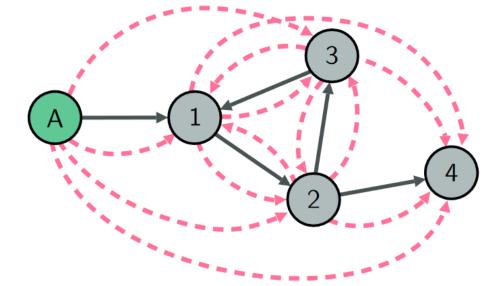
Ownership and Control

Ownership



(a) A simple indirect ownership.

(b) Indirect ownership with a self-loop.



(c) Indirect ownership with a strongly connected component.

Ownership

Definition 1. An ϵ -Baldone path P from s to t is a path $[s, p_1, \ldots, p_n, t]$ such that $s \neq p_i$ for $i = 1, \ldots, n$ and $w(P) > \epsilon$, with $\epsilon \in \mathbb{R}^+$ and $0 < \epsilon \leq 1$. We denote the weight of an ϵ -Baldone path as $w_{\epsilon}(P)$.

Definition 2. The ϵ -Baldone ownership of a company s on a company t in a graph G is a function $O_{\epsilon}^{G}(s,t):(N\times N)\to\mathbb{R}^{+}\cup\{\infty\}$ defined as $(s,t)\to\sum_{P_{i}\in B_{\epsilon}}w_{\epsilon}(P_{i})$, where B_{ϵ} is the set of all possible ϵ -Baldone paths from s to t.

Definition 3. The Baldone ownership (which we will also refer to as integrated ownership) of a company s on a company t in a graph G is a function $O^G(s,t)$: $(N \times N) \to \mathbb{R} \cup \{\infty\}$ defined as $(s,t) \to \lim_{\epsilon \to 0} O_{\epsilon}(s,t)$.

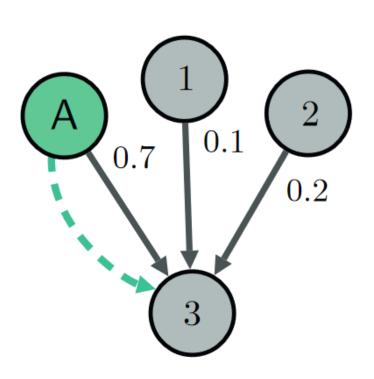


$$Own(x, y, w), w > \epsilon, v = sum(w), p = [x, y] \rightarrow IOwn(x, y, v, p).$$
(1)

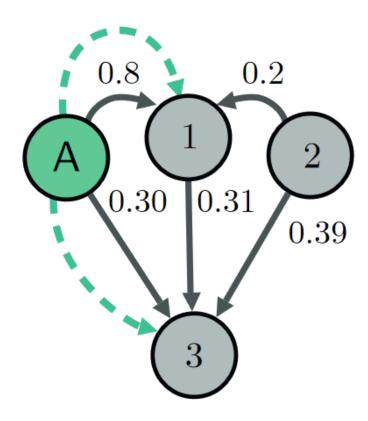
$$IOwn(x, z, w_1, p_1), IOwn(z, y, w_2, p_2), p = p_1|p_2, BaldonePath(p, v, \epsilon),$$

$$v = sum(w_1 \times w_2), \rightarrow IOwn(x, y, v, p).$$
(2)

Control



(a) Direct control.



(b) Indirect control.

Control

Definition 4. A company (or a person) x controls a company y, if: (i) x directly owns more than 50% of y; or, (ii) x controls a set of companies that jointly (i.e., summing the shares), and possibly together with x, own more than 50% of y.



$$Control(x) \to Control(x, x)$$
 (1)

 $Control(x, y), Own(y, z, w), v = msum(w, \langle y \rangle), v > 0.5 \rightarrow Control(x, z)$ (2)

Golden Power



Golden Power Check

Golden Power Check

Goal: The general goal is checking whether an acquisition (of shares,

stocks, etc.) causes any strategic Italian company to become con-

trolled by a foreign company.

Setting: Let S be a set of strategic companies and F be a set of foreign com-

panies. Let t be a transaction (e.g., an offer issued by a company

x to buy an amount s of shares of a company y), with $x, y \in S \cup F$.

Question: Decide whether t causes any company in F to control a company

in S.

Insight: Consider exerting "golden power" to block t.

Golden Power Check

Golden Power Check

Goal: The general goal is checking whether an acquisition (of shares,

stocks, etc.) causes any strategic Italian company to become con-

trolled by a foreign company.

Setting: Let S be a set of strategic companies and F be a set of foreign com-

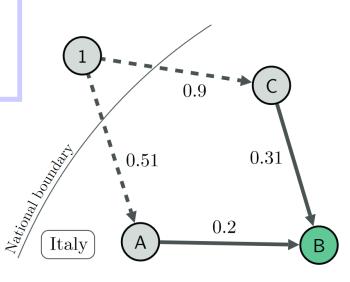
panies. Let t be a transaction (e.g., an offer issued by a company

x to buy an amount s of shares of a company y), with $x, y \in S \cup F$.

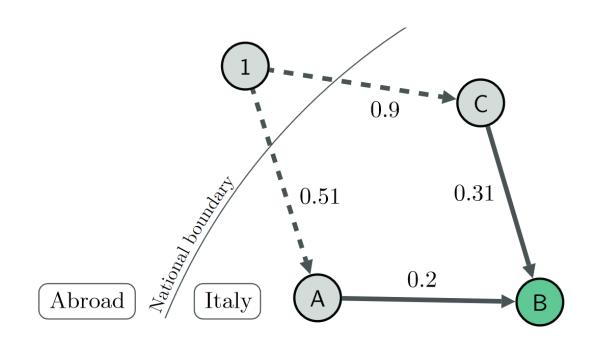
Question: Decide whether t causes any company in F to control a company

in S.

Insight: Consider exerting "golden power" to block t.



Golden Power Check

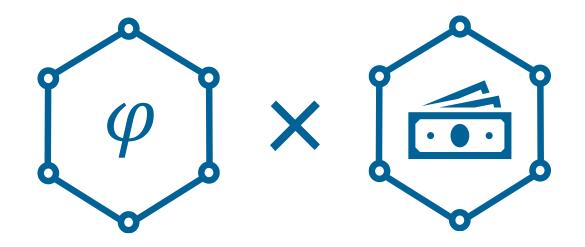


$$T(x, y, w) \rightarrow Own(x, y, w)$$
 (1)

$$Control(x, y) \to Control(x, x)$$
 (2)

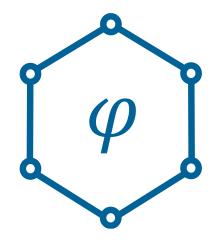
$$Control(x, y), Own(y, z, w), v = msum(w, \langle y \rangle), v > 0.5 \rightarrow Control(x, z)$$
 (3)

$$F(x), S(y), Control(x, y) \rightarrow GPCheck(x, y)$$
 (4)



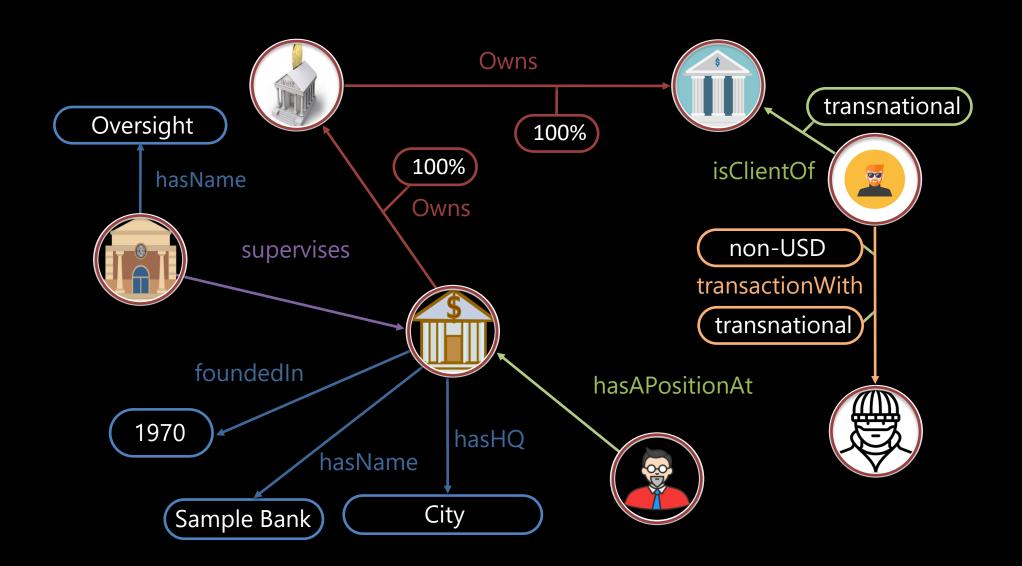
Logical Knowledge in KGs Recursion in the Real World

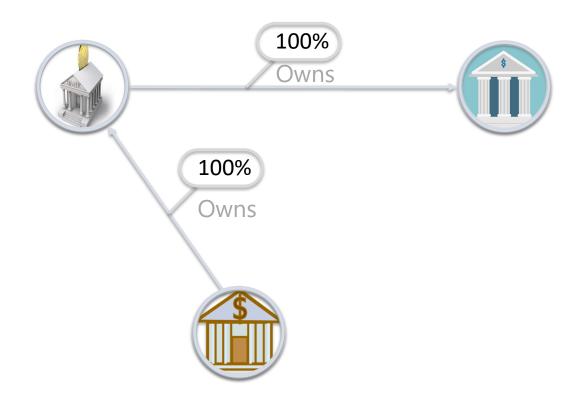
Emanuel Sallinger

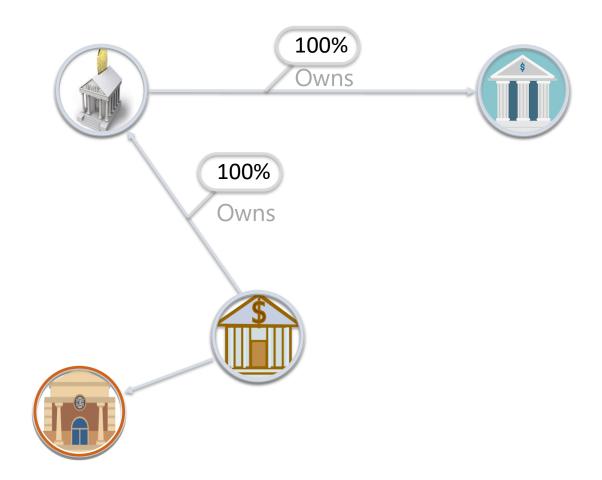


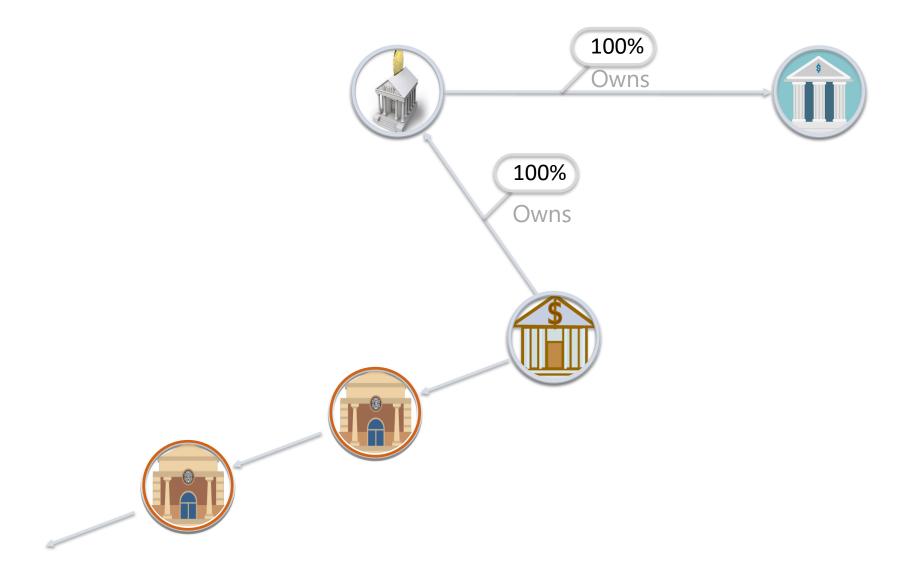
Logical Knowledge in KGs Creation

Emanuel Sallinger







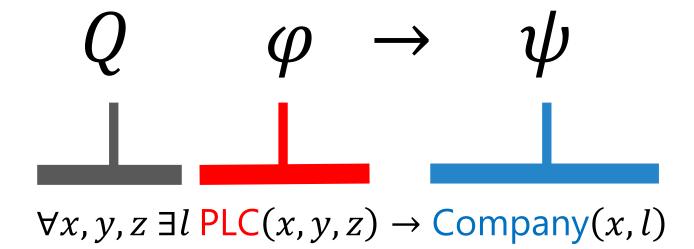


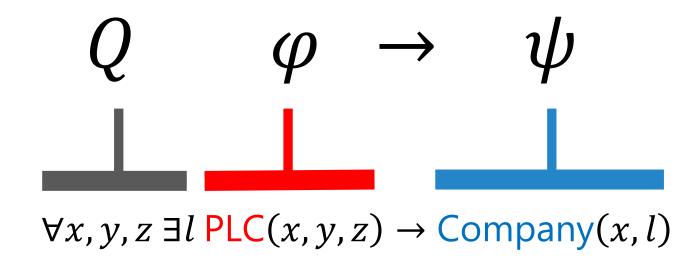
PLC(HSBC, UK, London) → Company(HSBC)

$$\forall x, z \ \mathsf{PLC}(x, \mathsf{UK}, z) \to \mathsf{Company}(x)$$

$$\forall x, y, z \ \mathsf{PLC}(x, y, z) \to \mathsf{Company}(x)$$

 $\forall x, y, z \ \mathsf{PLC}(x, y, z) \to \exists l \ \mathsf{Company}(x, l)$





Knowledge

"Dependency"

"Rule"

"Logical Formula"

"Ontology Axiom"

"Constraint"

"Named Query"

CREATE SEQUENCE locationSequence;

SELECT id, nextval('locationSequence')
INTO Company FROM PLC

Company(C,L) :- PLC(X,Y,C).

Recall

SQL: **NULL**

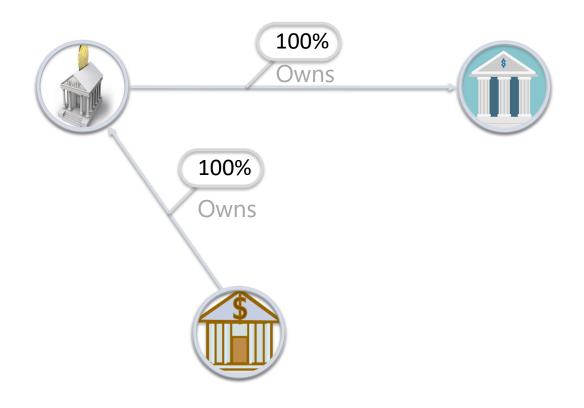
v IS [NOT] NULL

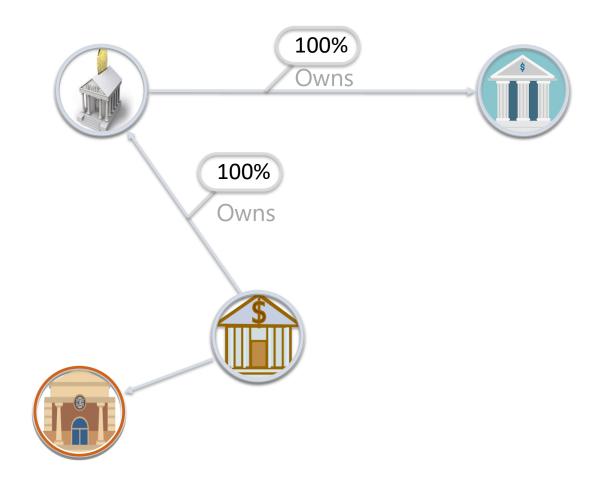
- NULL indicates an "unknown" value
 - many applications (not applicable, not existent, ...)
 - often misused
- NULL is different from any other value, including itself
 - NULL = NULL is not true!
 - to test for null, use IS [NOT] NULL

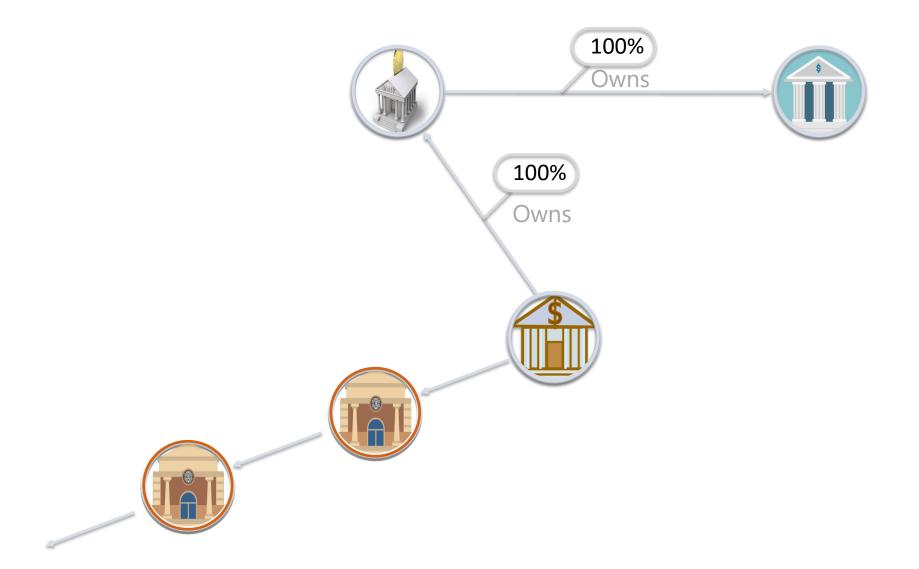
Recall

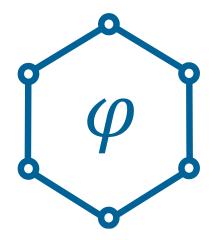
SQL: **NULL**

φ	ψ	φ AND ψ	φ OR ψ	NOT φ
true	true	true	true	false
true	false	false	true	false
true	null	null	true	false
false	true	false	true	true
false	false	false	false	true
false	null	false	null	true
null	true	null	true	null
null	false	false	null	null
null	null	null	null	null



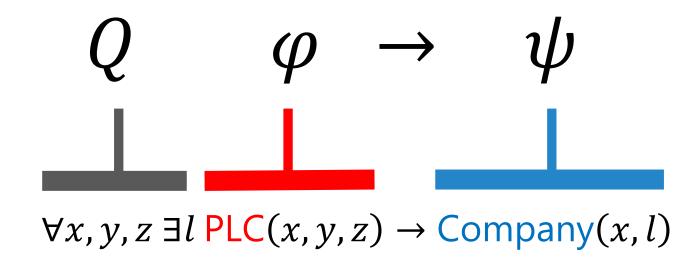






Logical Knowledge in KGs Warded and Vadalog

Emanuel Sallinger



Knowledge

"Dependency"

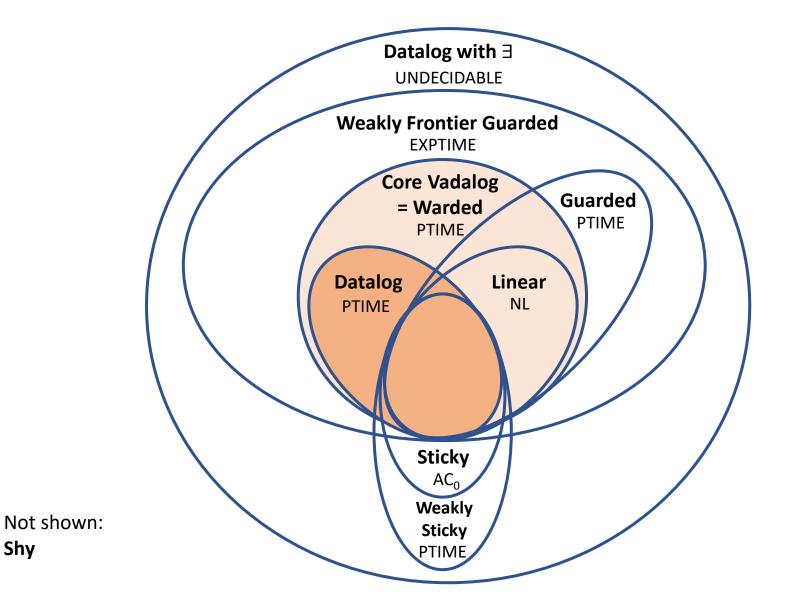
"Rule"

"Logical Formula"

"Ontology Axiom"

"Constraint"

"Named Query"





Language Requirements

- Recursive Reasoning:
 Full support of recursive Datalog
- Ontological Reasoning:Expressive power of SPARQL and OWL 2QL
- 3. **Tractable** Reasoning: **polynomial time**, sub-fragments that are **fully parallelizable**

$$\operatorname{Emp}(x) \to \exists z \operatorname{Mgr}(x, z) \operatorname{Mgr}(x, y) \land \operatorname{Pers}(x) \to \operatorname{Emp}(y)$$

$$\operatorname{Emp}(x) \to \exists \mathbf{z} \operatorname{Mgr}(x, \mathbf{z}) \operatorname{Mgr}(x, y) \wedge \operatorname{Pers}(x) \to \operatorname{Emp}(y)$$



$$\operatorname{Emp}(x) \to \exists \mathbf{z} \operatorname{Mgr}(x, \mathbf{z}) \operatorname{Mgr}(x, \mathbf{y}) \wedge \operatorname{Pers}(x) \to \operatorname{Emp}(\mathbf{y})$$



Dangerous

$$\operatorname{Emp}(x) \to \exists \mathbf{z} \operatorname{Mgr}(x, \mathbf{z}) \operatorname{Mgr}(x, \mathbf{y}) \wedge \operatorname{Pers}(x) \to \operatorname{Emp}(\mathbf{y})$$



Dangerous



1. all the "dangerous" variables should coexist in a single body-atom α , called the ward



Harmless

$$\operatorname{Emp}(x) \to \exists \mathbf{z} \operatorname{Mgr}(x, \mathbf{z})$$
 $\operatorname{Mgr}(x, \mathbf{y}) \land \operatorname{Pers}(x) \to \operatorname{Emp}(\mathbf{y})$
Ward

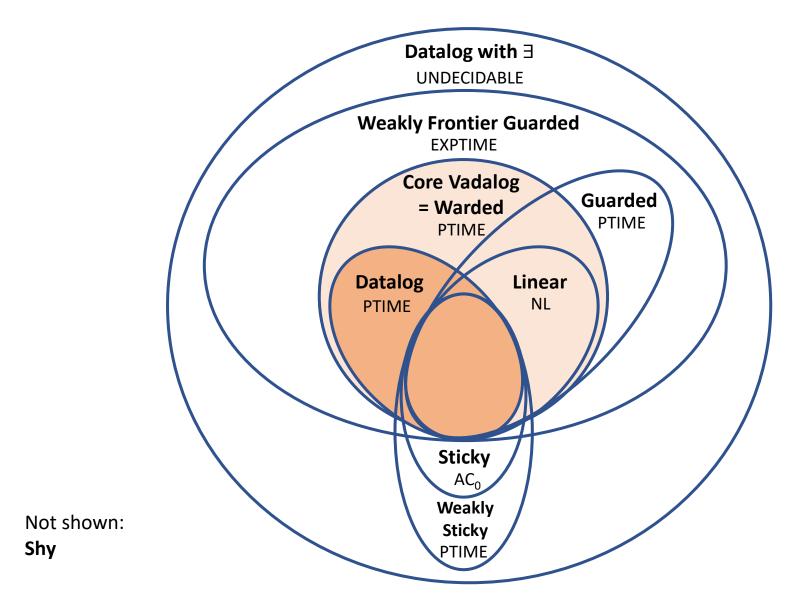
- 1. all the "dangerous" variables should coexist in a single body-atom α , called the ward
- 2. the ward can share only "harmless" variables with the rest of the body



Harmless $Emp(x) \rightarrow \exists \mathbf{z} \, Mgr(x, \mathbf{z}) \quad Mgr(x, \mathbf{y}) \, \wedge \, Pers(x) \rightarrow Emp(\mathbf{y})$

Ward

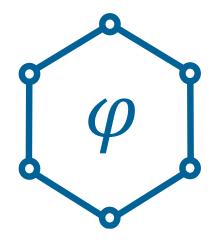
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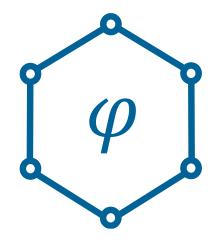


Main Challenges

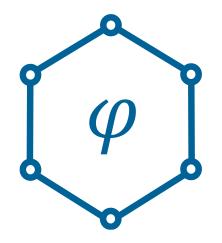
- 1. **Recursion**unlimited graph exploration
- 2. **Object Creation** *exploring unknown parts of the KG*



Logical Knowledge in KGs Warded and Vadalog



Logical Knowledge in KGs Creation



Logical Knowledge in KGs

Vadalog – Interacting with the World

```
connection(X,Y) :- flight(X,Y).
connection(X,Z) :- connection(Y,Z), flight(X,Y).
```

```
flight("VIE","LHR","BA").
flight("LHR", "SFO", "BA").
flight("LGW","OAK","DI").
flight("BUD", "VIE", "OS").
connection(X,Y) := flight(X,Y).
connection(X,Z) :- connection(Y,Z), flight(X,Y).
```

```
flight("VIE","LHR","BA").
flight("LHR", "SFO", "BA").
flight("LGW","OAK","DI").
flight("BUD", "VIE", "OS").
connection(X,Y):- flight(X,Y).
connection(X,Z) :- connection(Y,Z), flight(X,Y).
@output("connection").
```

Binding

```
@input("flight ").
@bind("flight","postgres","mw_kg4","eflight").
```

Binding

```
@input("flight ").
@bind("flight","postgres","mw_kg4","eflight").
```

Query Binding

```
@qbind("flight","postgres","mw_kg_db6",
    "select O,D,F from TestTable
    where k_id between 394823 and 4458773").
```

Query Binding

```
@qbind("flight","postgres","mw_kg_db6",
    "select O,D,F from TestTable
    where k_id between 394823 and 4458773").
```

```
@qbind("atomName","data source",
    "outer container","query").
```



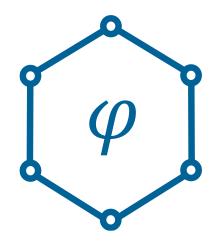
Query Binding



```
@qbind("flight", "mw_graph_db7",
"MATCH (a)-[o:Carrier]->(b)
  RETURN a,b,o.Carrier").
```

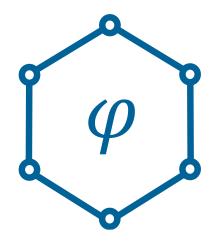
In- and Output Binding

```
flightOnly(X,Y) :- flight(X,Y,Z).
@input("flight ").
@bind("flight","csv","/d2","s1.csv").
@output("flightOnly").
@bind("flightOnly","csv","/d3","result.csv").
```



Logical Knowledge in KGs

Vadalog – Interacting with the World



Logical Knowledge in KGs

Vadalog –Aggregation and Operators

Operators (Example)

```
a("meltwater").
b("san francisco").

q(Y,J) :- a(X), b(Y), J = substring(X,5,9).
@output("q").
```

```
q("water","san francisco").
```

Operators (Example)

```
balanceItem("loans",23.0).
balanceItem("deposits",20.0).

operations(Q,Z,A) :-
    balanceItem(I1,X), balanceItem(I2,Y),
    I1="loans", I2="deposits", Z=X+Y, A=(X+Y)/2.

@output("operations").
```

```
operations(z1,43,21.5).
```

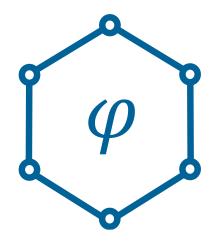
Aggregation

```
s(1.0,"a"). s(2.0,"a"). s(3.0,"a").
s(4.0,"b"). s(3.0,"b").

f(J,Y) :- s(X,Y), J = sum(X).

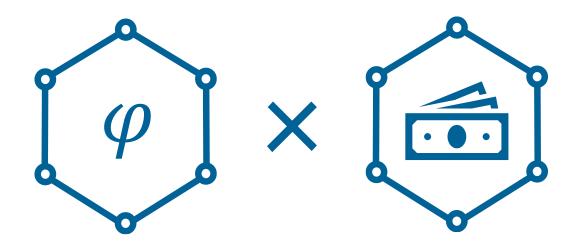
@output("f").
```

```
f(6.0,"a").
f(7.0,"b").
```

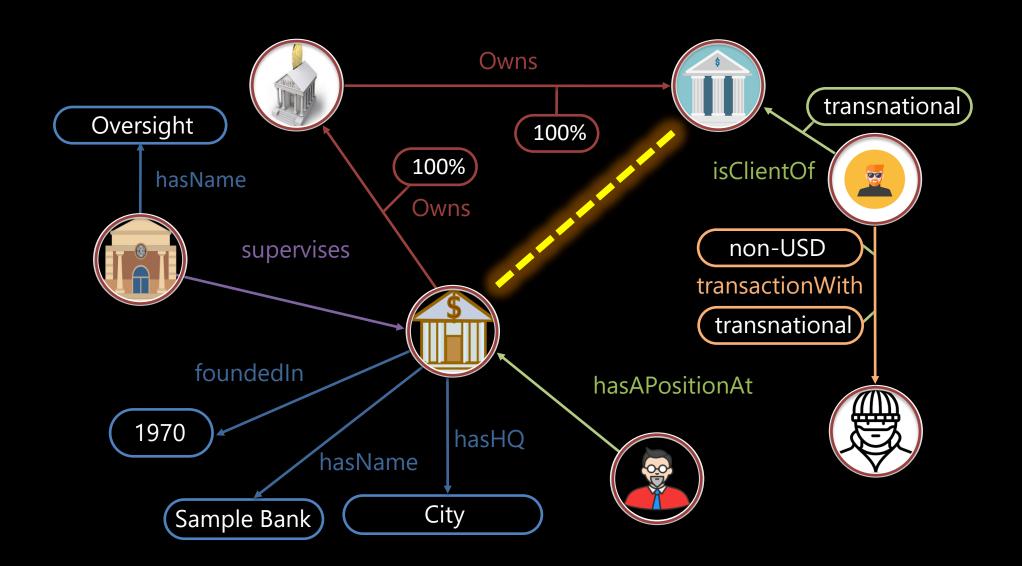


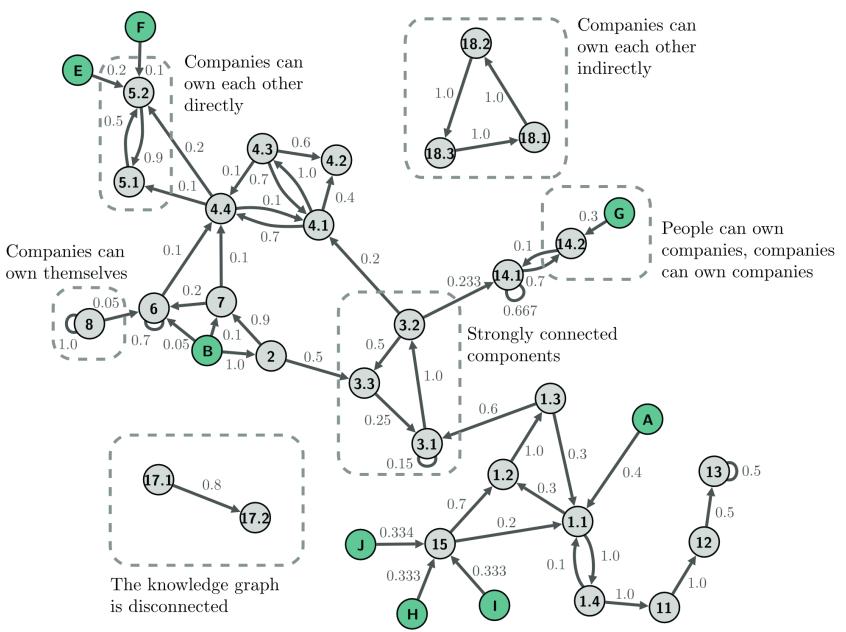
Logical Knowledge in KGs

Vadalog –Aggregation and Operators

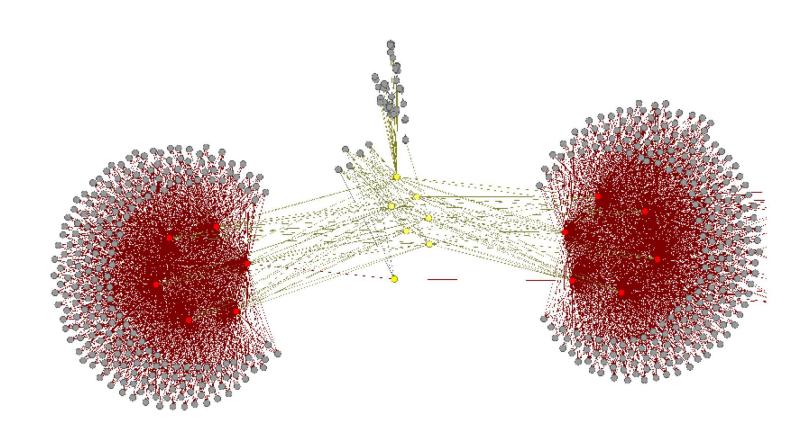


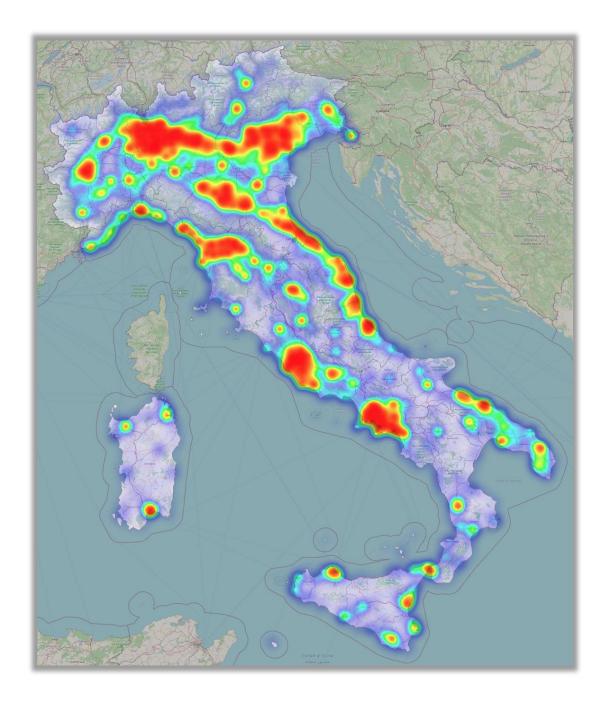
Logical Knowledge in KGs The Real World



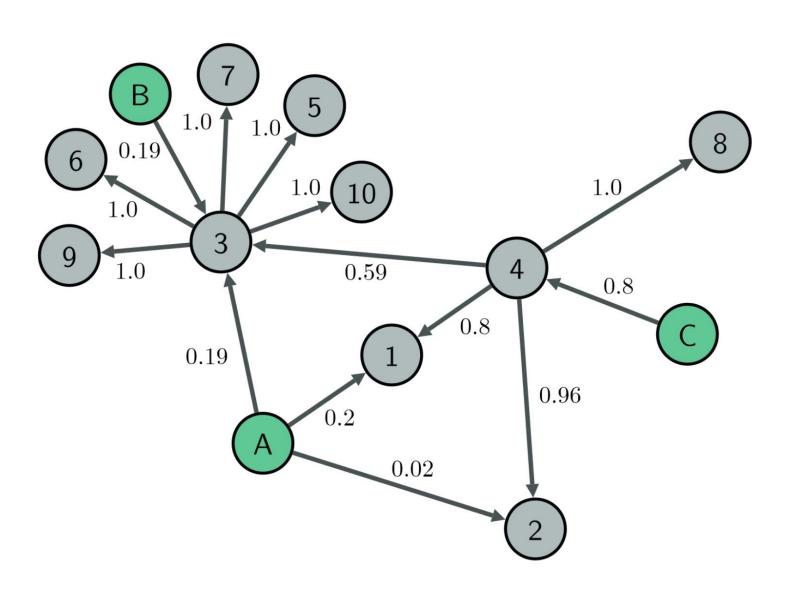


Source: https://arxiv.org/abs/2004.10119







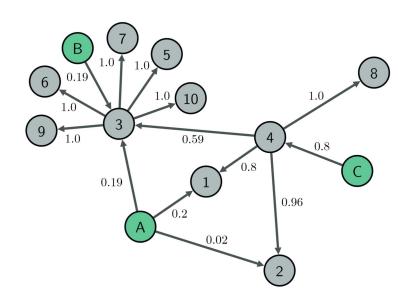


Definition 5. The undirected ϵ -Baldone ownership of a company s on a company t in a graph G is a function $\mathcal{U}_{\epsilon}^{G}(s,t) : \max\{O_{\epsilon}^{G}(s,t), O_{\epsilon}^{G}(t,s)\}.$

Definition 6. The binary relation vicinity $\mathcal{V}_{\epsilon}^{G}$ holds between two companies x and y of a graph G (and we say — they are close —), if: (i) $\mathcal{U}_{\epsilon}^{G}(x,y) > 0$; or, (ii) there exists a third party z of G such that $\mathcal{U}_{\epsilon}^{G}(z,x) > 0$ and $\mathcal{U}_{\epsilon}^{G}(z,y) > 0$.

Definition 7. An ϵ -conglomerate is an equivalence class of V_{ϵ}^{+G} , where + denotes the transitive closure of the vicinity relation defined on a graph G.





$$O(a, b, x), x > \epsilon \to U(a, b, x), U(b, a, x)$$
(1)

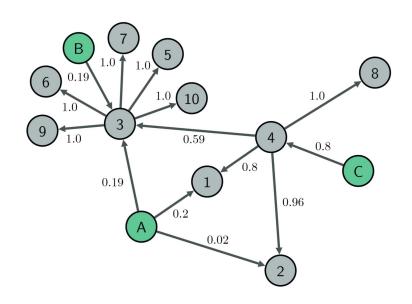
$$U(a, b, x), a > b \rightarrow \exists z \ C(z, a), C(z, b)$$
 (2)

$$U(w, a, x), U(w, b, x) \rightarrow \exists z \ C(z, a), C(z, b)$$
 (3)

$$Company(a) \to \exists z \ C(z, a)$$
 (4)

$$C(y, a), C(x, a) \rightarrow x = y$$
 (5)

Conglomerates



$$O(a, b, x), x > \epsilon \rightarrow U(a, b, x), U(b, a, x)$$
 (1)

$$U(a, b, x), a > b \rightarrow \exists z \ C(z, a), C(z, b)$$
 (2)

$$U(w, a, x), U(w, b, x) \rightarrow \exists z \ C(z, a), C(z, b)$$
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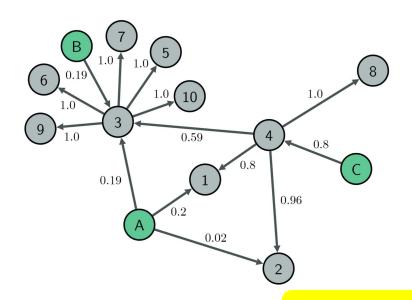
$$Company(a) \rightarrow \exists z \ C(z,a)$$

$$C(y, a), C(x, a) \rightarrow x = y$$
 (5)

(4)



Conglomerates



$$O(a, b, x), x > \epsilon \rightarrow U(a, b, x), U(b, a, x)$$

$$U(a, b, x), a > b \rightarrow \exists z \ C(z, a), C(z, b)$$

$$U(w, a, x), U(w, b, x) \rightarrow \exists z \ C(z, a), C(z, b)$$

$$Company(a) \rightarrow \exists z \ C(z,a)$$

$$C(y, a), C(x, a) \rightarrow x = y$$

(4)

(5)

Collusion





Collusion Golden Power Check

Goal: The goal is checking whether an acquisition (of shares, stocks, etc.)

causes any strategic Italian company to be possibly controlled by

a set of foreign companies acting in collusion.

Setting: Let S be a set of strategic companies and F be a set of foreign com-

panies. Let t be a transaction (e.g., an offer issued by a company

x to buy an amount s of shares of a company y), with $x, y \in S \cup F$.

Question: Decide whether t causes F to jointly control a company in S.

Insight: Consider the possibility to exert Golden Powers to block t.

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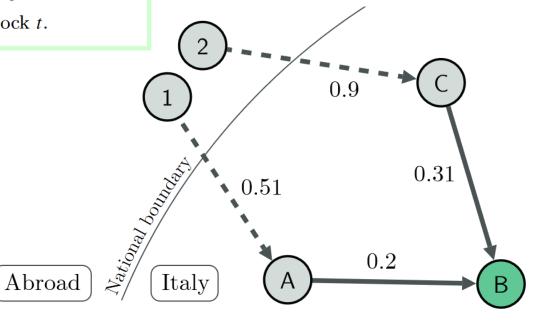
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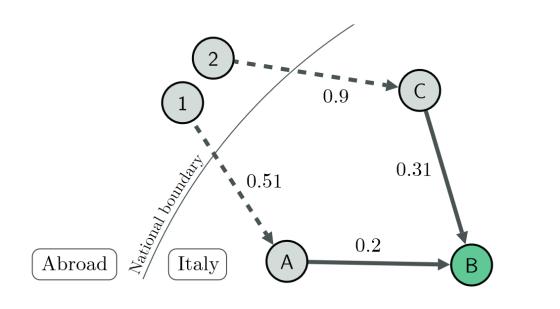
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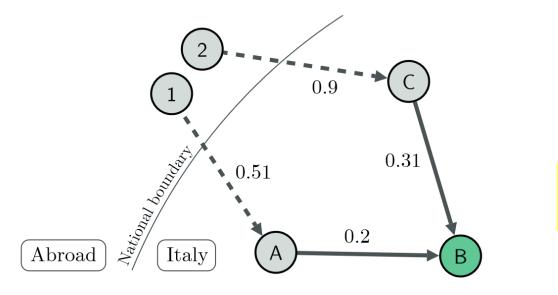
$$F(x), F(y) \to Control(x, y)$$
 (1)

$$T(x, y, w) \rightarrow Own(x, y, w)$$
 (2)

$$Control(x, y) \to Control(x, x)$$
 (3)

$$Control(x, y), Own(y, z, w), v = msum(w, \langle y \rangle), v > 0.5 \rightarrow Control(x, z)$$
 (4)

$$F(x), S(y), Control(x, y) \rightarrow CGPCheck(x, y)$$
 (5)



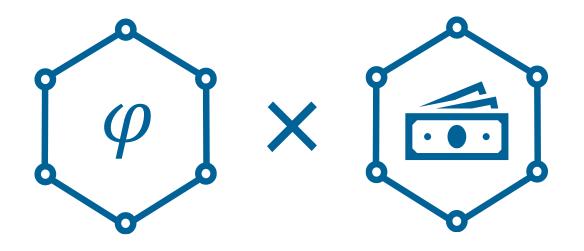
```
F(x), F(y) \to Control(x, y) (1)
```

$$T(x, y, w) \to Own(x, y, w)$$
 (2)

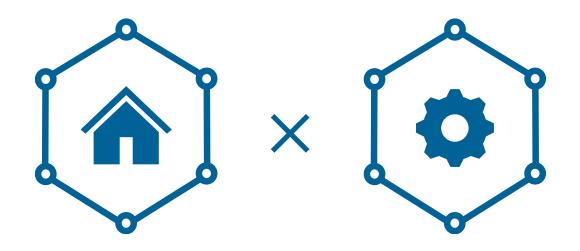
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Logical Knowledge in KGs The Real World



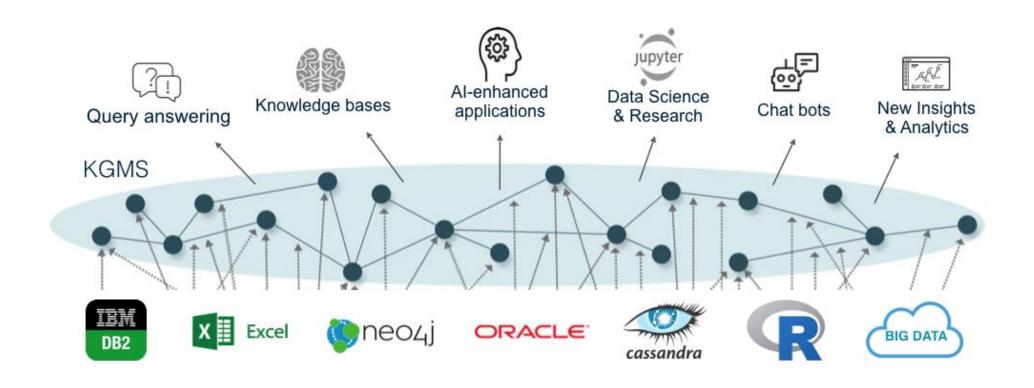
Knowledge Graph Management Systems

Application Appli-Service **Application** cation Service Service Management Management Management System System System Represen-Representation tation Tool Representation Tool Tool

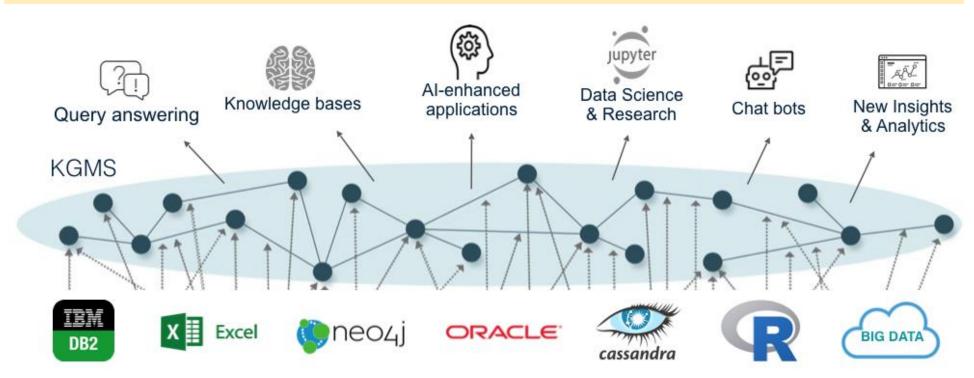
"Enterprise Knowledge Graphs must be deployed into a **Knowledge Graph Management System**, a middleware that:

- 1. provides a language and a formalism for representation of and reasoning on KGs
- 2. can access a rich set of data sources (including big data);
- 3. can embed procedural and third-party code
- 4. provides reasoning services via a rich set of APIs."

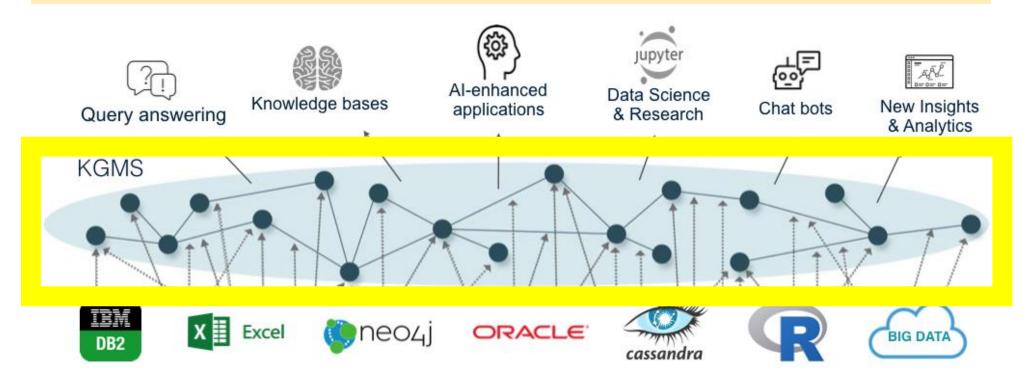
Bellomarini, Fakhoury, Gottlob, Sallinger. Knowledge Graphs and Enterprise AI: The Promise of an Enabling Technology. ICDE 2019.



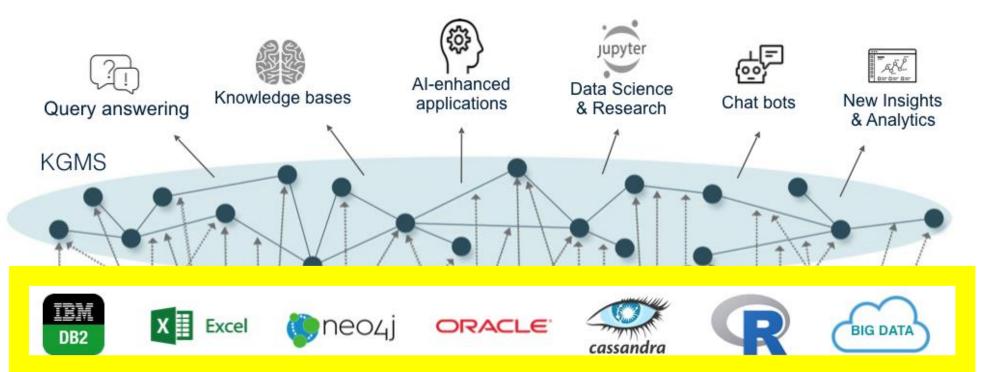
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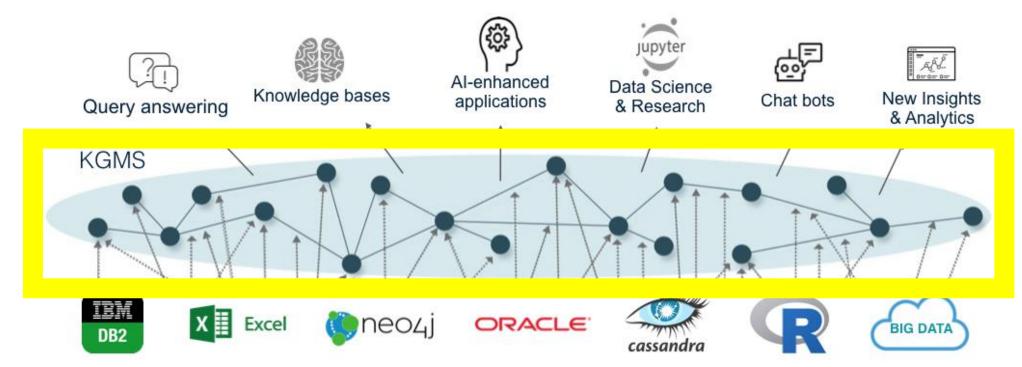
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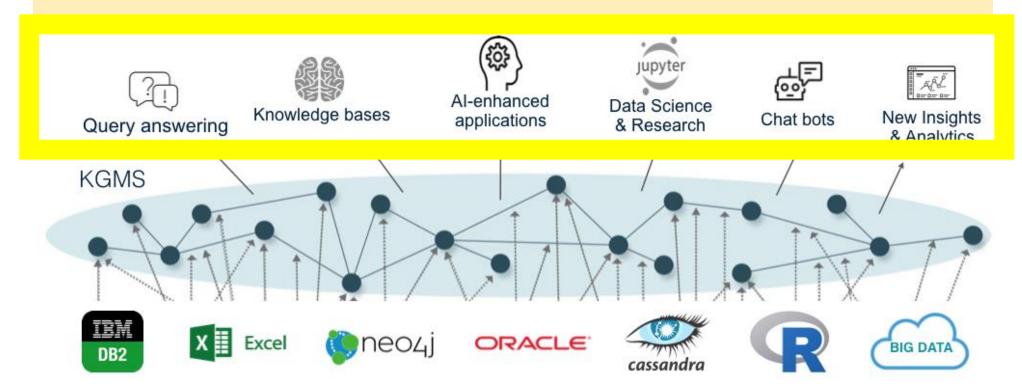
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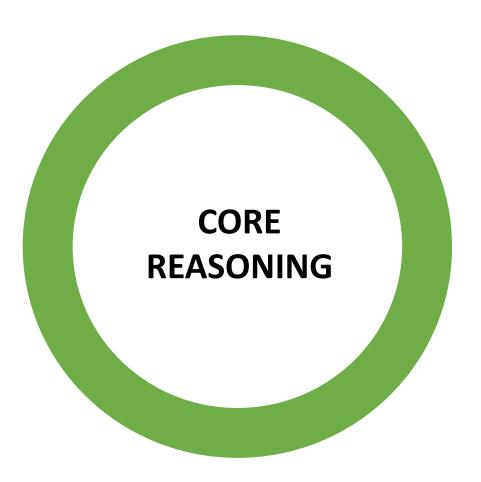


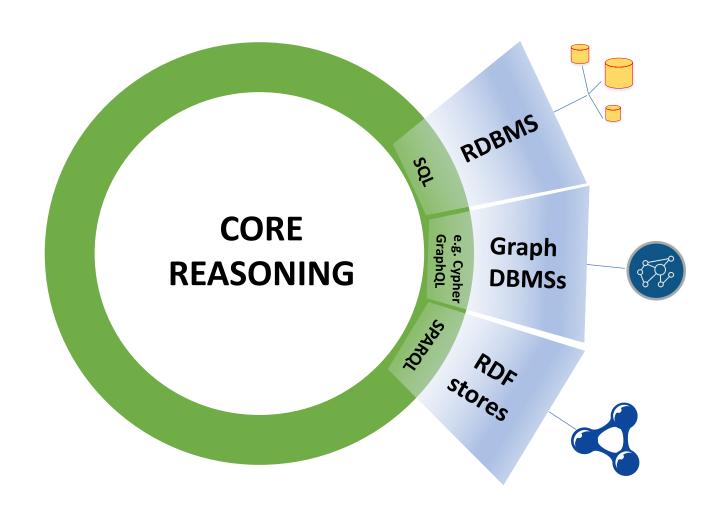
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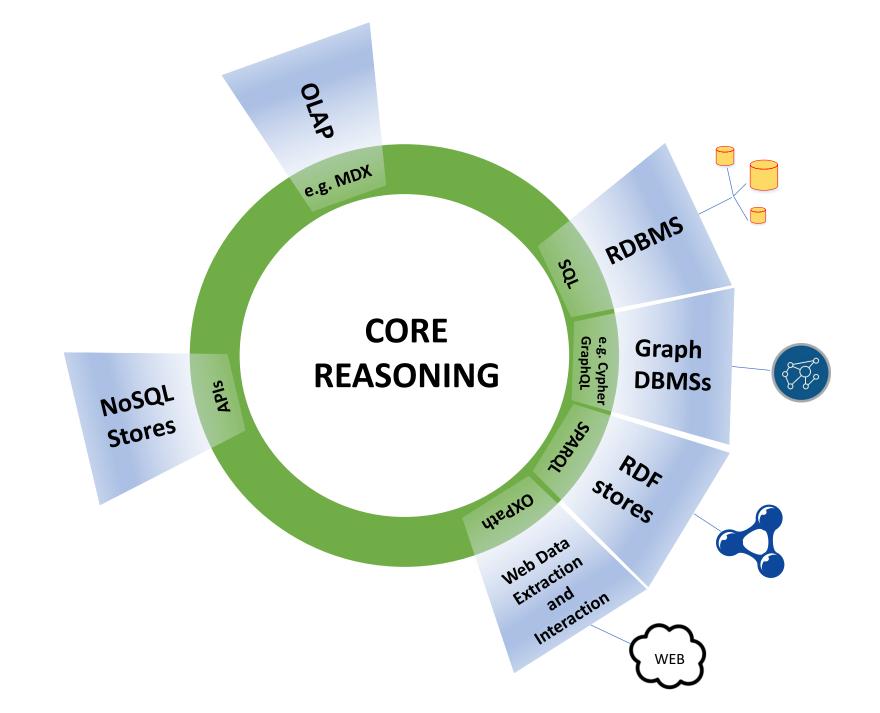


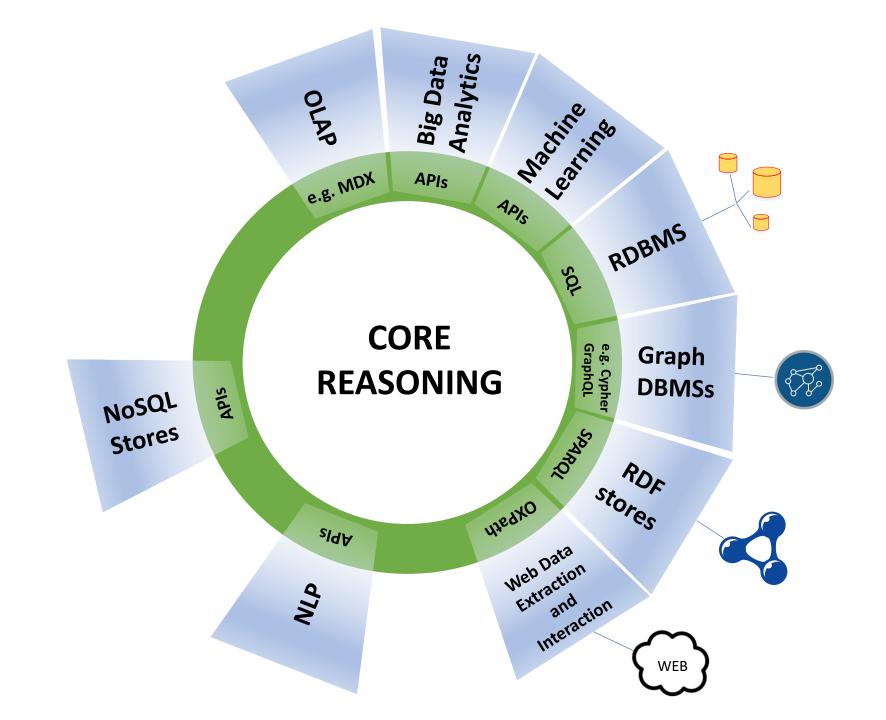
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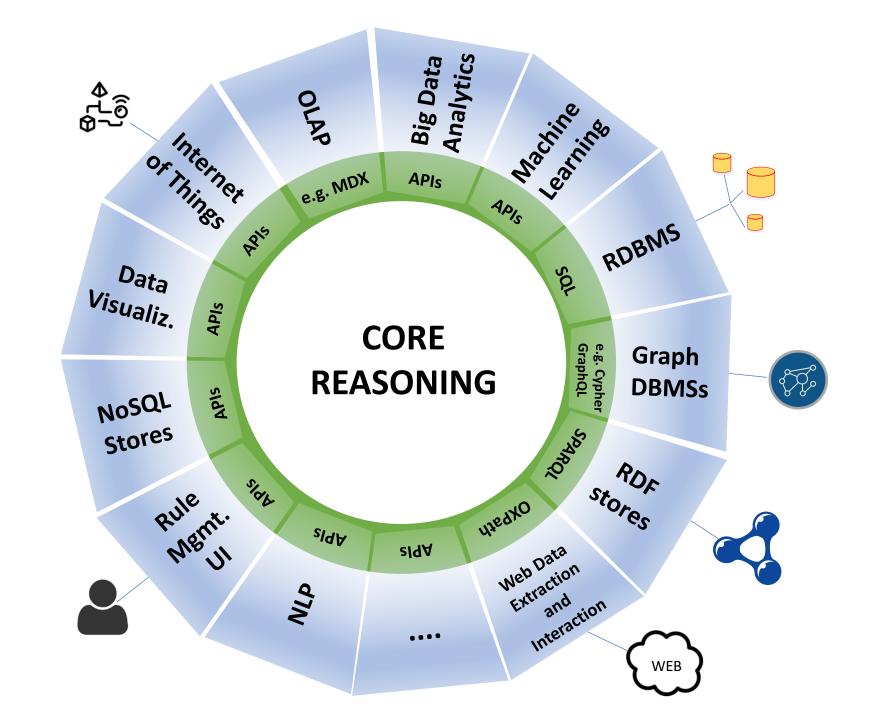


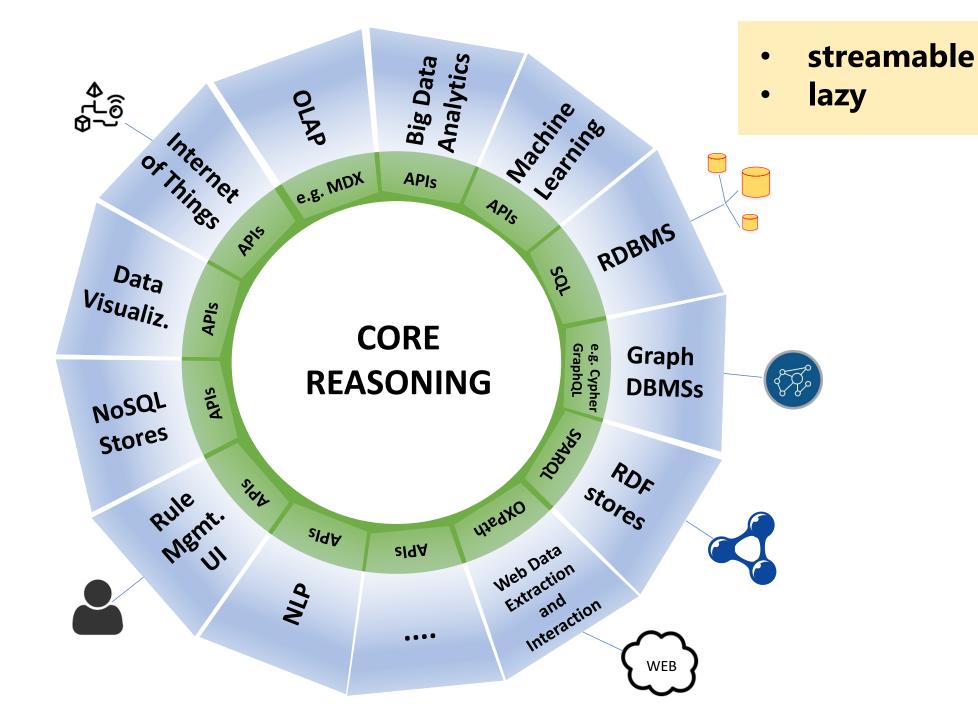




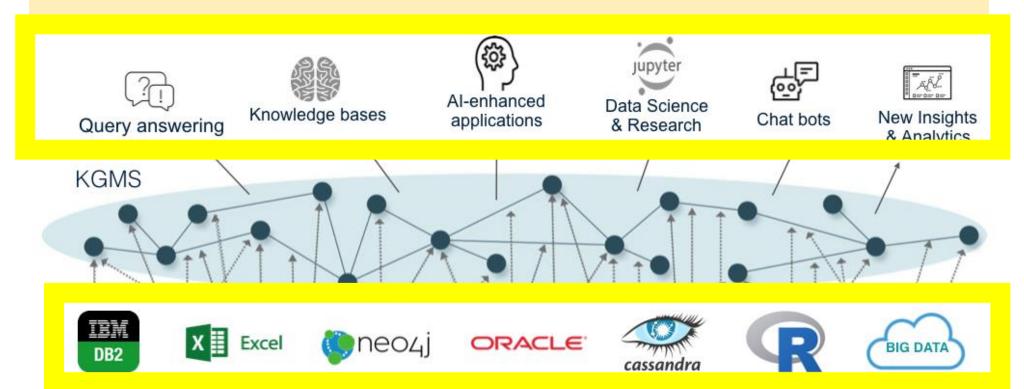




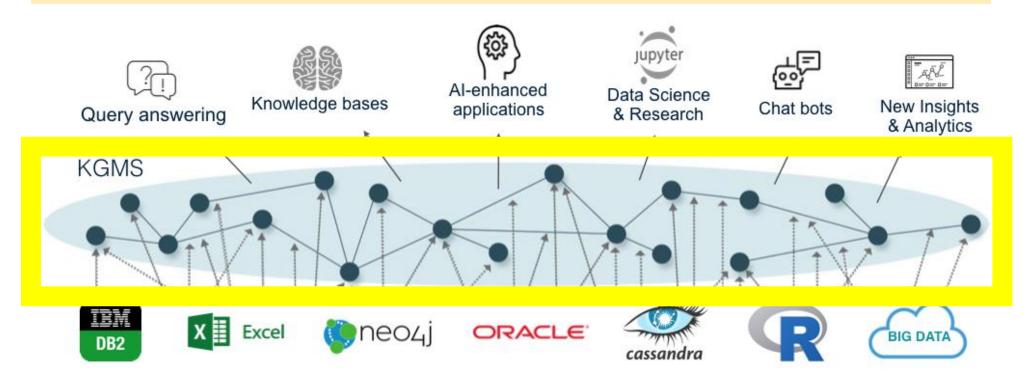


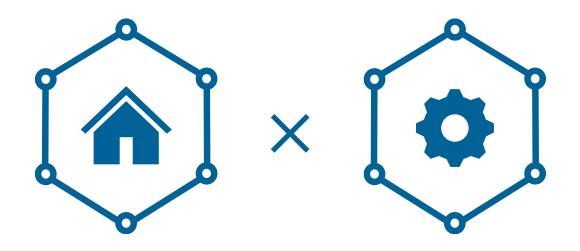


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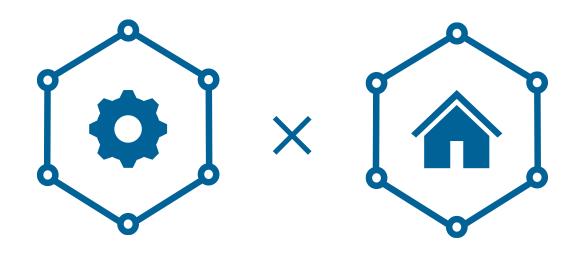


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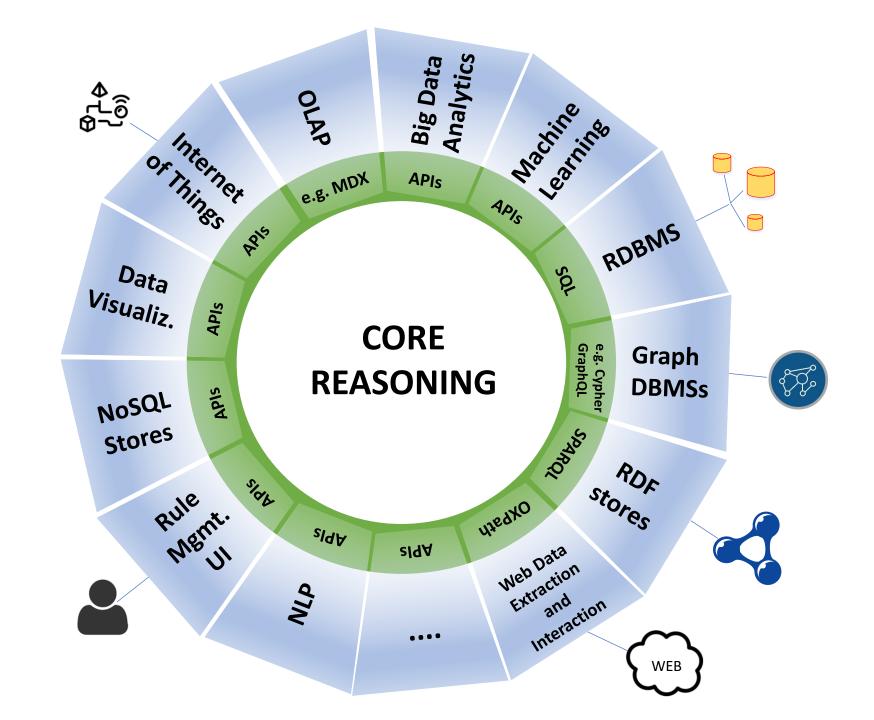


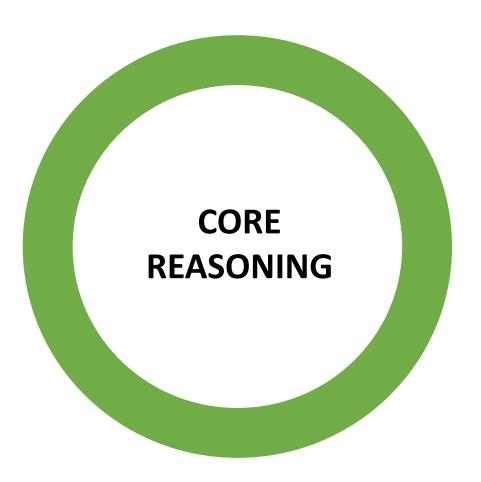


Knowledge Graph Management Systems



Knowledge Graph Management Systems Reasoning







- 1. **Recursive** Reasoning: full recursion over graphs
- 2. Ontological Reasoning: object creation, ...



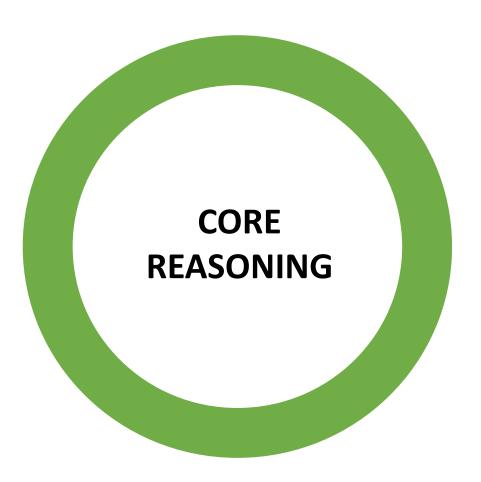
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- 7. Scalable Reasoning: coping with large datasets



Vadalog

- Recursive Reasoning:
 Full support of recursive Datalog
- Ontological Reasoning:Expressive power of SPARQL and OWL 2 QL
- 3. Scalable Reasoning: polynomial time, sub-fragments that are fully parallelizable



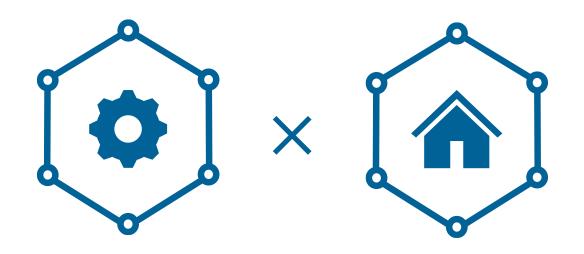
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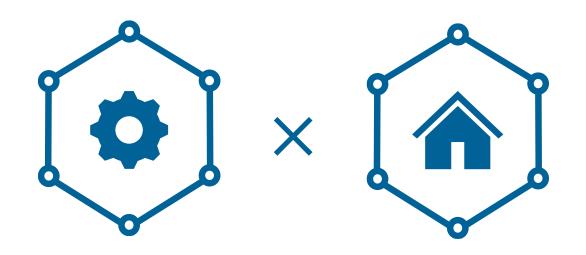
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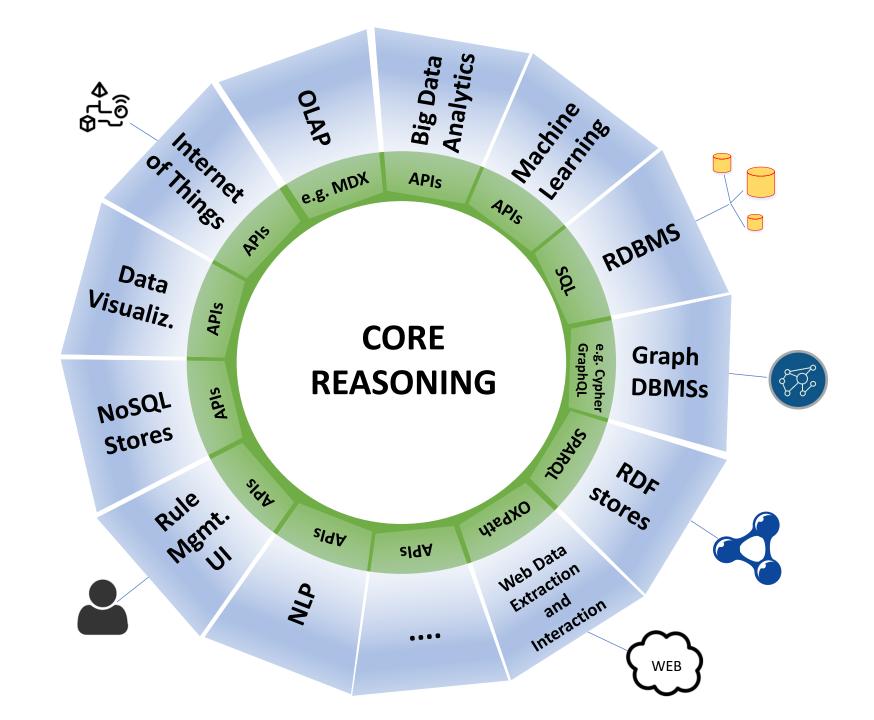
Knowledge Graph Management Systems Reasoning

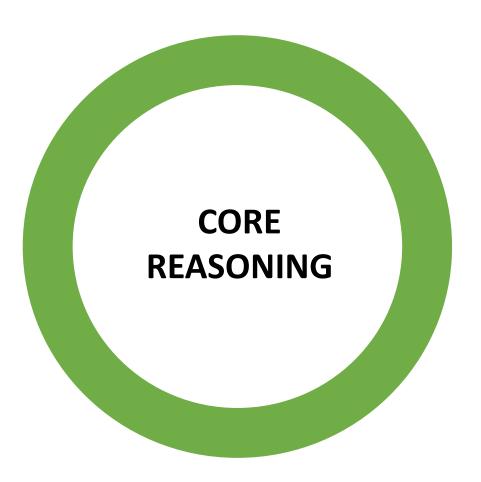


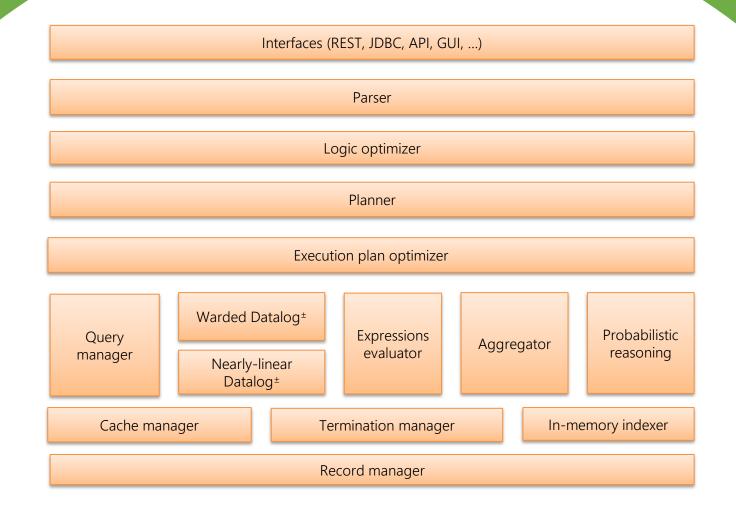
Knowledge Graph Management Systems Vadalog

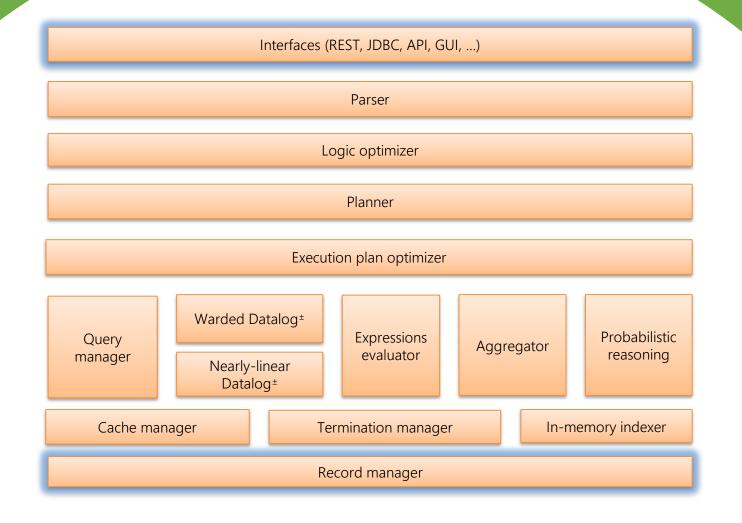


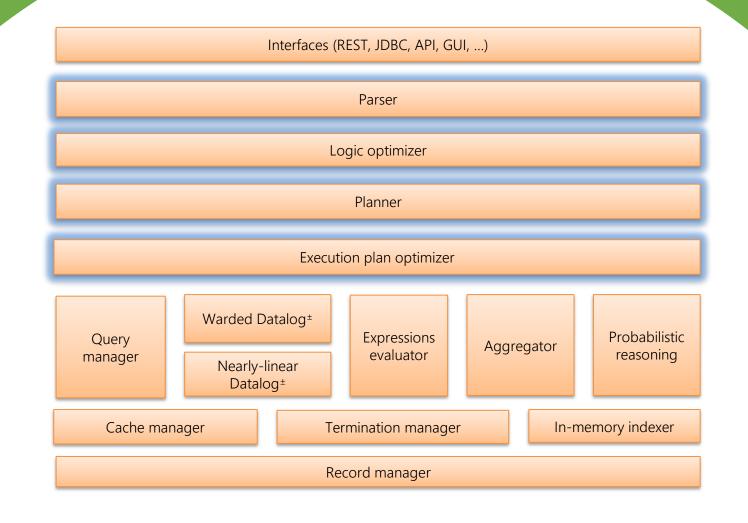
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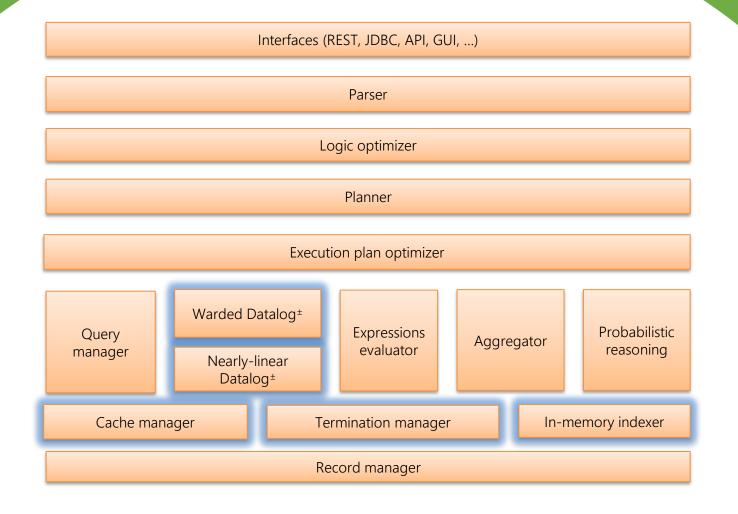


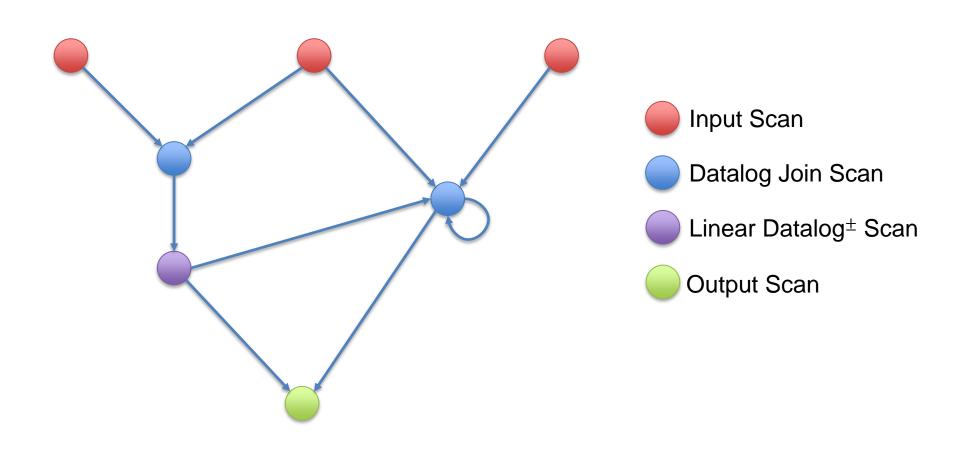




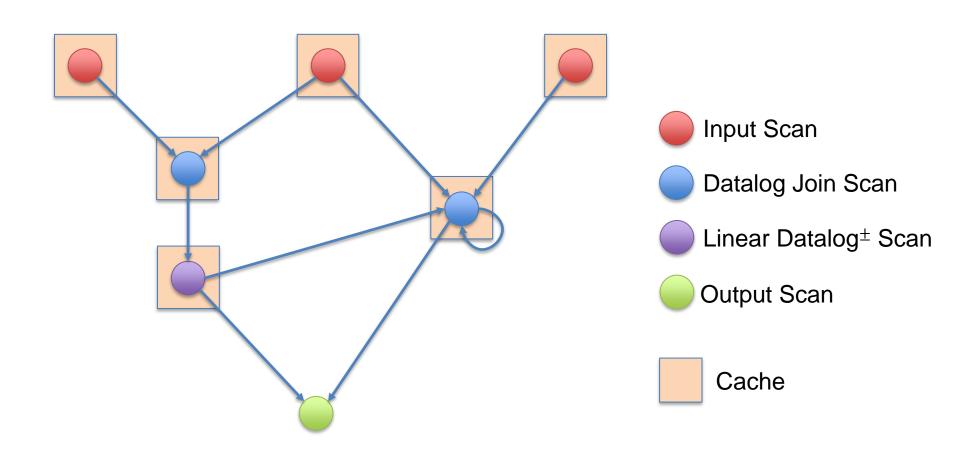




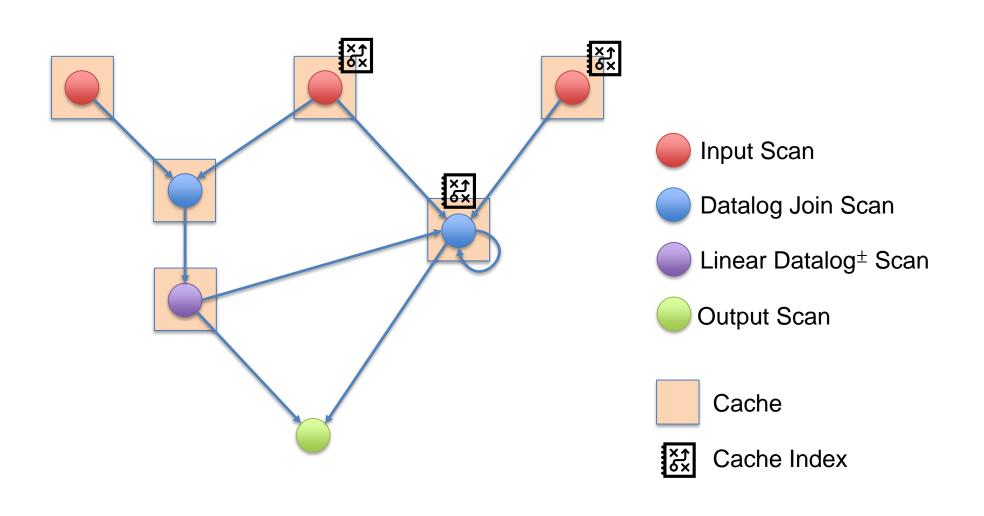




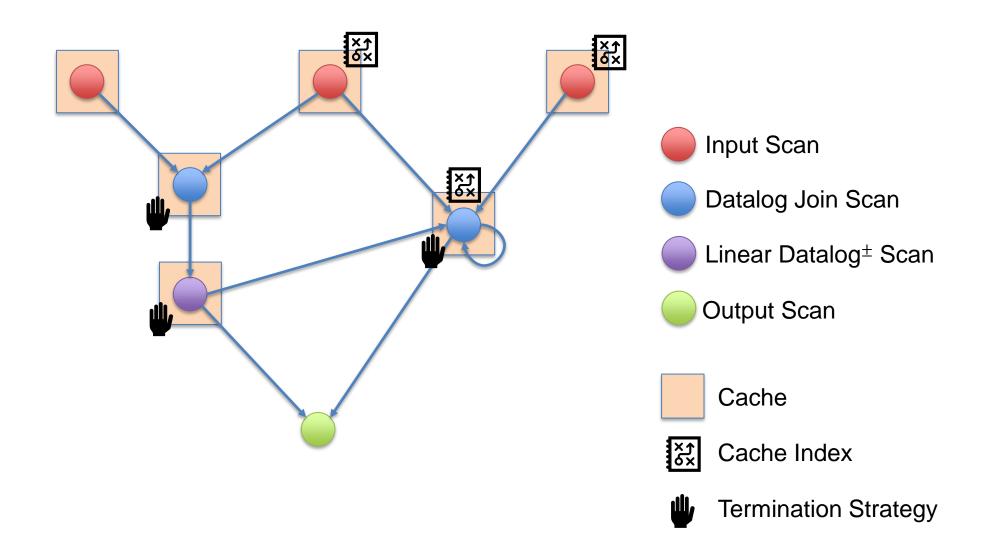


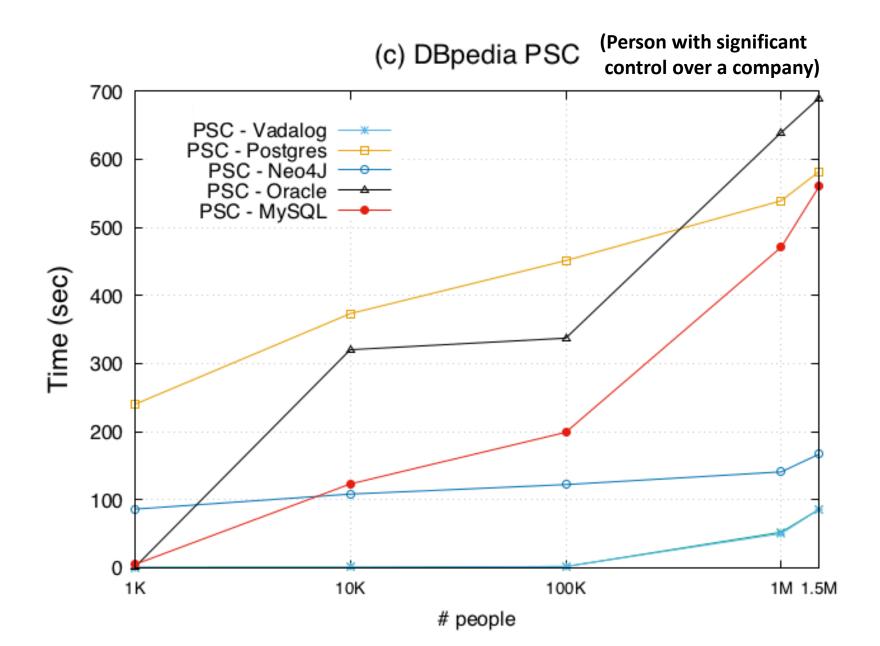




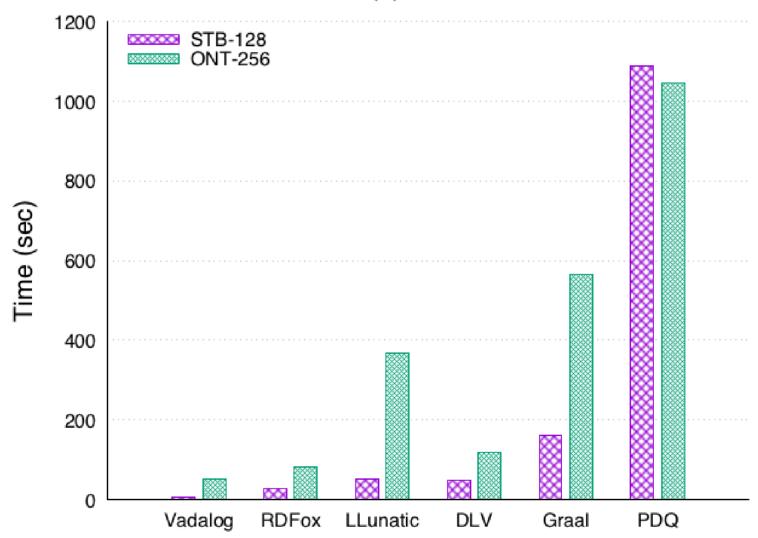


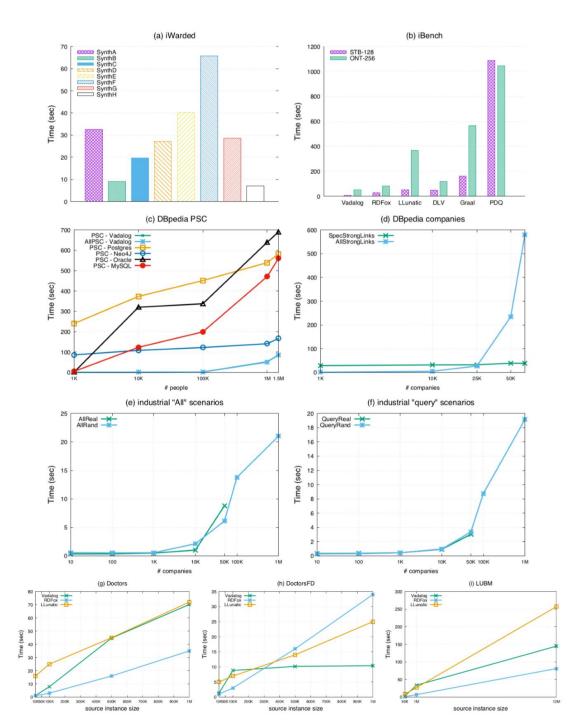


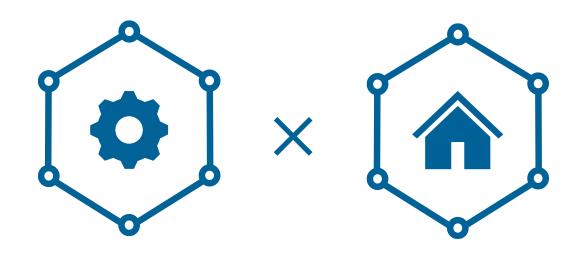




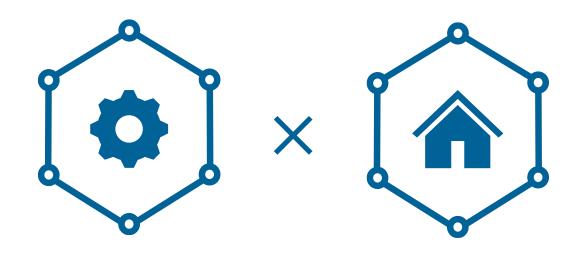








Knowledge Graph Management Systems Vadalog



Knowledge Graph Management Systems Vadalog

Advanced

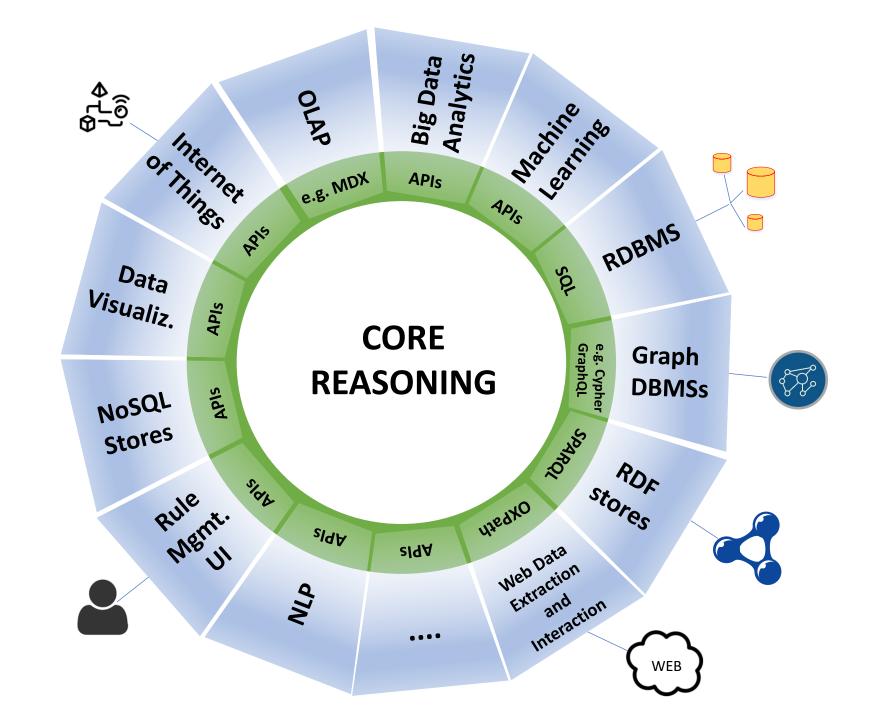


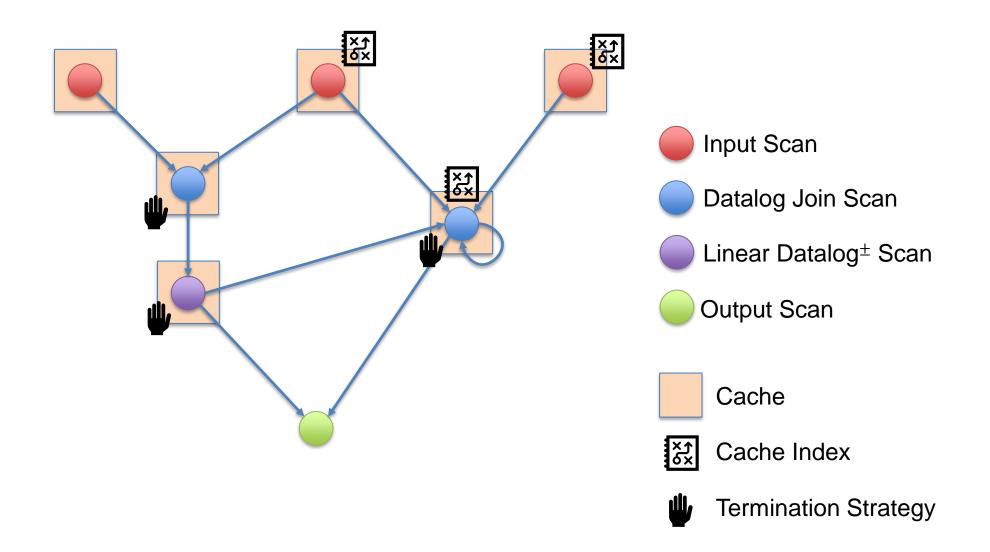
WARNING: Advanced Unit

Only for the interested Needs further reading to understand all concepts

Bellomarini, Sallinger, Gottlob.

The Vadalog System: Datalog-based Reasoning for Knowledge Graphs. VLDB, 2018.





 $2: \text{Owns}(\hat{p}, \hat{s}, x) \to \text{Stock}(x, \hat{s})$

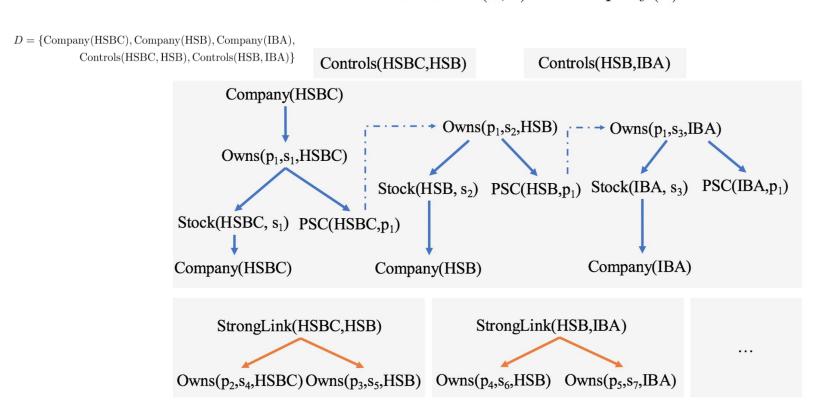
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 $4: \mathrm{PSC}(x,\hat{p}), \mathrm{Controls}(x,y) \to \exists s \; \mathrm{Owns}(\hat{p},\hat{s},y)$

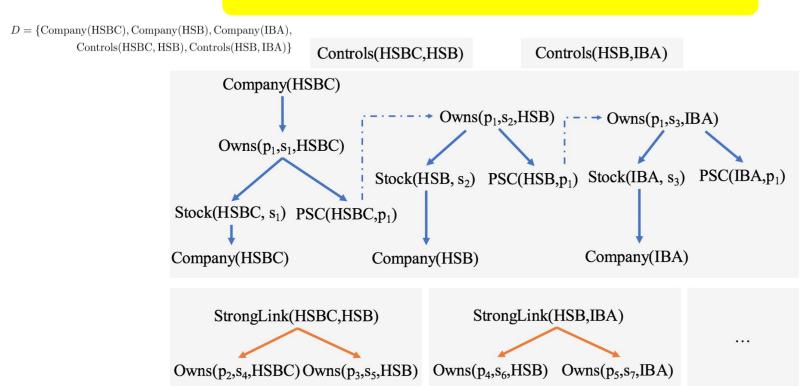
 $5: \mathrm{PSC}(x,\hat{p}), \mathrm{PSC}(y,\hat{p}) \to \mathrm{StrongLink}(x,y)$

6: StrongLink $(x, y) \to \exists p \exists s \text{ Owns}(\hat{p}, \hat{s}, x)$

7: StrongLink $(x, y) \to \exists p \exists s \text{ Owns}(\hat{p}, \hat{s}, y)$



```
1: \operatorname{Company}(x) \to \exists p \exists s \operatorname{Owns}(\hat{p}, \hat{s}, x)
2: \operatorname{Owns}(\hat{p}, \hat{s}, x) \to \operatorname{Stock}(x, \hat{s})
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7: \operatorname{StrongLink}(x, y) \to \exists p \exists s \operatorname{Owns}(\hat{p}, \hat{s}, y)
8: \operatorname{Stock}(x, \hat{s}) \to \operatorname{Company}(x).
```



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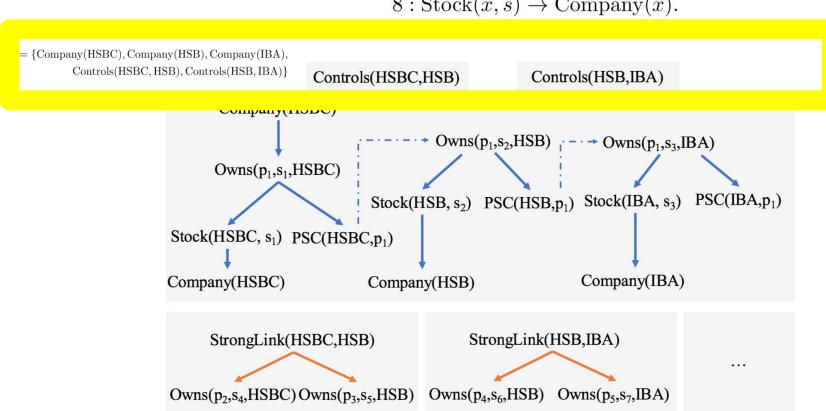
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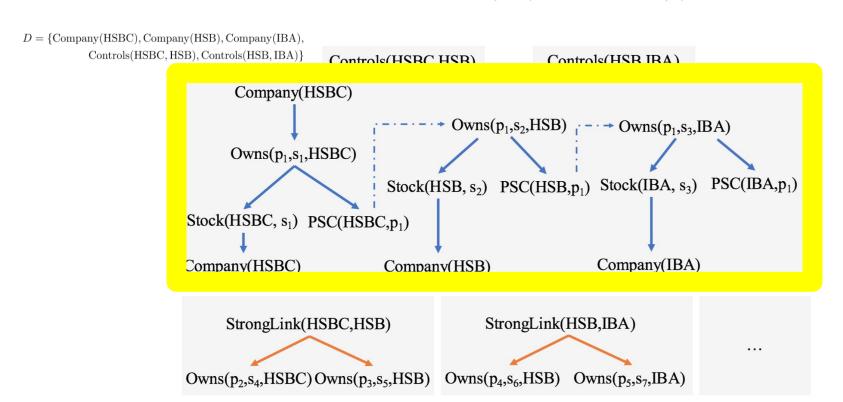
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Dangerous



1. all the "dangerous" variables should coexist in a single body-atom α , called the ward

 $2: \text{Owns}(\hat{p}, \hat{s}, x) \to \text{Stock}(x, \hat{s})$

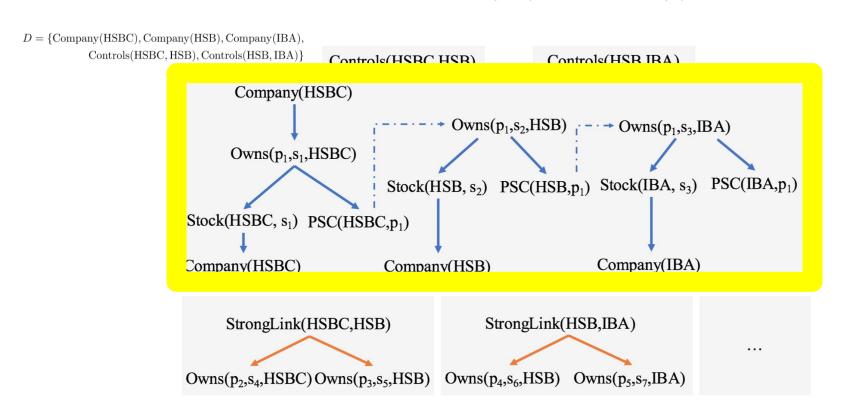
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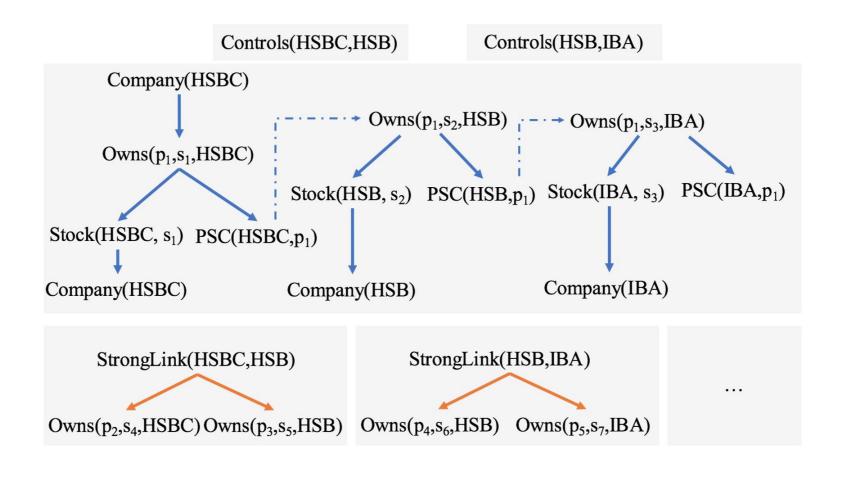
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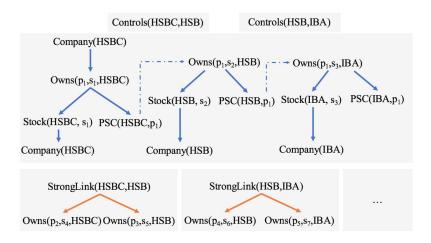
Theorem

Let a and b be two facts in a warded forest. If they are isomorphic, then subtree(a) is isomorphic to subtree(b).



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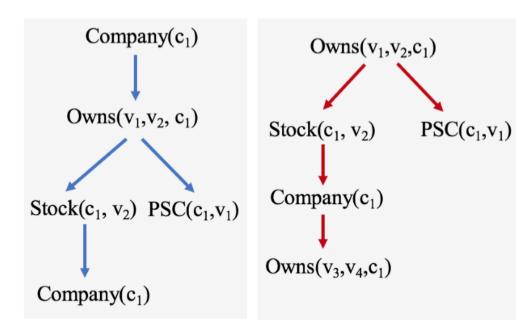
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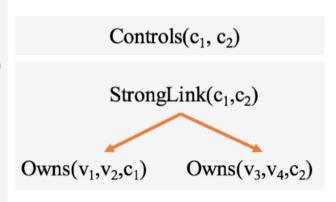
Let a and b be two facts in the chase graph of a set of harmless warded rules. If a and b are isomorphic, then subgraph(a) is isomorphic to subgraph(b).



Proposition

Let a and b be two facts in a linear forest. If they are pattern-isomorphic, then subtree(a) is pattern-isomorphic $to\ subtree(b)$.





Algorithm 1 Termination strategy for the chase step.

```
1: function CHECK_TERMINATION(a)
        if a.generating_rule == {LINEAR or WARDED} then
 2:
             if \exists \lambda \in S[\pi(\mathbf{a}.l\_root)] s.t. \lambda \subseteq \mathbf{a}.provenance then
 3:
                 return false

    beyond a stop provenance

 4:
             else if \exists \lambda \in S[\pi(a.l\_root)] s.t. a.provenance \subset \lambda then
 5:

    b within a stop provenance

                 return true
 6:
                                                                                     else
 7:
                 if \exists g \ in \ G[a.w\_root] \ s.t. \ a \ isomorphic to g \ then
 8:
                      S[\pi(\mathbf{a}.l_{\text{root}})]=\mathbf{a}.\text{provenance}
 9:
                      return false

    isomorphism found

10:
11:
                 else
                      G[a.w_root].append(a)
12:
                                                                                  13:
                      return true
        else if a \notin G then

    b other non-linear generating rules

14:
             G[\mathbf{a}.w_{root}].append(\mathbf{a})

    □ and reset provenance

15:
             return true
16:
                                                                                be the new tree is redundant
        else
17:
             return false
18:
```

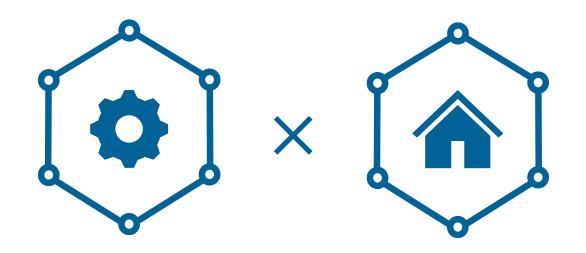
Algorithm 2 A generic chase using the termination strategy.

```
1: function CHASE(D, \Sigma)

2: for all \sigma \in \Sigma and x to which \sigma applies do

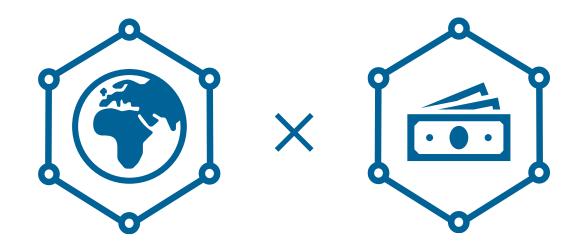
3: if CHECK\_TERMINATION(\sigma(\mathbf{x})) then

4: D = D \cup \{\sigma(\mathbf{x})\}
```



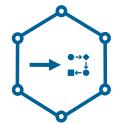
Knowledge Graph Management Systems Vadalog

Advanced

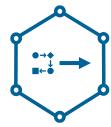


Financial Knowledge Graphs Company Knowledge Graphs









Ongoing work on the reference historical KG for all Italian companies, including:



- 6 million companies
- 10 million **people**
- 30 million **ownerships**
- 20 million roles (e.g. managers)
- 200k company events (like M&A)



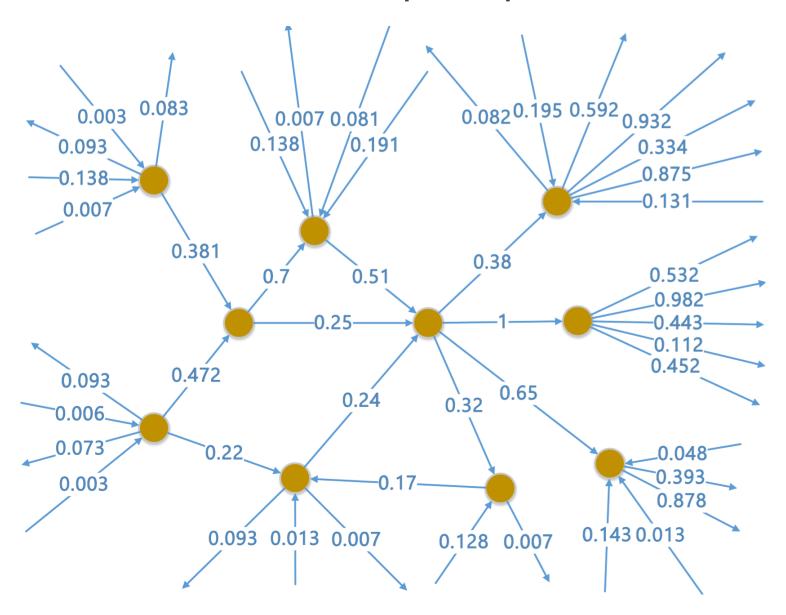
- 50+ million **nodes**
- 100+ million edges
- 1+ billion properties

plus, adding derived extensional knowledge:



- company control
- family links between people

Ownership Graph



Creditworthiness

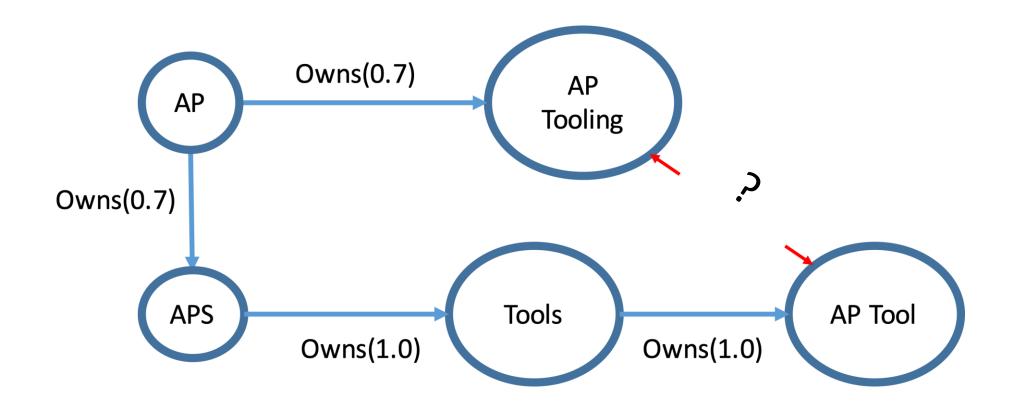
• Probability that a borrower company will not default on its debt obligations

	Credit DB							
	Company name	Total Debts		Avg Debt to Income Ratio	Rating			
	AP Tool	0	•••	0.28	Α			
	ACME	50k	•••	0.46	В			
	Big S	20k	•••	0.89	D			
	AP Tooling	0		0.10	Α			

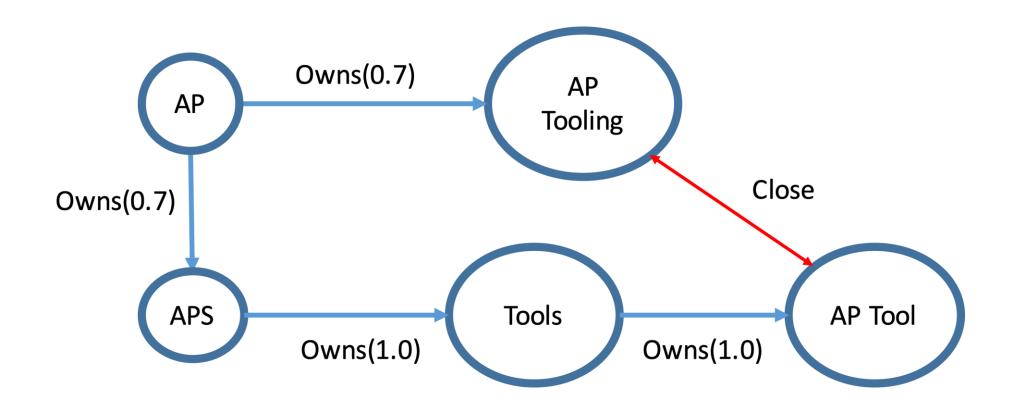
LOAN DENIED

AP Tool asks for 1M loan, with AP Tooling as guarantor

Company Graphs



Company Graphs



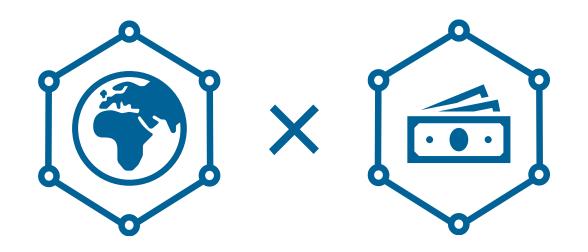


Company Graphs

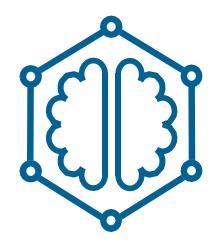
We build graphs of company networks, to:

- 1. reveal power
 - 1. finding controllers
 - 2. studying the **structure** of market
 - 3. studying dispersion of control
 - 4. global **shareholding** analysis
 - 5. intercept and prevent **hostile takeovers**
- 2. detect collusion and do forensics
 - 1. support AML
 - 2. detecting ultimate beneficial owners

- 3. evaluate and guarantee **anonymity** of **microdata**
- 4. evaluate risks
- 5. model **propagations** (e.g., of shocks)
- 6. guarantee compliance
- 7. perform enhanced due diligence
- 8. understand foreign shareholder structures
- 9. know real cash flows



Financial Knowledge Graphs Company Knowledge Graphs



Overview

Temporal Knowledge Graphs

Bonus

DatalogMTL

Temporal Operators

flags(x,z):- monitors(x,z), $\boxminus_{[0,5]}$. $\circlearrowleft_{[0,3]}$ signal(z).

monitors("Server1","SSH")@[0,∞). signal("SSH")@[2,2]. signal("SSH")@4.

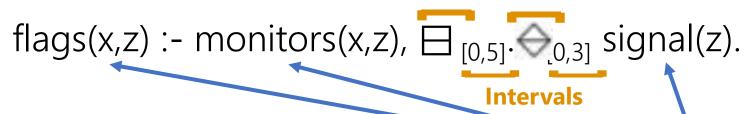
Hidden Time Information

DatalogMTL

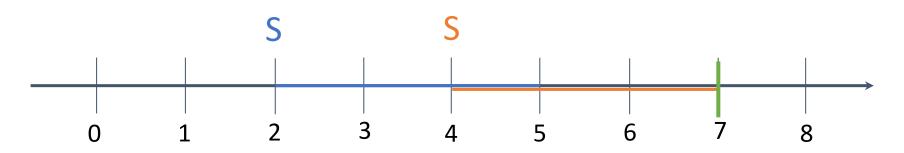
Temporal Operators

Hidden Time

Information



monitors("Server1","SSH")@[0,∞). signal("SSH")@[2,2]. signal("SSH")@4.



DatalogMTL – Intervals *ρ*

 ϱ of form $\langle t1, t2 \rangle$, where t1 in $\mathbb{Q}_2^{\geq 0}$ t2 in $\mathbb{Q}_2^{\geq 0} \cup \{\infty\}$

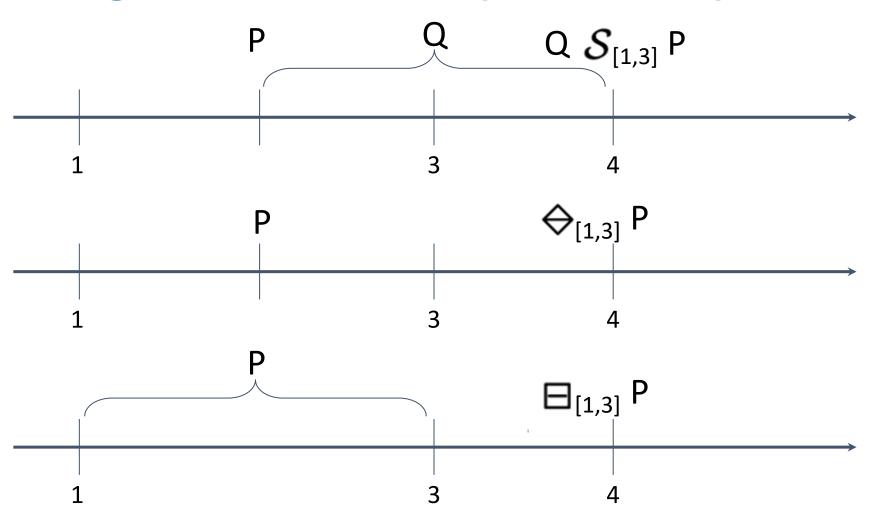
- [t1,t2], only if $t2 \neq \infty$
- [t1,t2)
- (t1,t2], only if $t2 \neq \infty$
- (t2,t2)

DatalogMTL – Rules

$$B \leftarrow A_1, \ldots, A_n$$

$$A \coloneqq \top \mid \bot \mid P(\tau) \mid \boxplus_{\varrho} A \mid \boxminus_{\varrho} A \mid \Leftrightarrow_{\varrho} A \mid \Leftrightarrow_{\varrho} A \mid A \mathcal{U}_{\varrho} A \mid A \mathcal{S}_{\varrho} A$$
$$B \coloneqq \top \mid \bot \mid P(\tau) \mid \boxplus_{\varrho} A \mid \boxminus_{\varrho} A$$

DatalogMTL – Temporal Operators

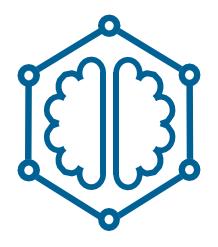


Consistency Checking - Data Complexity

	Rational Timeline		Integer Timeline		
	First-order	Prop.	First-order	Prop.	
$\overline{ m Datalog MTL}$	PSpace-c		PSpace-c		
$\overline{ m Datalog MTL_{lin}}$					
$\overline{{ m DatalogMTL_{core}}}$			NL-h	$ m NC^1$ -c	
$\overline{\mathrm{Datalog}\mathrm{MTL}^{\boxminus}_{\mathrm{lin}}}$		P-hard	PSpace-c		
$\overline{\mathrm{Datalog}\mathrm{MTL}^{\boxminus}_{\mathrm{core}}}$			$ m NC^1$ -h		
$\mathrm{DatalogMTL}_{\mathrm{lin}}^{\diamondsuit}$	NL-c		NL-c		
$\overline{\mathrm{DatalogMTL}_{\mathrm{core}}^{\diamondsuit}}$	TC^0 -c		in $AC^0[k]$ for $k \in \mathbb{N}$, not in AC^0		

Core: B :- A or \perp :- $A_1 \wedge A_2$

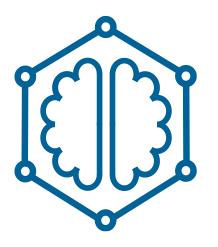
Linear: At most one A_i is IDB or $\bot :- A_1 \land A_2$



Logical Reasoning

Temporal Knowledge Graphs



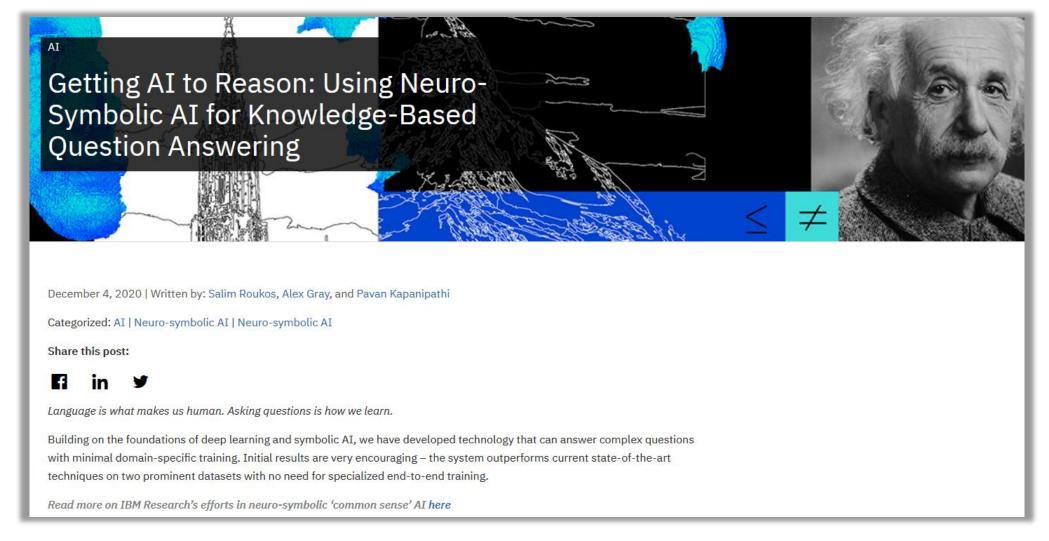


Grand Challenges Neuro-symbolic KGs

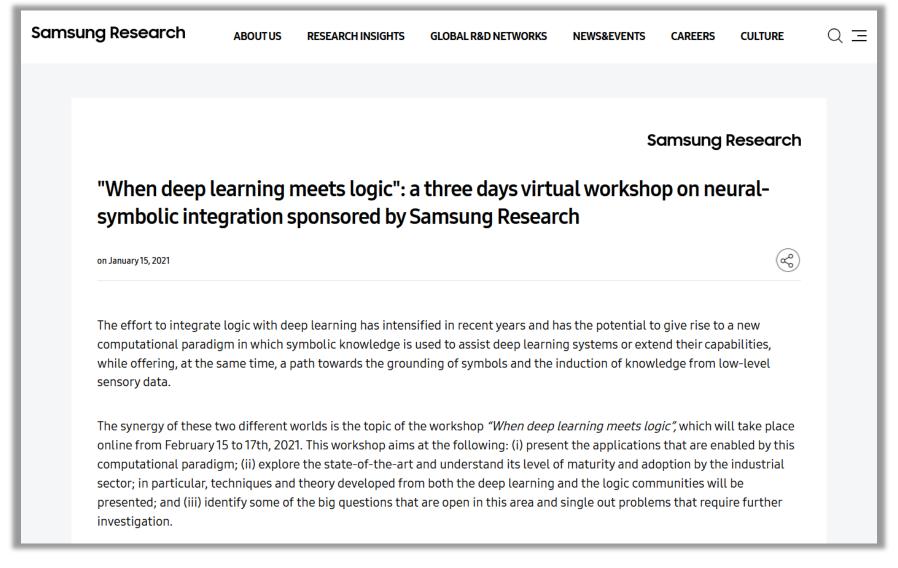
Teaser











Source: https://research.samsung.com/news/-When-deep-learning-meets-logic-a-three-days-virtual-workshop-on-neural-symbolic-integration-sponsored-by-Samsung-Research



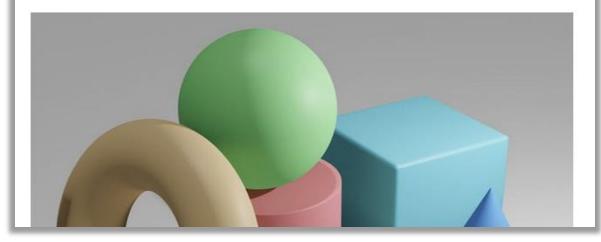
EMERGING TECH

Neuro-symbolic A.I. is the future of artificial intelligence. Here's how it works

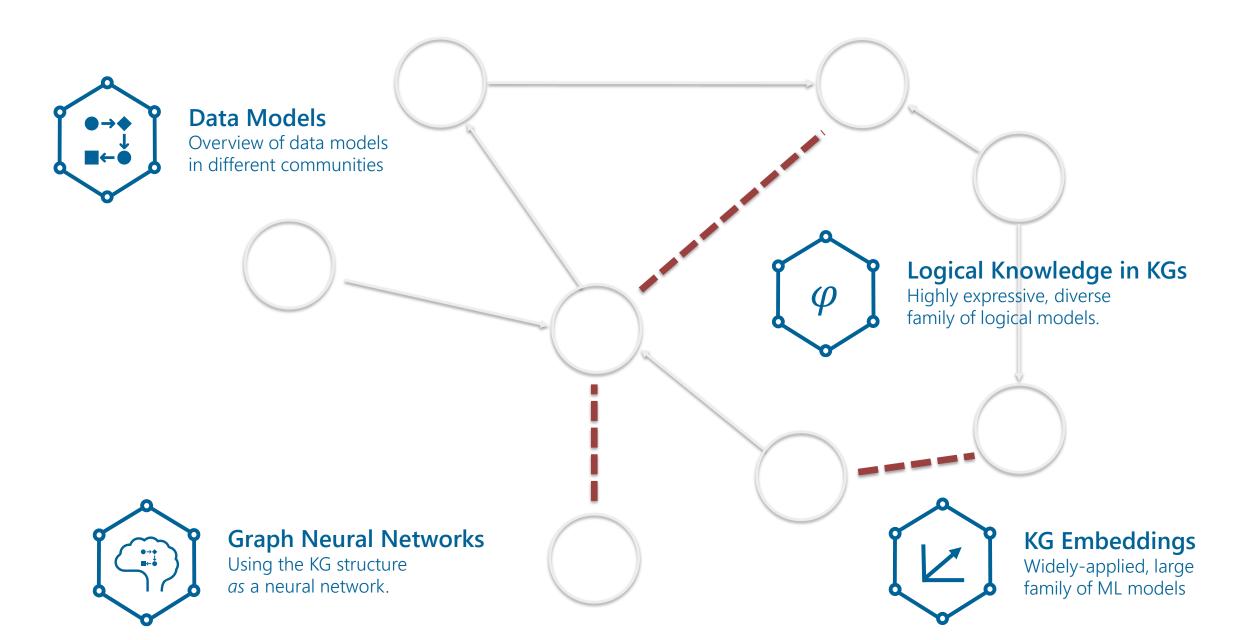
By Luke Dormehl January 5, 2020



Picture a tray. On the tray is an assortment of shapes: Some cubes, others spheres. The shapes are made from a variety of different materials and represent an assortment of sizes. In total there are, perhaps, eight objects. My question: "Looking at the objects, are there an equal number of large things and metal spheres?"



Source: https://www.digitaltrends.com/cool-tech/neuro-symbolic-ai-the-future/





Representations









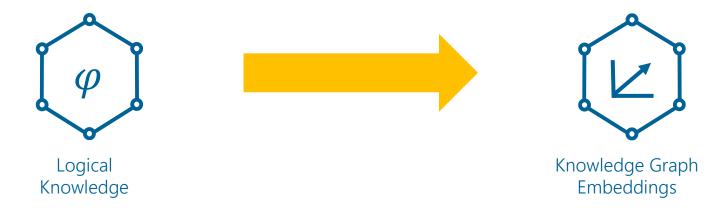
Knowledge Graph Embeddings

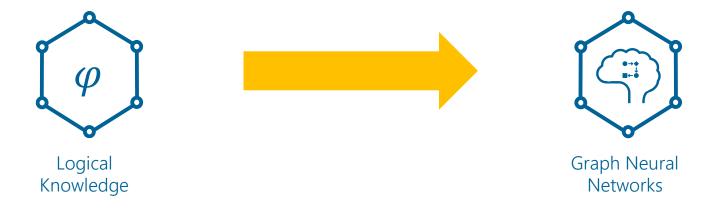


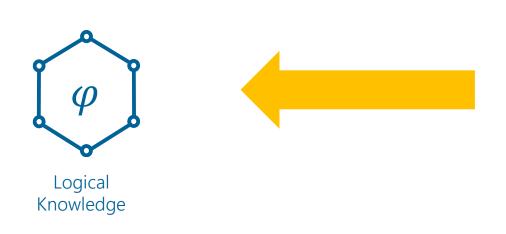
Logical Knowledge



Graph Neural Networks









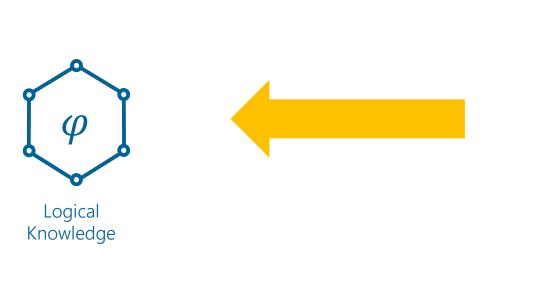
Graph Neural Networks



Knowledge Graph Embeddings



"Explainable AI"

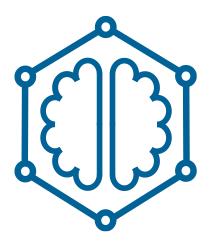




Graph Neural Networks



Knowledge Graph Embeddings



Grand Challenges Neuro-symbolic KGs

Teaser