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**The Causality/Repair Connection in
Databases:**

Causality-Programs

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Database Causality and Goals

- Causality appears at the foundations of many scientific disciplines
- We want to represent and compute causality in order to deal with the *uncertainty in data and knowledge*
- In data management, we *need to understand and compute why* certain (query) results are obtained or not

Why certain natural semantic conditions are not satisfied

- A DB system could provide *explanations*

To understand/explore the data or reconsider the query

- Our current research is motivated by trying to **understand causality in data management from different perspectives**
- We have established interesting and fruitful connections among different forms of reasoning:
 - inferring causes from databases
 - database repairs and consistent query answering (CQA)
 - model-based diagnosis
 - Updates through views in databases
- They all reflect some sort of **uncertainty** about the information at hand

They all have related **non-monotonic** reasoning tasks

- A notion of causality-based explanation for a query result:

(Meliou et al., VLDB 2010)

- A relational instance D and a boolean conjunctive Q
- A tuple $t \in D$ is a **counterfactual cause** for Q if $D \models Q$ and $D \setminus \{t\} \not\models Q$
- A tuple $t \in D$ is an **actual cause** for Q if there is a **contingency set** $\Gamma \subseteq D$, such that t is a counterfactual cause for Q in $D \setminus \Gamma$

Based on (Halpern and Pearl, 2001, 2005)

- Responsibility reflects relative degree of causality of a tuple for a query result (Meliou et al., VLDB 2010)

- The **responsibility** of an actual cause t for Q :

$$\rho_D(t) := \frac{1}{|\Gamma| + 1}, \quad |\Gamma| = \text{size of smallest contingency set for } t$$

- Tuples with **higher responsibility** tend to provide more interesting explanations for query results

Based on (Chockler and Halpern, 2004)

Example: Database D with relations R and S below

$$Q: \exists x \exists y (S(x) \wedge R(x, y) \wedge S(y)) \qquad D \models Q$$

Causes for Q being true in D :

R	A	B
	a_4	a_3
	a_2	a_1
	a_3	a_3

S	A
	a_4
	a_2
	a_3

$S(a_3)$ is counterfactual cause for Q : if $S(a_3)$ is removed from D , Q is no longer an answer; its responsibility is 1

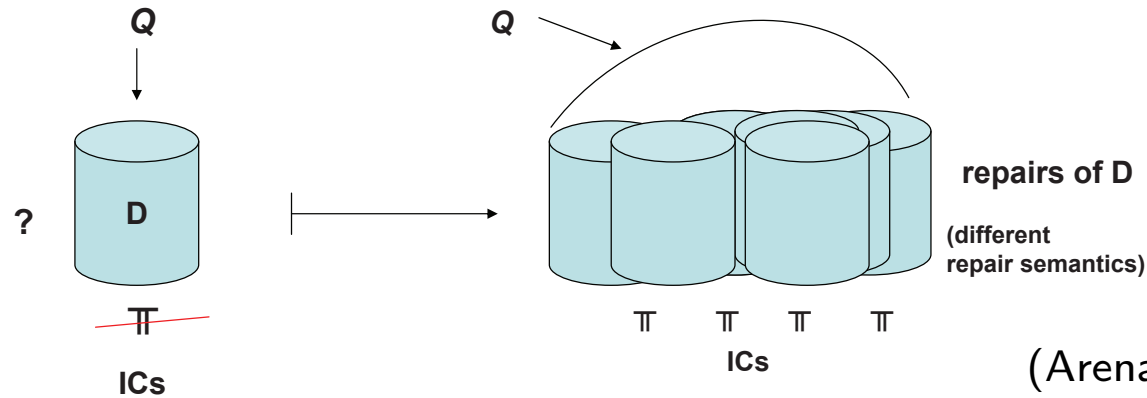
$R(a_4, a_3)$ is an actual cause for Q with contingency set $\{R(a_3, a_3)\}$

If $R(a_3, a_3)$ is removed from D , Q is still true, but further removing $R(a_4, a_3)$ makes Q false

The responsibility of $R(a_4, a_3)$ is $\frac{1}{2}$: its smallest contingency sets have size 1

$R(a_3, a_3)$ and $S(a_4)$ are actual causes, with responsibility $\frac{1}{2}$

Database Repairs



Example: Denial constraints (DC) and inconsistent DBs (also FDs)

$$\neg \exists x \exists y (P(x) \wedge Q(x, y))$$

$$\neg \exists x \exists y (P(x) \wedge R(x, y))$$

P	A
	a
	e

Q	A	B
	a	b

R	A	C
	a	c

Minimal subset-repairs (**S-repairs**): (maximal consistent sub-instance)

$$D_1 = \{P(e), Q(a, b), R(a, b)\}$$

$$D_2 = \{P(e), P(a)\}$$

Minimal cardinality-repairs (**C-repairs**): (maximum consistent sub-instance) D_1

The Repair/Causality Connection

- Assume BCQ: $Q: \exists \bar{x}(P_1(\bar{x}_1) \wedge \cdots \wedge P_m(\bar{x}_m))$

Q is (unexpectedly) true in D (or we expected $D \models \neg Q$)

What are the causes for Q to be true?

- We can obtain actual causes and contingency sets from database repairs

$\neg Q$ logically equivalent to DC:

$$\kappa(Q): \neg \exists \bar{x}(P_1(\bar{x}_1) \wedge \cdots \wedge P_m(\bar{x}_m))$$

Also written: $\leftarrow P_1(\bar{x}_1), \dots, P_m(\bar{x}_m)$

- If Q not expected to hold, we may consider D to be inconsistent wrt. $\kappa(Q)$

- Repairs of D wrt $\kappa(Q)$ may be considered ...
- First the class of S -repairs wrt. DCs

S -repairs are S -maximally consistent subsets of D (no proper subset is a repair)

→ causes and responsibilities (Salimi, Bertossi, ICDT'15)

- Collect the classes of set-differences between D and those S - or C -repairs that do not contain tuple t , and are obtained by removing a subset of D

$$Diff^s(D, \kappa(Q), t) = \{D \setminus D' \mid D' \text{ is } S\text{-repair, } t \in (D \setminus D') \subseteq D\}$$

$$Diff^c(D, \kappa(Q), t) = \{D \setminus D' \mid D' \text{ is } C\text{-repair, } t \in (D \setminus D') \subseteq D\}$$

Proposition: (causality)

$t \in D$ is an **actual cause** for Q iff $Diff^s(D, \kappa(Q), t) \neq \emptyset$

Proposition: (responsibility)

(a) $Diff^s(D, \kappa(Q), t) = \emptyset$ iff $\rho(t) = 0$

(b) Otherwise, $\rho(t) = \frac{1}{|s|}$ for a maximum-cardinality $s \in Diff^s(D, \kappa(Q), t)$

Corollary: (most responsible actual cause)

t is a **MRAC** for Q iff $Diff^c(D, \kappa(Q), t) \neq \emptyset$

So, maximum responsibility tuples are associated to C-repairs

- Similarly database repairs wrt. sets of DCs can be obtained from causes for unions of BCQs (UBCQs)
- Most computational problems related to repairs, in particular C-repairs, are provably hard (Lopatenko, Bertossi, ICDT'07)
- Techniques and results for the latter can be leveraged

This leads to **high-complexity results** for causality and **responsibility**

Some Data Complexity Results for Causality

- Causality problem (CP): Computing/deciding actual causes

(a) In **polynomial time** for CQs (Meliou et al. 2010)

(b) It also holds for UCQs

- Responsibility problem: deciding membership of

$$RDP(Q) = \{(D, t, v) \mid t \in D, v \in \{0\} \cup \{\frac{1}{k} \mid k \in \mathbb{N}^+\}, \text{ and } D \models Q \text{ and } \rho_D(t) > v\}$$

NP-complete for UCQs

(Salimi, Bertossi, ICDT'15)

In general, responsibility-related computations are hard

Answer Set Programs for Database Repairs

- ASPs can be used to specify, compute and query S- and C-repairs

Examples for S-repairs follow

Example: Schema $R(A, B, C, D)$ and FD $A, B \rightarrow C$

$$\neg \exists x y z_1 z_2 v w (R(x, y, z_1, v) \wedge R(x, y, z_2, w) \wedge z_1 \neq z_2)$$

Repair program contains the rules: (with global tuple ids)

$$R'(t_1, x, y, z_1, v, \mathbf{d}) \vee R'(t_2, x, y, z_2, w, \mathbf{d}) \leftarrow R(t_1, x, y, z_1, v), R(t_2, x, y, z_2, w), z_1 \neq z_2$$
$$R'(t, x, y, z, v, \mathbf{s}) \leftarrow R(t, x, y, z, v), \text{ not } R'(t, x, y, z, v, \mathbf{d})$$

- A stable model M of the program determines a repair D' of D :

$$D' := \{P(\bar{c}) \mid P'(t, \bar{c}, \mathbf{s}) \in M\} \quad (\text{and every repair obtained in this way})$$

Example: (cont., page 6) $\kappa(Q): \neg\exists x\exists y(S(x) \wedge R(x, y) \wedge S(y))$

Repair-ASP contains the facts (with tids):

$R(1, a_4, a_3), R(2, a_2, a_1), R(3, a_3, a_3), S(4, a_4), S(5, a_2), S(6, a_3)$

Rules:

$$\begin{aligned} S'(t_1, x, d) \vee R'(t_2, x, y, d) \vee S'(t_3, y, d) &\leftarrow S(t_1, x), R(t_2, x, y), S(t_3, y), \\ S'(t, x, s) &\leftarrow S(t, x), \text{ not } S'(t, x, d). \quad \text{etc.} \end{aligned}$$

Repair D_1 represented by model

$M_1 = \{R'(1, a_4, a_3, s), R'(2, a_2, a_1, s), R'(3, a_3, a_3, s), S'(4, a_4, s), S'(5, a_2, s), S'(6, a_3, d), \dots\}$

- For DCs and FDs repair programs can be made non-disjunctive

May be non-stratified, as in the case of FDs and DCs with self-joins

Certain query answering (QA) becomes NP-complete in data

Specifying Causes with Repair-ASPs

- Repair programs (and ASPs) provide right expressive power and complexity for causality-related computations
- Causes for the query (represented by tids) obtained by QA on the repair program Π : for each DB predicate P in a DC

$$\Pi \models_{brave} P(t, \bar{x}_i, \mathbf{d}) \quad (\text{true in some model of } \Pi)$$

Example: (cont., page 6) Causes? Define:

$$Ans(t) \leftarrow R'(t, x, y, \mathbf{d})$$

$$Ans(t) \leftarrow S'(t, x, \mathbf{d})$$

$$\text{QA: } \Pi \models_{brave} Ans(t)?$$

- For responsibility we need contingency sets associated to causes

New predicate $CauCon(t, t')$: t is an actual cause, and t' accompanies t as a member of the former's contingency set

(as captured by repair at hand or the corresponding model)

For each pair of predicates P_i, P_j in DC $\kappa(Q)$, the rule

$$CauCon(t, t') \leftarrow P'_i(t, \bar{x}_i, \mathbf{d}), P'_j(t', \bar{x}_j, \mathbf{d}), t \neq t'$$

Inequality only when P_i and P_j are the same predicate

Needed even without FDs or DCs with self-joins

Example: (cont.) Π extended with rules to compute causes with contingency sets

$$CauCon(t, t') \leftarrow S'(t, x, d), R'(t', u, v, d)$$

$$CauCon(t, t') \leftarrow S'(t, x, d), S'(t', u, d), t \neq t'$$

$$CauCon(t, t') \leftarrow R'(t, x, y, d), S'(t', u, d)$$

$$CauCon(t, t') \leftarrow R'(t, x, y, d), R'(t', u, v, d), t \neq t'$$

From model M_2 corresponding to repair D_2 : $CauCon(1, 3)$ and $CauCon(3, 1)$ from repair difference $D \setminus D_2 = \{R(a_4, a_3), R(a_3, a_3)\}$

- Contingency sets computed with extensions of ASP with set- and numerical aggregation, e.g. DLV

$$\begin{aligned}
 preCon(t, \{t'\}) &\leftarrow CauCon(t, t') \\
 preCon(t, \#union(C, \{t''\})) &\leftarrow CauCon(t, t''), preCon(t, C), not \#member(t'', C) \\
 Con(t, C) &\leftarrow preCon(t, C), not aux(t, C) \quad (\text{maximal sets}) \\
 aux(t, C) &\leftarrow CauCon(t, t'), \#member(t', C)
 \end{aligned}$$

Responsibility Computation

- Computation of a **cause's responsibility within a model/repair**:
(maybe not be overall maximum)

$$\rho(t, M) := 1/(1 + |d(t, M)|), \text{ with } d(t, M) := \{CauCon(t, t') \in M\}$$

Computed by:

$$pre\text{-}rho(t, n) \leftarrow \#count\{t' : CauCon(t, t')\} = n$$

$$rho(t, m) \leftarrow m * (pre\text{-}rho(t, m) + 1) = 1$$

- Obtaining the responsibility (a global maximum) means aggregation (optimization) over all models, not within individual models

Off-line computation: $\rho(t) = \max\{\rho(t, M) \mid M \text{ model}\}$

- Not needed: each C-repair gives such a global maximum

- C-repairs can be specified with ASPs with **weak constraints**

Example: (cont.) Add to the program

$$\Leftarrow R(t, \bar{x}), R'(t, \bar{x}, d)$$

$$\Leftarrow S(t, \bar{x}), S'(t, \bar{x}, d)$$

Only the models that minimize the number violations of the weak program constraints (here $\#$ of deleted tuples) are kept

- Local responsibilities above become global responsibilities

Conclusions

- Several classes of repairs have been investigated in the literature
- There is rather general notion of **preferred (or prioritized) repair**

(Chomicki et al., 2012)

Minimization criterion corresponds to a *priority relationship* \preceq on instances

- Optimization criteria for preferences among models of ASP programs have been considered (Gebser et al., TPLP 2011)
- **Can we use prioritized ASPs to compute prioritized repairs and causes?**

It should: our repair/causality connection is quite generic

- What about causality for Datalog queries?

For Datalog queries, cause computation can be NP-complete

Through a connection to Datalog abduction

(Bertossi, Salimi, IJAR 17)

- What is the notion of repair wrt. Datalog constraints?

E.g. navigational constraints on graph databases

- Can repairs wrt. Datalog constraints be specified by ASPs?

And causes computed with those programs?

EXTRA SLIDES