A UML-Based Approach to System Testing

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ABSTRACT

System testing is concerned with testing an entire system based on its specifications. In the context of object-oriented, UML development, this means that system test requirements are derived from UML analysis artifacts such as use cases, their corresponding sequence and collaboration diagrams, class diagrams, and possibly Object Constraint Language (OCL) expressions across all these artifacts. Our goal here is to support the derivation of functional system test requirements, which will be transformed into test cases, test oracles, and test drivers once we have detailed design information. In this paper, we describe a methodology in a practical way and illustrate it with an example. In this context, we address testability and automation issues, as the ultimate goal is to fully support system testing activities with high-capability tools.

Keywords: Testing of object-oriented systems, System testing, UML, Use Cases, Sequence Diagrams, Testability

1 INTRODUCTION

System testing is concerned with testing an entire system based on its specifications, and involves several activities such as functional testing (testing from behavioral descriptions of the system) and performance testing (response time and resource utilization) [5]. In other words, the implementation under test is compared to its intended specification. In this article, we concentrate on functional system testing and we are thus interested in deriving test cases from the analysis stage [19]. In the context of object-oriented, UML development, this means that we use UML analysis artifacts to derive system test requirements, that is a precise specification of what test scenarios should be executed. For example, use cases, their corresponding sequence or collaboration diagrams, and class diagrams can be used as a source of relevant information for testing purposes.

As mentioned in [5], little has been written about system testing for object-oriented systems as it is often believed that existing approaches (e.g., [4, 15]) apply with no loss of generality to both conventional and object-oriented systems (e.g., [12]). However, though system testing techniques are in principle implementation-independent, they depend on the notations used to represent the system specifications. In the context of UML-based object-oriented analysis, it is then necessary to develop techniques to derive system test requirements from analysis models such as use case models, interaction diagrams, or class diagrams. A recent work [2] proposes to use message sequences between objects from UML sequence diagrams and then combine it with category-partition testing [18]. The algorithms to generate message sequences and identify oracles are not described but this is nevertheless an attempt to integrate existing black-box testing techniques in the UML framework. [16] proposes test criteria to generate test cases based on statecharts. However, in most methodologies, statecharts are used to model state-dependent classes or small class clusters and, therefore, it does not apply to system testing. In [17], the authors adapt traditional data-flow coverage criteria (e.g., all definition-uses) in the context of UML collaboration diagrams but do not address test case generation. Last, some of the earlier approaches are interesting but too general as they lack detailed, operational descriptions¹.

The small amount of work regarding object-oriented system testing is also due to the fact that UML analysis models vary significantly from one development method to another. As there is no well-accepted standard method for object-oriented development, some variability in the analysis models' content and structure is unavoidable. For example, [2] does not make specific assumptions about the usage of UML use cases and sequence diagrams, e.g., use of guard conditions, modeling and indexing of alternative scenarios, and it is a reason why it is then difficult to propose algorithms to automate their testing approach. However, most development methods assume that Analysis produces use case diagrams, use case descriptions in some standard format, sequence and/or collaboration diagrams associated with each use case, a class diagram including application domain

¹ For instance in OOSE [12], system testing from use cases is not described in great details. During system testing, each use case is initially tested separately: "Basic course" and "alternative course" tests are derived. When all use cases have been tested separately, the entire system is tested as a whole. Then several use cases are executed in parallel.

objects, and possibly a set of contracts for each operation (pre- and post- conditions) and class (invariant). With the exception of use cases, this description is, for example, similar to what the Fusion method [9] proposed before UML became a standard.

Based on analysis artifacts that we precisely define in Section 2, our goal is to support the derivation of test requirements. At a later point in the development process, using test requirements and detailed design information, test cases, test oracles, and test drivers can be developed. Test requirements can be generated early, after analysis artifacts are completed. This is very important as they help devising a system test plan, size the system test task, and plan appropriate resources early in the life cycle. Once the low level design is complete, when detailed information is available regarding both application domain and solution domain classes, then test requirements can be used to derive test cases, test oracles, and test drivers.

One important issue is the one of *testability*: The degree to which a model (in our case, a UML diagram) has sufficient information to allow automatic generation of test cases [5]. Since the use of the UML notation is not constrained by any particular, precise method, one can find a great variability in terms of the content and form of UML artifacts, whether at the analysis or design stages. However, the way UML is used determines the testability of the produced UML artifacts. We therefore address the testability requirements we need to impose on UML artifacts – and therefore on any development methodology – to be able to support functional system testing efficiently (Section 4).

Another important aspect is *automation*. Large systems are inherently complex to test and require, regardless of the test strategy, large numbers of test cases. If a system testing method requires the tester to perform frequent, complex manual tasks, then such a method is not likely to be usable in a context where time to market is tight and qualified personnel is scarce. Therefore, the potential for automation of a test methodology is an important criterion to consider (Section 5).

The paper starts by providing an overview of our methodology for system testing, referred to as the TOTEM² methodology (Section 2). Section 3 then gets into the core of

² This is named after the project that this work is part of: http://www.sce.carleton.ca/Squall/Totem/.

the paper, describing the procedure we use to derive functional test requirements, using a system analysis example that is further detailed in the appendices. Section 4 summarizes the testability requirements of our approach and justifies the decisions and trade-offs that were made. Section 5 is dedicated to automation issues. Section 6 then concludes and outlines future work.

2 OVERVIEW OF THE TOTEM SYSTEM TEST METHODOLOGY

The TOTEM system test methodology, as far as deriving test requirements is concerned, is based on the artifacts produced at the end of the Analysis development stage. These artifacts include:

- Use case diagram;
- Use case descriptions;
- Sequence or collaboration diagrams for each use case;
- Class diagrams composed of application domain classes;
- A data dictionary that describes each class, method, and attribute.

In addition, as discussed further in Section 4, we assume each class is characterized by a class invariant expressed with OCL and each operation is described by a contract in OCL, detailing pre- and post-conditions [21].

Those artifacts are similar, though we use a different terminology, with what is proposed by Fusion [9]. Furthermore, as discussed in detail in Section 3, use cases have sequential constraints that have to be specified. Such constraints are the direct result of the logic of the business process the system purports to support³. In other words, use case scenarios are usually not executed in arbitrary orders. Some use case scenarios need to be executed before others. We can think, for example, of a library system⁴ where a user needs to register before being able to borrow a book. Registering and borrowing correspond to different use cases and, for a given library user, one has to be performed before the other. Therefore, in addition to the artifacts above, we will see that one of our testability

³ This aspect bears some similarity with the notion of *life-cycle model* in Fusion.

⁴ We use a Library system as a running example throughout the paper, as it is readily understandable by all readers. Details regarding the analysis artifacts are provided in the appendices.

requirements is to specify such sequential constraints, for example in the form of an activity diagram [8].

Figure 1 summarizes the steps of the TOTEM system testing methodology. In this paper, we will focus on activities A2, A3, and A5 and leave the evaluation of their relative cost to future work. A1 is the first step where we check that the provided UML diagrams are complete and fulfill our testability requirements. A4 is not addressed here though it is an important contribution to test requirements [5] and is to be addressed by future work. However, activities A2, A3, and A5 constitute by themselves a self-contained methodology and the fact that A4 is missing will not affect the validity and usefulness of what we present in this paper.



Figure 1 – TOTEM System Test Steps (activity diagram)

Once testability is ensured (A1), we go on to derive test requirements from the different artifacts (from A2 to A5). Then these requirements are merged into one set of test requirements, thus avoiding redundancy and combining test requirements into one test plan. A7 and A8 are concerned with generating the test cases and code for oracles, and embedding them into executable test drivers. These steps are typically performed at a later stage once detailed design information is available and they will not be discussed

here. One important objective of TOTEM is to provide a systematic methodology to perform the activities presented above and to automate them to the maximum extent possible.

3 GENERATING SYSTEM TEST REQUIREMENTS AT THE COMPLETION OF ANALYSIS

This section covers the steps A2, A3, and A5 of the TOTEM system test methodology in a chronological order, covering each activity with one subsection.

3.1 Generating Use Case Sequences

Use cases are a first good source for deriving system test requirements. After all they represent the high level functionalities provided by the system to the user . But they are usually not independent. Not only they may have <<extend>> and <<include>> dependencies but they may also have *sequential* dependencies [5, 8] which stem from the logic of the business process the system supports. When planning test cases for use cases, we need to identify *possible* execution sequences of use cases. We aim at "covering" such use case sequences during testing as they may trigger different failures.

In this section, we will provide an overview of the principles underlying the representation and generation of possible use case test sequences. These principles are formalized by the description of algorithms provided in Appendix H. In a subsequent subsection, we provide a detailed, illustrative example based on the Library system.

3.1.1 Representation of Use Case Sequential Dependencies

We represent sequential dependencies between use cases by the means of an activity diagram for each actor in the system [8]. Such a representation will facilitate the identification and visualization of these dependencies by application domain experts, as activity diagrams are easy to interpret.

In such a diagram, the vertices are use cases and the edges are sequential dependencies between the use cases: An edge between two use cases (from a tail use case to a head use case) specifies that the tail use case must be executed in order for the head use case to be executed, but the tail use case may be executed without any execution of the head use case. In addition, specific situations require that several use cases be executed independently (without any sequential dependencies between them) for another use case to be executed, or after the execution of this other use case. This is modeled by *join* and *fork* synchronization bars in the activity diagram, respectively.

To be more precise, the vertices of our activity diagram are *extended* use cases, as described in [5]. Whether explicitly specified or not, use cases have parameters that determine the behavior they can exhibit, as well as output values (results of their execution). Extended use cases require *Formal* use case parameters to be defined by providing their type (either basic UML type or user-defined type) and kind, i.e., whether they are in, out, or inout, like for operations. Furthermore, *Actual* use case parameters are represented in the activity diagram by simply listing them between brackets. The reason to have actual parameters in this context is to show the dependencies between parameters during the execution of a path in the activity diagram, e.g., an out parameter from one use case being an in parameter of a subsequent use case.

The use cases are grouped into *swimlanes*⁵, according to their responsibilities in terms of manipulated objects (application domain classes). Each swimlane represents what is referred to as *Entity-life histories* in [11]. Entity-life histories describe the life cycle of an application domain object (in the Analysis class diagram) from their creation in the system, through all the functions being performed on them, to their destruction. If not related by cross-swimlanes sequential dependencies or synchronizations (or their transitive closure), use cases from different swimlanes are independent, and thus can occur independently, in any order. This is modeled by the concept of *interleaving* when modeling sequences in the Fusion method [9].

An example from our Library system (see use case diagram in Appendix A) can be found in Figure 2 (use cases are identified by their name and also, for brevity, by a capital letter from A to K). Formal parameters are provided for each use case in Appendix B. Such definitions should be part of any template to define use cases so as to make them testable [5]. Actual parameters, such as uid (user ID), are visible within each action state in the activity diagram and can be mapped to their corresponding formal parameter based on their ordering.

⁵ Swimlanes partition an activity diagram to assign responsibilities for actions to objects [6].



Figure 2 – Use Case Sequential Constraints for the Librarian (activity diagram)

This activity diagram is built for the Librarian (actor) and, in general, one diagram should be provided for each actor. If we use this example to illustrate some of the concepts presented above, the sequential dependency between AddTitle and RemoveTitle specifies that AddTitle must be executed first in order to execute RemoveTitle, but the execution of AddTitle does not require the execution of RemoveTitle. Both AddUser and AddItem need to be executed before BorrowLoanCopy can, as modeled by a join synchronization. Regarding actual parameters, isbn is required as an input by RemoveTitle (and matches formal parameter isbn: Integer in Appendix B) and uid and itemid are input parameters required by the BorrowLoanCopy use case (matching formal parameters uid: Integer and itemid: Integer).

3.1.2 Generation of Use Case Sequences

In this context, our objective is to generate legal sequences of use cases (according to the sequential dependencies specified in the activity diagram), in a fully automated way. Those use case sequences will constitute the first component of the system test requirements.

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Paths in the activity diagram represent a possible life history for an object type (e.g., path⁶ AddUser.RemoveUser for class User) or a combination of object types (e.g., path AddTitle.AddItem.RemoveItem.RemoveTitle for classes Title and User). The activity diagram in Figure 2 specifies an infinite number of paths, a property due to the loop between use cases CollectFine and RenewLoan. However, given that a loan can be renewed only twice, the number of paths between use cases BorrowLoanCopy and ReturnLoanCopy equals 14, thus leading to 130 paths in the whole activity diagram⁷. Note that when the maximum number of times a loop can be taken is too high (thus leading to too many paths), we can use a strategy similar to what is used to test loops in code (i.e., we can make sure that each loop is bypassed – if possible, taken only once, a representative or average number above 1, and a maximum number of times).

Paths are first determined through a simple depth-first search (that accounts for loops) in the directed graph corresponding to our activity diagram. Then we need to determine dependencies in terms of actual parameter values between the use cases in a path. For instance, in path AddTitle.AddItem.RemoveItem.RemoveTitle, parameter isbn for use case AddItem must be identical to parameter isbn in AddTitle. Similarly, the itemid (resp. isbn) removed in use case RemoveItem (resp. RemoveTitle) must be the one added in AddItem (resp. AddTitle). Such dependencies among actual parameter values are needed in order to identify the data flow between use case executions, something that will be necessary for the generation of test input data. They can simply be determined based on the actual parameters in our activity diagram, such parameters serving as placeholders for actual values. We can simply document such dependencies by adding actual parameters into the use case sequences, which are referred to as *parameterized* use case sequences. Using the example path above, we obtain:

AddTitle(isbn).AddItem(isbn,itemid).RemoveItem(itemid).RemoveTitle(isbn)

⁶ We use '.' to denote the sequence of two use cases in a path (like regular expressions).

⁷ Given that node E can appear at the most twice in a path, there are 14 possible paths between nodes D and F (a tree representing these paths is easy to build). Nodes A, I, and G (with I always before G) must be taken before D, thus leading to 3 possibilities (A.I.G, I.A.G, I.G.A). The same situation occurs after node F, with nodes C, H, and J. Then there are 3 x 3 x 14 = 126 paths involving all nodes from A to J. There exist four other paths: K, I.J, I.G.H.J, and A.C.

If we execute any path between AddTitle and RemoveTitle, such as the one above which is an output of the depth first search, use cases AddTitle and AddItem are executed at most once. That is, at best, each title corresponds to only one item in the library. If we want to test our Library system under more realistic situations, we obviously need more than one item per title and more than one loan per user and item. We also need to proceed with large number of users, items, and loans if we want to test the scalability of our system.

As a consequence, our construction of use case sequences may need to instantiate several times, with different values, the parameters of a number of use cases specified by the activity diagram. The number of times use case parameters must be instantiated is determined by the information provided by tester in terms of the scale of the test to take place, e.g., the (average) number of users, or items per title. In the simple example where 2 items and 1 title must be created, we get two *instantiated* use case sequences (S1, S2) from the parameterized sequence above, where title1, item1, and item2 are symbolic values⁸ for the isbn and itemid parameters:

S1:AddTitle(title1).AddItem(title1,item1).RemoveItem(item1).RemoveTitle(title1)
S2:AddTitle(title1).AddItem(title1,item2).RemoveItem(item2).RemoveTitle(title1)

Similarly, the tester must indicate constraints on dependency loops, e.g., in our Library system use case RenewLoan can be executed at most twice for a particular loan. Furthermore, the test strategy for loops needs to be specified in ways that are similar to code loop testing, as discussed above. This is necessary to determine which use case sequences need to be tested.

At this point, all instantiated use case sequences need to be combined to generate *complete* sequences to be tested. This is due to the fact that the sequences we have generated so far are incomplete as synchronizations were not accounted for. For our simple example above (S1, S2), a possible combined sequence is:

AddTitle(title1).AddItem(title1,item1).AddItem(title1,item2).
RemoveItem(item2).RemoveItem(item1).RemoveTitle(title1)

⁸ They are just place holders for values to be assigned based on formal parameters type analysis.

The combination of instantiated use case sequences must be carefully performed as it must preserve the use case dependencies and avoid the duplication of instantiated use cases. This can be formalized by the concept of interleaving [9] (where || denotes interleaving in a sequence) and implemented as such to derive possible sequences. In our simple example, the two sequences (S1, S2) would be combined as:

Let us take a more general example and suppose we have to combine the two following sequences:

```
prefix<sub>1</sub>.X.middle<sub>1</sub>.Y.suffix<sub>1</sub>
prefix<sub>2</sub>.X.middle<sub>2</sub>.Y.suffix<sub>2</sub>
```

where x and Y represent common instantiated use cases and the prefix/middle/suffixkeywords represent any subsequence. It is implied that $prefix_1$ and $prefix_2$ (and middle₁ and middle₂, and suffix₁ and suffix₂, respectively) are instantiated use case sequences that do not have common elements (same use case with the same symbolic values). They show different indices so as to express that their corresponding subsequences are different. In this situation, the resulting set of sequences to test can be modeled and derived using interleaving:

```
(prefix<sub>1</sub> || prefix<sub>2</sub>).X.(middle<sub>1</sub> || middle<sub>2</sub>).Y.(suffix<sub>1</sub> || suffix<sub>2</sub>)
```

From this example, we can understand what the general procedure to combine instantiated use case sequences will look like. Common instantiated use cases will be identified across pairs of sequences and, for each pair, all the subsequences in between each common, instantiated use cases will be combined using interleaving. This procedure will be performed for all pairs of sequences extracted from the activity diagram. Furthermore, when performing the interleaving to generate sequences, we will only sample a subset of all possible resulting sequencing in order to avoid a combinatorial explosion.

3.1.3 Summary

To summarize (Figure 3), parameterized use case sequences are derived from the activity diagram. Given the information provided by the tester about the scale of testing, these sequences are instantiated (with symbolic values) and then combined using an iterative procedure in order to obtain the final instantiated use case sequences to be tested. In a subsequent step, which is out of the scope of this paper, actual values for these symbolic values will have to be (e.g., randomly) generated by analyzing the type of the corresponding use cases' formal parameters.



Figure 3 – Steps for Extracting Use Case (UC) sequences to be tested

All three activities in Figure 3 must be automated. We discuss below the complexity of doing so:

- 1 The derivation of parameterized use case sequences from the (augmented) UML activity diagram can easily be done with a depth first search through a directed graph capturing the activity diagram in Figure 2.
- 2 The derivation of instantiated use case sequences from the test scale information provided by the tester does not require any complex algorithm either. Recall that we

want to cover all parameterized test sequences. In addition, we want now to "cover" as many instances of each class as specified by the tester. Typically, parameterized sequences will be instantiated several times so as to fulfill the test scale specification.

3 This is the most complex activity to automate. It requires the identification of common instantiated use cases across sequences, which indicate either a synchronization or a common initial subsequence. Subsequences between synchronizations are then interleaved to generate complete use case sequences. However, as we will see, it is not practical, in most cases, to generate all possible sequences so some random sampling is likely to be necessary.

We will now illustrate the details of each step by using our working example.

3.1.4 Example

In this section we show how, in the case of our Library system, the three activities in Figure 3 produce complete use case sequences to be tested. In Step 1, parameterized use case sequences are derived from a directed graph (Figure 4) corresponding to the activity diagram that describes sequential dependencies between use cases (Figure 2). Such a directed graph can be derived by transforming join and fork synchronizations into regular edges, e.g, join synchronization from activities A and G to activity D in Figure 2 are transformed into an edge from A to D and an edge from G to D (Figure 4).

From this directed graph, a depth-first search, that takes into account that edge E (use case RenewLoan) cannot be taken more than twice, produces 60 paths that we show as a tree in Figure 5. Those path represent possible sequences of parameterized use cases that can be executed. In this figure, any path that begins with Start.A.D eventually reaches F and continues with either C.End or H.J.End. Due to space constraints, we omitted this last alternative in all these paths (denoted with '...'). For the same reason, all the branches from D are omitted in the paths that start with Start.I.G.D.



Figure 4 – Directed Graph corresponding to activity diagram in Figure 2.



Figure 5 – Tree derived from directed graph in Figure 4

Step 2 in Figure 3 requires test scale information. Let us assume that the tester wants: 2 users, 3 titles, 2 items per title, 1 loan per user, no renew or collect fine for loans, and no system monitoring. Such a situation, though not representative of a realistic use of the Library system, is deemed adequate as it implies a small number of sequences (7 out of 60 are now possible) but allows us to illustrate all the steps. For that particular example, Table 1 summarizes the requirements for the derivation of instantiated use case sequences. The first row presents the parameterized use case sequences to be tested. The

last sequence, using interleaving, models 9 sequences⁹. The second row shows, for each class, the parameter instances (using place holders as symbolic values) corresponding to the test scale specified by the tester. The instantiation of parameterized use case sequences is aimed to replace actual parameters with symbolic values as derived from the test scale information. Note that, in Table 1, Loan instances are characterized by pairs (uid, itemid) and that we do not use symbolic values for Loan instances. This stems from the fact that a loan is uniquely identified by a user and item and that there is no use case parameter of type Loan.

Parameterized Use Case Sequences	 A(uid).C(uid) I(title).J(title) I(title).G(title, item).H(item).J(title) (A(uid) I(title).G(title,item)).D(uid,item). F(uid,item).(C(uid) H(item).J(title))
Parameter Instances (Symbolic values)	 Users (2): u1, u2 Titles (3): t1, t2, t3 Items (one per title): (t1, i11), (t1, i12), (t2, i21), (t2, i22), (t3, i31), (t3, i32) Loans (one per user and item): pairs (u1, i22) and (u2, i32)

 Table 1 – Requirements for the derivation of instantiated use case sequences.

The instantiation selects one parameterized sequence at a time, assigns actual parameters with symbolic values, and starts again from the first sequence if symbolic values are still to be assigned after covering all sequences. So the instantiated use case sequences we obtain are, to some extent, arbitrary, as it selects parameterized sequences and symbolic values in arbitrary orders. But what is important is that these sequences fulfill our requirements: They cover the parameterized use case sequences and match the test scale specification. Regarding our example, following the orders in Table 1, we would obtain the following 8 instantiated use case sequences:

Seq1: A(u1).C(u1)
Seq2: I(t1).J(t1)
Seq3: I(t2).G(t2, i21).H(i21).J(t2)

 $^{^{9}}$ There are three possibilities for the two interleavings in the sequence (e.g., A||I.G produces sequences A.I.G, I.A.G, and I.G.A), and thus a total of 9 sequences.

Seq4: I(t3).A(u2).G(t3,i32).D(u2,i32).F(u2,i32). C(u2).H(i32).J(t3) Seq5: I(t1).G(t1, i11).H(i11).J(t1) Seq6: I(t1).G(t1, i12).H(i12).J(t1) Seq7: A(u1).I(t2).G(t2,i22).D(u1,i22).F(u1,i22).H(i22). C(u1).J(t2) Seq8: I(t3).G(t3, i31).H(i31).J(t3)

We can see that we end up with 4 and 2 instances of the 3rd and 4th sequence in Table 1, respectively. This is necessary in order to cover all parameter instances.

Another issue is that some sequences are included in others. What we mean is that all the instantiated use cases in one sequence are present, in the same order, in another sequence. For example, Seq1 and Seq2 are included in Seq7 and Seq5, respectively. In order to decrease the number of sequences, a reasonable heuristic is to keep only sequences that are not included in others. In our example, we would then obtain the following final set of sequences: {Seq3, Seq4, Seq5, Seq6, Seq7, Seq8}.

Instantiated use case sequences are then combined together, in a stepwise manner, to produce *complete* use case sequences to be tested (Step 3 in Figure 3). Each time two sequences are combined¹⁰, interleaving of instantiated use case subsequences can occur, thus possibly leading to large numbers of complete sequences to be tested. In practice, a reasonable number of sequences will have to be determined, e.g., by sampling the entire set of sequences in order to maintain the number of test sequences under a threshold. Regarding our example, we illustrate a complete series of interleaving steps leading to a complete test sequence but we only show one resulting test sequence at each step.

First, following the order of sequences, Seq3 and Seq4 are combined and produce 495 interleavings¹¹ which include:

¹⁰ Recall that common elements must be identified first. Algorithms for the combination of sequences are provided in Appendix H.

¹¹ We use this term as a shorthand for sequences resulting from the interleaving of a pair of sequences. Given two sequences S1 and S2 of length n and m, respectively, the number of interleavings from S1 and S2 is C(m+n, n) = (m+n)!/(n!m!).

Then, Seq5 and S are combined and produce 1820 interleavings which include:

Seq6 and S^1 produce 45 interleavings (two elements in common) which include:

Seq7 and S^2 produce 18018 interleavings which include:

In this particular case, we perform the interleaving of 2 sequences which have 2 common instantiated use cases (I(t2), J(t2)). The subsequences between them are interleaved as illustrated by the following table. The total number of possible interleavings results from multiplying the number of interleavings of subsequences between common instantiated use cases (18018 = 6 * 3003).

Seq7	A(u1).		G(t2,i22).D(u1,i22). F(u1,i22).H(i22). C(u1).		
Common		I(t2).		J(t2)	
S ² 1	I(t3).I(t1). G(t1,i11). G(t1,i12). A(u2).		G(t3,i32).H(i11). G(t2,i21).D(u2,i32). H(i12).H(i21).J(t1). F(u2,i32).C(u2).H(i32).		J(t3)
	6 interleavings		3003 interleavings		

The last step shown here leads to a complete instantiated use case sequence to be tested. Seq8 and S^3 produce 276 interleavings (two elements in common, i.e., I(t3) and J(t3)) which include:

To address step A7 in Figure 1, symbolic values will have to be substituted to actual ones. This will require to perform a type analysis of the corresponding formal parameters in the use case descriptions (Appendix B) and generate legal values that

satisfy a number of constraints. This is out of the scope of this paper and will be addressed by future work.

3.2 Identifying Use Case Scenarios

To each use case corresponds an interaction model, i.e., either a collaboration or a sequence diagram. These diagrams show how the use case is realized through the interactions of objects, that is instances of classes in the analysis class diagrams. In practice, such diagrams may be decomposed into several interconnected diagrams, for the sake of legibility. But these diagrams still represent one interaction model describing alternative object interactions, each of them realizing one possible scenario of a use case. In many cases, an interaction diagram models one *nominal* scenario and a number of error/exceptional scenarios, where the system has to react appropriately. At the analysis stage, interaction diagrams may also be seen as modeling alternative execution *sequences* of public operations belonging to application domain classes, each alternative sequence capturing a scenario.

In the previous section, we have seen how to derive use case sequences that should be part of the test plan. Now, using the interaction diagrams associated with use cases, we have to go down one more level into details, and derive sequences of use case *scenarios* to be tested. This bears some similarity with the work of [17] on deriving operation sequences from collaboration diagrams. The main difference lies in the fact that the authors make use of low-level design information (e.g., data flow within operations) rather than analysis documents. Furthermore, the issues of initial test conditions and test oracles are not addressed.

Let us illustrate the procedure we propose using an example and then summarize this procedure. Figure 6 presents a sequence diagram for the use case Remove Title. The class diagram for our library system and other sequence diagrams that we will use in this example are provided in Appendices C and D, respectively.



Figure 6 – Analysis Sequence Diagram for Remove Title (after merging it with *included* use cases)

Note that UML conventions for numbering messages in sequence diagrams have been extended to better address alternatives [10]: Capital letters are used to denote alternatives. In Figure 6, message numbered 1.2.1 is the main branch, and message numbered 1.2.1A is the alternative. Given this extension, both sequence and collaboration diagrams can equally be used to derive sequences of use case scenarios as described in this section. We describe here the procedure using sequence diagrams since they are more often used during Analysis than collaboration diagrams (e.g., [8]).

3.2.1 Expressing Sequence Diagrams as Regular Expressions

In order to represent them in an analyzable and compact form, the sequence diagrams can be re-expressed as a regular expression whose alphabet are the public methods of the objects playing a role in sequence diagrams. So, for example, for Remove Title, this would yield the following regular expressions where we use the notation $Operation_{class}$ to denote which operation is executed and to which class it belongs¹²:

```
Remove Title ->
RequestTitleInfo<sub>LibrarianTerminal</sub>.create<sub>TitleControl</sub>.requestTitleInfo<sub>TitleControl</sub>.
(
    getItem<sub>Title</sub>.displayTitleInfo<sub>LibrarianTerminal</sub>.displayTitleInfo<sub>User</sub>.
    displayItemInfo<sub>User</sub>*.removeTitle<sub>LibrarianTerminal</sub>.removeTitle<sub>TitleControl</sub>.
    (destroy<sub>Title</sub>.destroy<sub>Item</sub>*+loanORreservationExist<sub>LibrarianTerminal</sub>)+
    titleNotExist<sub>LibrarianTerminal</sub>.titleNotExist<sub>User</sub>).exit<sub>LibrarianTerminal</sub>.destroy<sub>TitleControl</sub>
```

To automate the transition to regular expressions, the sequence diagram can be modeled as a labeled graph (where the labels are the operations) and matrix based algorithms can be used to automatically derive the corresponding regular expression [4].

The next step, in order to be able to identify scenarios, is to re-express the regular expression above in a *sum-of-products* form (here 3 *product terms* separated by "+"):

```
RequestTitleInfo_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.
getItem_Title.displayTitleInfo_LibrarianTerminal.displayTitleInfo_User.
displayItemInfo_User*.removeTitle_LibrarianTerminal.removeTitle_TitleControl.
destroy_Title.destroy_Item*.exit_LibrarianTerminal.destroy_TitleControl
+
RequestTitleInfo_LibrarianTerminal.create_TitleControl.requestTitleInfo_User.
displayTtemInfo_User*.removeTitle_LibrarianTerminal.removeTitle_TitleControl.
displayTtemInfo_User*.removeTitle_LibrarianTerminal.removeTitle_TitleControl.
loanORreservationExist_LibrarianTerminal.loanORreservationExist_User.
exit_LibrarianTerminal.destroy_TitleControl
+
RequestTitleInfo_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.
loanORreservationExist_LibrarianTerminal.loanORreservationExist_User.
exit_LibrarianTerminal.destroy_TitleControl
+
RequestTitleInfo_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.titleNotExist_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.titleNotExist_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.titleNotExistUser.exit_LibrarianTerminal.destroy_TitleControl
```

Each product term represent either a use case scenario or a set of scenarios if iteration symbols are present.

3.2.2 Identifying Path Realization Conditions for Product Terms

From our example above, we have obtained a regular expression with three product terms (referred to below as Term 1, 2, and 3, respectively). Each term is associated with a number of conditions enabling or disabling its execution. Indeed, associated with each path within a sequence/collaboration diagram, one can derive from the guard conditions associated with these paths, the conjunction of conditions that must be fulfilled for that

¹² We do not address here the issue of overloading. In that case, the name is not enough and the operation signatures are required to model sequence diagrams as regular expression.

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path to be enabled. Recall we require that these conditions be expressed in the Object Constraint Language (OCL) so as to be unambiguous [21]. So for Term 1 listed above, the *path realization condition* is:

Term1, path realization condition:

```
self.titleControl.title ->exists(t:Title | t.isbn=isbn) and
(self.loancopy->select(loancopyStatus=onloan)->size=0 and
self.title.titleReservationCounter=0)
```

In the path realization conditions, the elements that do not take part in a navigation expression, e.g., isbn, can either be parameters of the operation that triggered the use case or strings matching enumeration types, e.g., onloan.

Note that OCL guard conditions, which compose the conjuncts of path realization conditions such as the one above, have to be re-expressed as they assume different *contexts*¹³ in the interaction diagrams. The transformation should ensure that every guard condition in the path realization condition uses the same context. It is convenient to assume, as a general rule, that the *boundary class* [8] corresponding to the use case executed¹⁴ (e.g., LibrarianTerminal in our example) be used as a common context.

For Term 2, the situation is a bit more complex than for Term 1. The path realization condition is:

Term2, path realization condition:

```
self.titleControl.title->exists(t:Title | t.isbn=isbn) and
(self.titleControl.loancopy->select(loancopyStatus=onloan)->
size>0 or self.titleControl.title.titleReservationCounter>0)
```

Because the above condition contains a disjunction, it can be satisfied in three ways:

Term2, Condition 1:

```
self.titleControl.title ->exists(t:Title | t.isbn=isbn) and
(self.titleControl.loancopy->select(loancopyStatus=onloan)-> size>0
and self.titleControl.title.titleReservationCounter>0)
```

¹³ We use the OCL definition of *context* here [21]. In a sequence diagram, the context of an OCL guard condition is the message source class. All attributes and operations of this class can be used directly. Public attributes and operations of other classes can be reached through OCL navigation.

¹⁴ There are, in most cases, several boundary classes involved in a use case. But one actor *initiates* the use case through a specific boundary class. This is this particular class we refer to here.

Term2, Condition 2:

```
self.titleControl.title ->exists(t:Title | t.isbn=isbn) and
(self.titleControl.loancopy->select(loancopyStatus=onloan)-> size>0
and self.titleControl.title.titleReservationCounter=0)
```

Term2, Condition 3:

```
self.titleControl.title ->exists(t:Title | t.isbn=isbn) and
(self.titleControl.loancopy->select(loancopyStatus=onloan)-> size=0
and self.titleControl.title.titleReservationCounter>0)
```

It is important that all three conditions be tested as the implementation may not implement one or more cases correctly and not testing one of them could lead to the nondetection of a fault in the implementation of the path realization condition of Term 2. This issue is related to the literature on testing logic expressions [5]. Complex conditions need to be tested by exercising operation sequences under several alternative conditions. These alternatives correspond to the different combinations of truth values of logical clauses in a path realization condition such that this condition holds true.

3.2.3 Specifying Operation Sequences

Having identified the test conditions under which each term is going to be executed and therefore tested, we need to identify the precise operation sequences to be executed for each term. Since product terms may contain iteration symbols (*, +), precise sequences to be tested need to be defined by giving those iteration symbols actual values. We can use a strategy which is similar to what we did earlier to cover use case sequences: The iteration is bypassed (for * only), performed once, an intermediary number of times (possibly a statistical median if available), and a maximum M number of times. Term 3 has no iteration symbol. If we take Term 2 – which is simpler than Term 1 – as a first example, the sequences obtained using this strategy are:

Term 2, sequence 1: displayItemInfo_{User} is bypassed

 $\begin{array}{l} \label{eq:control} \mbox{RequestTitleInfo}_{\mbox{LibrarianTerminal}}.\mbox{create}_{\mbox{TitleControl}}.\mbox{requestTitleInfo}_{\mbox{LibrarianTerminal}}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{removeTitle}_{\mbox{LibrarianTerminal}}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{removeTitle}_{\mbox{LibrarianTerminal}}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{librarianTerminal}.\mbox{displayTitleInfo}_{\mbox{User}}.\mbox{d$

Term 2, sequence 2: displayItemInfo_{User} is executed once

$$\begin{split} & \texttt{RequestTitleInfo}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{TitleControl}}.\texttt{requestTitleInfo}_{\texttt{TitleControl}}.\\ & \texttt{getItem}_{\texttt{Title}}.\texttt{displayTitleInfo}_{\texttt{LibrarianTerminal}}.\texttt{displayTitleInfo}_{\texttt{User}}. \end{split}$$

$$\label{eq:list_list_result} \begin{split} \text{displayItemInfo}_{\text{\tiny User}}.\texttt{removeTitle}_{\text{\tiny LibrarianTerminal}}.\texttt{removeTitle}_{\text{\tiny TitleControl}}.\\ \text{loanORreservationExist}_{\text{\tiny LibrarianTerminal}}.\texttt{exit}_{\text{\tiny LibrarianTerminal}}.\text{destroy}_{\text{\tiny TitleControl}} \end{split}$$

Term 2, sequence 3: displayItemInfo_{User} is executed twice (intermediary value)

 $\begin{array}{l} \label{eq:result} {\sf RequestTitleInfo}_{{\scriptstyle {\rm LibrarianTerminal}}}.{\sf create}_{{\scriptstyle {\rm TitleControl}}}.{\sf requestTitleInfo}_{{\scriptstyle {\rm TitleControl}}}.\\ {\sf getItem}_{{\scriptstyle {\rm Title}}}.{\sf displayTitleInfo}_{{\scriptstyle {\rm User}}}^2.{\sf removeTitle}_{{\scriptstyle {\rm LibrarianTerminal}}}.{\sf removeTitle}_{{\scriptstyle {\rm TitleControl}}}.\\ {\sf displayItemInfo}_{{\scriptstyle {\rm User}}}^2.{\sf removeTitle}_{{\scriptstyle {\rm LibrarianTerminal}}}.{\sf removeTitle}_{{\scriptstyle {\rm TitleControl}}}.\\ {\sf loanORreservationExist}_{{\scriptstyle {\rm LibrarianTerminal}}}.{\sf exit}_{{\scriptstyle {\rm LibrarianTerminal}}}.{\sf destroy}_{{\scriptstyle {\rm TitleControl}}}.\\ \end{array}$

Term 2, sequence 4: displayItemInfouser is executed a maximum M number of times

RequestTitleInfo_{LibrarianTerminal}.create_{TitleControl}.requestTitleInfo_{TitleControl}. getItem_{Title}.displayTitleInfo_{LibrarianTerminal}. displayTitleInfo_{User}.displayItemInfo_{User}.removeTitle_{LibrarianTerminal}. removeTitle_{TitleControl}. loanORreservationExist_{LibrarianTerminal}.exit_{LibrarianTerminal}.destroy_{TitleControl}

The maximum number of iterations M represents the number of items corresponding to a

title, modeled in OCL by title.item->size in the UML interaction diagram. The specific number of items depends on the test scale information provided by the tester (see Section 3.1).

If we now turn our attention to Term 1, which contains 2 iteration symbols:

Term 1, sequence 1:

```
\begin{array}{l} \label{eq:constraint} RequestTitleInfo_{\tt LibrarianTerminal}.create_{\tt TitleControl}.requestTitleinfo_{\tt TitleControl}.\\ getItem_{\tt Title}.displayTitleInfo_{\tt LibrarianTerminal}.displayTitleInfo_{\tt User}.\\ removeTitle_{\tt LibrarianTerminal}.removeTitle_{\tt TitleControl}.\\ exit_{\tt LibrarianTerminal}.destroy_{\tt titleControl}\end{array}
```

Term 1, sequence 2:

```
\begin{split} & \text{RequestTitleInfo}_{\text{LibrarianTerminal}}.\text{create}_{\text{TitleControl}}.\text{requestTitleinfo}_{\text{TitleControl}}.\\ & \text{getItem}_{\text{Title}}.\text{displayTitleInfo}_{\text{LibrarianTerminal}}.\text{displayTitleInfo}_{\text{User}}.\text{display}\\ & \text{ItemInfo}_{\text{User}}.\text{removeTitle}_{\text{LibrarianTerminal}}.\text{removeTitle}_{\text{TitleControl}}.\\ & \text{destroy}_{\text{Title}}.\text{destroy}_{\text{Item}}.\text{exit}_{\text{LibrarianTerminal}}.\text{destroy}_{\text{TitleControl}} \end{split}
```

Term 1, sequence 3:

```
\begin{split} & \texttt{RequestTitleInfo}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{TitleControl}}.\texttt{requestTitleinfo}_{\texttt{TitleControl}}.\\ & \texttt{getItem}_{\texttt{Title}}.\texttt{displayTitleInfo}_{\texttt{LibrarianTerminal}}^2 \texttt{.removeTitle}_{\texttt{LibrarianTerminal}}.\texttt{removeTitle}_{\texttt{LibrarianTerminal}}.\texttt{removeTitle}_{\texttt{TitleControl}}.\\ & \texttt{veTitle}_{\texttt{TitleControl}}.\texttt{destroy}_{\texttt{Title}}.\texttt{destroy}_{\texttt{Titme}}^2 \texttt{.exit}_{\texttt{LibrarianTerminal}}.\\ & \texttt{destroy}_{\texttt{TitleControl}}.\\ \end{split}
```

Term 1, sequence 4:

```
\begin{array}{l} {\tt RequestTitleInfo}_{{\tt LibrarianTerminal}}.{\tt create}_{{\tt TitleControl}}.{\tt requestTitleinfo}_{{\tt TitleControl}}.{\tt getItem}_{{\tt Title}}.{\tt displayTitleInfo}_{{\tt LibrarianTerminal}}\cdot{\tt M}\\ {\tt displayTitleInfo}_{{\tt User}}.{\tt displayItemInfo}_{{\tt Uger}}{\tt M}.{\tt removeTitle}_{{\tt LibrarianTerminal}}.{\tt remo}\\ {\tt veTitle}_{{\tt TitleControl}}.{\tt destroy}_{{\tt Title}}.{\tt destroy}_{{\tt Item}}.{\tt exit}_{{\tt LibrarianTerminal}}.{\tt destroy}_{{\tt TitleControl}}.{\tt dest
```

In the sequences above, the two iteration symbols are inter-dependent. More specifically, they must be the same since they are both determined by the number of *items* associated with a *title*. In general we have to expect such dependencies between iteration symbols.

Such dependencies can automatically be detected from the sequence diagram, where iteration conditions are specified. In Figure 6, the *iteration conditions* of both iterative operations in Term 1 are identical: [i:=1..self.title.item->size]. Multiple iterations in a term do not have to share identical iteration conditions and may exhibit more complex relationships. This is the type of analysis that automation needs to support.

3.2.4 Identifying Test Oracles

Now assuming we have defined the operation sequences to be executed and tested, we need to derive test oracles for each tested sequence. It is crucial to address efficiently the oracle problem in order to make automated testing possible. The main source for deriving a test oracle is the post-condition of operations in a sequence, which are defined using OCL.

If we take Sequence 4 in Term 1 as an example, we note that only the two removeTitle operations have a non-trivial post-condition. The removeTitle_{LibrarianTerminal} operation merely delegates to removeTitle_{ritleControl} (see sequence diagram in Figure 6) and they, therefore, have the same post-conditions (but defined using a different context, as expected). From the data dictionary, where all model elements are defined and where preand post-conditions are assumed to be provided, we can extract:

This expression's context is a titleControl object, created to control the execution of the Remove Title use case. This object has, however, disappeared by completion of the use case as the last message triggers it destruction and cannot be used as context object in the test oracle expression¹⁵. Then, the oracle that needs to be checked by the test driver for our example is :

```
Title.allInstances= Title.allInstances@pre-set{title} and Item.allInstances.title->select(isbn = title.isbn)->size=0
```

We therefore need, in general, to transform the postconditions to make them usable as test driver oracles. A general transformation rule is that self should be removed in the

¹⁵ It is typical [9] to instantiate a control object during a use case's initiation and then to dispose of it when its corresponding use case is completed.

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postcondition and allInstances should be used to refer to the instances of the class following self in the navigation expression (Title here). Then select can be used, if necessary, to select the appropriate instances and check the required condition. It is, however, not necessary in the above example as all Title instances are of interest.

In the above oracle expression, just after the select bracket, isbn is not the result of a navigation expression and is a parameter of an operation triggered by the use case on the boundary class LibrarianTerminal:: requestTitleInfo(). Such parameters, defined in what Binder calls *extended* use cases [5], were first introduced in Section 3.1 for the identification of use case sequential dependencies. We will see that they play an important role at a later stage (Section 3.3). We discuss further this issue in Section 4.

The case above is rather simple since, as mentioned above, only two operations have a non-trivial and identical post-condition. In the general case, the conjunction of post-conditions in the sequence of operations has to be used to determine the test oracle. This may lead to complex cases where, for example, one subsequent operation's post-condition clause cancels out a former post-condition clause. This issue will be addressed by future work.

A simpler alternative, that does not require complex OCL expression analyses and transformations but entail more code instrumentation, is to systematically execute assertions that instrument pre/post-conditions and class invariants at the entry/exit of each operation and raise an exception when they are violated. This was recently suggested as a potential solution to the oracle problem in [3] and [7]. In [7], the authors investigate whether instrumented contracts, defined during Analysis, can be used as a substitute to hard-coded test oracles in the test drivers and whether they help with diagnosing failures and locate faults. Based on a case study, results indicate that, in roughly 80 percent of the cases, instrumented contracts are good enough substitutes to hard-coded oracles in test drivers.

3.2.5 Constructing Decision Tables

Once we have, for a given use case, identified the operation sequences to be tested, their initial conditions and oracles, we can formalize all this in a decision table that will be used as a formal set of test requirements, which will be part of the test plan. For

Variants	nts Condition Section				Action Section				
(use case J)						Messages to Actor			State Change
	Α	В	C	D	Е	Ι	II		
jı	Yes	No	No	No	No	No	No	Yes	Yes
j ₂	No	Yes	No	No	No	No	Yes	Yes	No
j ₃	No	No	Yes	No	No	No	Yes	Yes	No
j4	No	No	No	Yes	No	No	Yes	Yes	No
j₅	No	No	No	No	Yes	Yes	No	No	No

RemoveTitle, the corresponding decision table is provided in Table 2. Decision tables for the other use cases of the Library example are provided in Appendices E, F, G.

 Table 2 – Decision Table for RemoveTitle (use case J)

Each row in Table 2 is what is called in testing terminology a *variant* [5]. Test cases should cover all variants, at least once. Due to the fact that a product term (Section 3.2.2) is tested instantiating iteration symbols into several operation sequences (Section 3.2.3), each variant will be covered by several test cases, one for each tested operation sequence. The columns model the *initial conditions* in which test cases must be run, the *actions* that are taken as a result of running the test cases. Namely, this corresponds to *system state changes* and *output messages* being sent to actors. Further details describing the columns of Table 2 are provided below.

Initial Conditions¹⁶:

Α:	<pre>self.titleControl.title ->exists(t:Title t.isbn=isbn) and</pre>
	<pre>self.titleControl.loancopy->select(loancopyStatus=onloan)</pre>
	->size=0 and
	self.titleControl.title.titleReservationCounter=0

B: self.titleControl.title ->exists(t:Title | t.isbn=isbn) and self.titleControl.loancopy->select(loancopyStatus=onloan) ->size>0 and self_titleControl_title_titlePercenterCounter 0

self.titleControl.title.titleReservationCounter>0

C: self.titleControl.title ->exists(t:Title | t.isbn=isbn) and self.titleControl.loancopy->select(loancopyStatus=onloan) ->size>0 and self.titleControl.title.titleReservationCounter=0

 $^{^{16}}$ The context of OCL expressions A-E is the boundary class for the corresponding use case, i.e., LibrarianTerminal.

D: self.titleControl.title ->exists(t:Title | t.isbn=isbn) and self.titleControl.loancopy->select(loancopyStatus=onloan) ->size=0 and self.titleControl.title.titleReservationCounter>0 E: not self.titleControl.title->exists(t:Title | t.isbn=isbn)

Messages to Actor User:

- I: titleNotExist
- II: loanReservationExist
- III: displayTitleInfo.displayItemInfo*

A * associated to a message, like in case III above, indicates that the message may be sent several times. This number of iterations is determined by the operation sequence that is being executed, as discussed in Section 3.2.3.

State Changes:

Title.allInstances= Title.allInstances@pre-set{title} and Item.allInstances.title.select(isbn = title.isbn)->size=0

In this example, there is only one possible state change or no state change at all. But in general, we have to expect that some alternative state changes will be possible.

Based on the example above, we can now summarize the steps of the procedure used to extract a decision table for each use case. Our source of information is an Analysis model described in UML, which is complying with our testability requirements (summarized in Section 4).

- 1. For each use case, model possible operation sequences in a *regular expression* having a *sum-of-product terms* form, where the alphabet are the public operations of the objects involved in the use case sequence diagram.
- 2. For each product term, which models a set of possible operation sequences, determine the *initial conditions* that must be set up by the test driver to be able to execute any of the sequences matching the term.
- 3. Specify precisely the *operation sequences* that match the term to be executed and tested. We use a strategy similar to loop testing but in a different context.
- 4. Identify *test oracles* by making use of the operation *post-conditions* specified in the Analysis model (data dictionary).

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5. Formalize all the information above into *decision tables* that follow the format proposed above, which is similar to what is described in [5].

3.3 Generating Variant Sequences

If we assume that each use case has a decision table such as the one presented above, we need to go further and devise a sequence of operations to be tested over an entire *use case sequence* (as defined in Section 3.1). In other words, we need to go from use case sequences to use case *variant* sequences, using use case *decision tables*. Assuming we would have a use case sequence of three use cases A.B.C, having respectively a number of variants |A|, |B|, and |C|, the maximum number of variant sequences would then be |A| * |B| * |C|. As described in Section 3.2.5, one variant corresponds to a possible path realization condition for one of the product terms in the interaction diagram regular expression. A variant may require several test cases, as iteration symbols may be present in the corresponding product term, which therefore requires several operation sequences to be tested. More specifically, up to 4 test cases (number of iterations sets to 0, 1, an intermediary number, and a maximum M) may be needed if we use the sequence test strategy presented in Section 3.2.3. Note that, at the beginning of a use case variant sequence, the system is in its initial state.

An issue to be noted is that the test scale specified by the tester (Section 3.1.1) determines what use case variant sequences are possible. The scale of testing must then be chosen carefully if the tester wants to consider all the possible use case variants sequences in the decision tables. To illustrate this, let us take the following simplistic example: In the Library system testing, assume the tester only wants one title and one item for this title (no user or loan, ...). In this situation, the only possible use case sequence to be tested (following what is described in Section 3.1) is: AddTitle(t).AddItem(i). RemoveItem(i).RemoveTitle(t). Since we do not have any loan for the item or reservation for the title, variants 2, 3, and 4 for use case RemoveTitle are not possible (see Table 2). In addition, variant 5 (removing a title that does not exist) for use case RemoveTitle(t) is also impossible because title t is created in the sequence (the parameter of RemoveTitle is the one of AddTitle). Therefore, RemoveTitle variant 1 is the only possibility. For similar reasons, RemoveItem variant 1 is the only possible variant. Then, the only possible use case variant sequence is $AddTitle_1.AddItem_1.RemoveItem_1.RemoveTitle_1$. This variant sequence is the case where a title is added, one corresponding item is added, and then the item and title are subsequently removed. This corresponds to the first (nominal) variant in each of the decision tables in Appendices E, F, G and Table 2.

In practice another issue may arise. Some variant sequences may turn out to be impossible as some of the variants are not *compatible*. A variant b_i of B is incompatible with a variant a_j of A if the state of the system after the execution of a_j is contradicting (a part of) the initial condition of b_i . This is an issue that needs to be addressed as the detection of impossible variant sequences need to be supported to help generate clean, concise test requirements.

4 TESTABILITY

Since the application of the UML notation is not constrained by any particular, precise development method, one can find a great variability in terms of the content and form of UML artifacts, whether at the analysis or design stages. However, the way UML is used determines the *testability* of the UML artifacts. That is, in our context, the ease with which they can be used to support testing activities and the derivation of test artifacts (test requirements, cases, oracles, drivers). Moreover, since automation is a crucial consideration here, our methodology and its associated algorithms have precise requirements regarding the information to be contained in UML artifacts. Thus, in the previous sections, we made a number of assumptions regarding the way a UML analysis model is to be developed. Those assumptions were carefully thought out and are referred to as *testability requirements*. We discuss and justify them in this section, using the metamodel in Figure 7, and explain how they can be automatically verified in the next Section (Section 5).

The very first of those testability requirements concerns the sequential constraints between use cases, in addition to the other dependencies shown in the use case diagram (class UCSequentialDependencies class in Figure 7). We decided to build one activity diagram per actor in the system to model such dependencies (see Section 3.1 and Figure

2). These activity diagrams capture the sequential dependencies between the use cases related to the actors.



Figure 7 – Meta-model describing Analysis testability requirements for TOTEM

Then each use case is described using an interaction diagram, which in UML is either an interaction diagram or a collaboration diagram. We assume that these diagrams use OCL for the description of the alternative object interactions (guard conditions), and extended the UML numbering rules for messages in interaction diagrams (see Section 3.2), thus making them unambiguous (see Figure 6). In addition, we are defining and using extended use cases (as described in [5]) that specify, among other things, information about the parameters that determine the behavior to be exhibited. For example, we show in Section 3.2.2 that isbn is a formal parameter for the Remove Title use case. We further show that the values of these parameters need to be carefully chosen to execute some of the variant sequences (Section 3.3).

Finally, the data dictionary is assumed to provide – in addition to an informal description of classes, attributes, and operations – the contracts (pre- and post-conditions for the operations) and class invariants in OCL. For example, we presented such a post-condition in Section 3.2.4, for method removeTitle in class TitleControl.

Testability requirements are a trade-off between better testability and the effort overhead they entail during Analysis and Design. We believe that having a description of the business model supported by the system (the activity diagram capturing sequential constraints between use cases), as well as precise definitions for operations and classes (contracts), is not only relevant for testing but also a sound practice for a precise and rigorous Analysis¹⁷. A similar argument can be made for precise OCL guard conditions in the sequence diagrams describing each use case. Furthermore, [5] indicates that guard conditions should be expressed in an executable syntax and, in the context of the UML, OCL is a natural choice. Overall, our testability requirements seem realistic and justified, though their costs and benefits during analysis are to be investigated further through case studies.

Our view on testability is related to functional and behavioral models. In other words, how easily can we derive complete test artifacts from UML diagrams? There exist other, complementary testability definitions that are more related to source code and structural models. Built-in test support (e.g., set and get methods for attributes) can improve two important components of testability: observability (retrieving the state of the system) and controllability (setting the system in a particular state) [5]. From a completely different perspective, [1] assesses testability by quantifying the effort required for different unit test strategies based on measures of control flow graphs.

5 AUTOMATION

The purpose of this section is to describe what should be the internal structure of a tool to support our testing methodology, both in terms of packages and, when relevant, at the class level. This led us to the development of a prototype tool that implements the core architecture needed by the TOTEM strategy. Another benefit of this modeling exercise is that we recap, in a structured manner, how all the concepts, representations, and algorithms introduced earlier relate to each other.

Automation of the different steps of the TOTEM strategy requires that information provided by UML diagrams is available, in full conformance to our testability requirements. The meta-model in Figure 7 is therefore one of the core packages

¹⁷ This view is supported by a number of articles and books (two examples are [9, 14]).

(RequirementsMetamodel) of the TOTEM tool (see Figure 8), which serves as a repository of UML diagrams' information. The other packages in Figure 8 concern the automatic construction of system test requirements (SystemTesting, which classes are described in Figure 9), and parsing UML and OCL information.

Since these diagrams are built using UML case tools, a first solution is to use the API provided by these tools to access UML diagrams' information. An alternative relies on an XMI representation of the diagrams, which are exported by an increasing number of case tools, and for which parsers already exist. This second solution has the advantage of not depending on a particular case tool, as long as the tool is able to produce XMI files.



Figure 8 – Packages of the TOTEM System Testing tool

RequirementsMetaModel depends on OCLparser as it needs to verify the correctness of OCL expressions. Depending on our test oracle strategy (Section 3.2.4), SystemTesting may need to manipulate OCL expressions to compare or transform them.

Testability requirements can be automatically verified in order to make sure UML Analysis models are compliant before performing any further analysis for testing purposes:

- An activity diagram describing sequential dependencies between use cases must be available for each actor;
- Each use case must be described by an interaction diagram;

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- Interaction diagrams must make use of adequate numbering conventions for messages;
- Guard conditions for messages in interaction diagrams as well as class invariants, pre- and post-conditions must use the OCL.

Then, once the UML models have been shown to be compliant with testability requirements, the different activities described in Section 3 can be automated:

- Given an activity diagram, producing use case sequences to be tested as described in Section 3.1 needs to be automated. We provide algorithms for the most complex parts of this process (Appendix H). In Figure 9, class SystemTestingRequirements initializes (1) the composition allParamUCSeq (all the parameterized use case sequences) with class ParamUCSeq (parameterized use case sequence) from the activity diagram, (2) the composition allOriginalInstUCSeq (all the original instantiated use case sequences) with class InstUCSeq (instantiated use case sequence) from the test scale information, and then (3) the composition completeUCSeq (the complete set of use case sequences to be tested) with InstUCSeq;
- The generation of use case scenarios from interaction diagrams is formalized, for each use case, as a decision table and modeled in the SystemTesting package (Figure 9):
 - Regular expressions describing interactions diagrams as method sequences, each unique sequence describing a use case scenario.
 - Path realization condition and operation sequences for the product terms in the regular expressions (i.e., the decision table variants).
 - Test oracles for operation sequences. As discussed in Section 3.2.4, this requires complex manipulations of OCL expressions, i.e., pre- and post-conditions of operations in sequences. For example, we need to be able to determine whether two OCL expressions contradict or subsume each other. All this is not required though if we decide to use instrumented contracts, as discussed above.

- The next step is to produce variant sequences (Section 3.3) using both use case sequences and scenario decision tables. One important automation issue is the detection of incompatible variants across decision tables.



Figure 9 – Classes in the SystemTesting package

6 CONCLUSION AND FUTURE WORK

This paper has presented the TOTEM (Testing Object-orienTed systEms with the unified Modeling language) functional system test methodology. We derive test requirements from early artifacts produced at the end of the analysis development stage, namely use case diagram, use case description, interaction diagram (sequence or collaboration) associated with each use case, and class diagram (composed of application domain classes and their contracts). This early use of analysis artifacts is very important as it helps devising a system test plan, size the system test task, and plan appropriate resources early in the life cycle. Once the low level design is complete, when detailed information is available regarding both application domain and solution domain classes, then test requirements can be used to derive test cases, test oracles, and test drivers.

We emphasized here the fundamental principles of our methodology, which is based in part on published material [4, 5, 11]. We first showed how activity diagrams can be used to capture sequential dependencies between use cases and allow the specification of use case sequences to be tested. For each use case involved in a particular sequence, the key issues regarding the selection of use case scenarios to undergo testing were then addressed, i.e., what paths to cover in the corresponding sequence diagrams. The derivation of key information for determining the initial system conditions for testing scenarios and their corresponding test oracles was also addressed. Our methodological decisions were justified in terms of their potential for automation and their implications in terms of testability.

The TOTEM testing methodology can be easily embedded into incremental development methods such as the Rational Unified Process (RUP) [13]:

- It only requires analysis artifacts to devise an early but precise test plan. Design information is only needed later on to help with the generation of test cases and harness. Our testability requirements for Analysis artifacts can be fulfilled in the context of the RUP.
- Our methodology focuses on test automation, a feature that is of extreme importance in the context of incremental development such as in the RUP.

Ongoing and future work include:

- How these test requirements (derived from use case dependencies and from sequence diagrams) are used together with test requirements derived the system class diagram (choosing specific object configurations the classes involved in the scenarios) in order to produce *complete* test requirements for system testing.
- How system test requirements are used at a later stage to produce test cases, oracles, and drivers. This is similar to the path-sensitization problem (i.e., deriving input values to execute selected paths), which is known to be undecidable in the general case [4]. Similarly to [20], we will investigate the use of meta-heuristics, such as genetic algorithms, to automatically generate test data from test requirements.
- Go into more depth regarding automation and all the core algorithms that it entails. This is important since a testing methodology without effective tool support is not likely to be adopted. We have provided (1) some of the algorithms for the construction of sequences of use cases to be tested and (2) a precise procedure for the construction of use case scenarios such that the definition of the

corresponding algorithms should be straightforward. In general, our automation strategy is based on a systematic use of OCL for contracts and guard conditions.

- The last point above leads us to the issue of testability. We have defined clear testability requirements and justified why they were a good trade-off. We still need to provide effective automation to help people achieve good testability (i.e., consistency and completeness checks).
- Last but not least, our methodology needs to be carefully experimented with, within control settings and through industrial case studies. In particular, the cost of our testability requirements (e.g., the definition of extended use cases) will have to be evaluated.
- How non-functional aspects of system testing, such as performance testing, can be integrated in the TOTEM approach.

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APPENDIX A: USE CASE DIAGRAM FOR THE LIBRARY SYSTEM



Figure 10 Use case diagram for the Library System

APPENDIX B: USE CASES DECRIPTIONS

In this appendix, we give the textual description (following what is suggested in [8]) of the use cases used in the paper, that is the twelve use cases that appear in the activity diagram in Figure 2. Note that we have added a section, named Parameters, that indicates the formal parameters of the use case: formal parameters are described by their name, type and kind (in, out or in/out).

Add Item

Use case name: Add Item Participating actor: Librarian Parameters: in Isbn: Integer, out ItemID: Integer Entry condition:

1. The *librarian* requests the *title* information from the *librarianterminal*. The Find Title use case is used. If the *title* doesn't exist, the system will ask the *librarian* to add the *title*, the Add Title use case is used.

Flow of events:

2. The *title* information is displayed on the *librarianterminal*.

Exit condition:

3. The *librarian* adds *item*, an itemId is generated for it.

Add User

Use case name: Add User

Participating actor: Librarian

Parameters: in UserID: Integer

Entry condition:

1. The *librarian* requests to add *user* from the *librarianterminal*.

Flow of events:

2. The *librarian* inputs the user information to the system. If the user information has already been recorded in the system, the *librarian* will not be allowed to add the *user*.

Exit condition:

3. The user information has been stored in the system, a userId is generated for it or the *librarian* is not allowed to add the *user*.

Add Title

Use case name: Add Title

Participating actor: Librarian

Parameters: in Isbn: Integer

Entry condition:

- 1. The *librarian* requests to add *title* from the *librarianterminal*.
- Flow of events:
- 2. The *librarian* inputs the title information such as isbn to the system. If any information requested is missing or the same with other *title*, the system will prompt an error message and go to the the beginning of this step; if the *title*'s information is same with other *title*, the *librarian* will not be allowed to add the *title* and go to 3.

Exit condition:

3. A new *title* has been added to the system or the *librarian* is not allowed to add the *title*.

Borrow Loancopy

Use case name: Borrow Loancopy

Participating actor: Librarian

Parameters: in UserID: Integer, in ItemID: Integer

Entry condition:

1. The *librarian* requests the *user* information from the *librarianterminal*. The Find User use case is used. If the *user* doesn't exist, then proceeds to 5.

Flow of events:

- 2. The *librarian* requests the *title* information. The Find Title use case is used. If the title doesn't exists, then proceeds to 5.
- 3. The *librarian* requests add *loan*. The system judges if the *user* is able to borrow book. If the *user's* privilege is revoked, the system will prompt a corresponding message. The *librarian* can collect the fine. The Collect Fine use case is used. If the user's fine is not cleared, proceeds to 5. If the *item* is a *referencecopy*, or, the *user* already has 10 *loans*, then the *user* is not allowed to borrow *loancopy* and proceeds to 5. The system also checks the book reservation. The Check Reservation use case is used. If the system denies the borrow request, then proceeds to 5.
- 4. The *library* lends the *loancopy* to the *user*. If the user has reached loan limit, the system updates the user's loan privilege. If the *user* has a *reservation* on that *title*, the *reservation* is removed. The Remove Reservation use case is used.

Exit conditions:

5. The system denies the borrow request or a new *loan* is registered, a loanId is generated for the *loan*.

Collect Fine

Use case name: Collect Fine

Participating actor: Librarian

Parameters: in UserID: Integer, in ItemID: Integer

Entry condition:

- 1. The *librarian* requests the *user* information from the *librarianterminal*. The Find User use case is used. If the *user* doesn't exist, then proceeds to 3.
- 2. The *librarian* enters the fine collected, the system updates the *user's* fine information. If the *user's* privilege is revoked, then system updates the *user's* privilege.

Exit condition:

3. The *user's* fine is cleared or the *librarian* is unable to collect the *user's* fine.

Monitor System

Use case name: Monitor System

Participating actor: Librarian

Parameters:

Entry condition:

1. The *librarian* requests to monitor the system from the *librarianterminal*.

Flow of events:

2. All the book *titles* and the *users* of the library are displayed on the *librarianterminal*.

Exit condition:

3. The *librarian* completes monitoring the system.

Remove Item

Use case name: Remove Item

Participating actor: Librarian

Parameters: in ItemID: Integer

Entry condition:

1. The *librarian* requests the *title* information from the *librarianterminal*. The Find Title use case is used. If the *title* doesn't exist, then proceeds to 4.

Flow of events:

- 2. The *title* information is displayed on the *librarianterminal*.
- 3. The *librarian* specifies the *item* should be removed. If the *item* is loaned, the *librarian* is not allowed to remove the *item*.

Exit condition:

4. The specified *item* has been removed or the *librarian* is not allowed to remove the *item*.

Remove Title

Use case name: Remove Title

Participating actor: Librarian

Parameters: in Isbn: Integer

Entry condition:

1. The *librarian* requests the *title* information from the *librarianterminal*. The Find Title use case is used. If the title doesn't exist, then proceeds to 3.

Flow of events:

2. The title information is displayed on the *librarianterminal*. If the *title* is reserved or some of the title's *loancopies* are loaned, the *librarian* is not allowed to remove the *title*.

Exit condition:

3. The *title* has been removed, along with all the *items* associated with the *title* or the *librarian* is not allowed to remove the *title*.

Remove User

Use case name: Remove User

Participating actor: Librarian

Parameters: in UserID: Integer

Entry condition:

1. The *librarian* requests the *user* information from the *librarianterminal*. The Find User use case is used. If the user doesn't exist or the user's privilege is revoked, proceeds to 3.

Flow of events:

2. The user information is displayed on the *librarianterminal*. If the *user* has *loan*, the *librarian* is not allowed to remove the *user*.

Exit condition:

3. The *user* has been removed along with his/her reservation if any or the *librarian* is not allowed to remove the *user*.

Renew Loan

Use Case Name: Renew Loan

Participating actor: Librarian

Parameters: in UserID: Integer, in ItemID: Integer

Entry condition:

1. The *librarian* requests the *loan* information from the *librarianterminal*. The Find Loan use case is used. If the loan doesn't exist, or the loan owner's privilege is revoked, proceeds to 5.

Flow of events:

- 2. The *loan* information is displayed on the *librarianterminal*.
- 3. The *librarian* requests renew *loan*. If the *user's* privilege is revoked, the system will prompt a corresponding message. The *librarian* can collect the fine. If the *user's* fine is not cleared, then proceeds to 5. The system checks whether the *title* is reserved. The Check Reservation use case is used. If the *title* is reserved, the *librarian* is not allowed to renew the *loan* and proceeds to 5.
- 4. The system identifies the *loan* of the *loancopy*. If the *loan* is overdue, the system prompts loan status information. The system checks the times of the renewing the *loan*, if the *loan* has been renewed 2 times, the *librarian* is not allowed to renew the *loan*.

Exit condition:

5. The corresponding *loan* is renewed, a new dueDate is generated for the *loan* or the *librarian* is not allowed to renew the *loan*.

Return Loancopy

Use case name: Return Loancopy Participating actor: Librarian Parameters: in UserID: Integer, in ItemID: Integer

Entry condition:

1. The Librarian requests the *loan* information from the *librarianterminal*. The Find Loan use case is used. If the *loan* doesn't exist, then proceeds to 4.

Flow of events:

- 2. The *loan* information is displayed on the *librarianterminal*.
- 3. The *librarian* requests remove *loan*. The system checks whether the *loan* is overdue. If the *loan* is overdue, the system prompts the corresponding message to notify the *librarian* and the fine information will be recorded. If the loan has been overdue for more than 3 days, the loan owner's privilege will be revoked. Only after the user's fine is cleared, can the user's privilege be retained.

Exit condition:

4. The corresponding *loan* is destroyed or the request is denied.

APPENDIX C: CLASS DIAGRAMS



Figure 11 - Class Diagram (first view): links between boundary and control classes.



Figure 12 – Class Diagram (second view): links between control and entity classes.



Figure 13 – Class Diagram (third view): links between entity classes.

APPENDIX D: OTHER USE CASE SEQUENCE DIAGRAMS (ADD ITEM, ADD TITLE, REMOVE ITEM)



Figure 14 – Add Item sequence diagram



Figure 15 – Add Title sequence diagram



Figure 16 – Remove Item sequence diagram

APPENDIX E: DECISION TABLES FOR USE CASE ADD ITEM

Regular expression:

$$\begin{split} & \text{requestTitleInfo}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{TitleControl}}.\texttt{requestTitleInfo}_{\texttt{TitleControl}}.\\ & (\texttt{getItem}_{\texttt{Title}}.\texttt{displayTitleInfo}_{\texttt{LibrarianTerminal}}.\texttt{displayTitleInfo}_{\texttt{User}}.\\ & \texttt{displayItemInfo}_{\texttt{user}}+\texttt{titleNotExist}_{\texttt{LibrarianTerminal}}.\texttt{titleNotExist}_{\texttt{User}}\\ & \texttt{requestAddTitle}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{TitleControl}}.\texttt{requestAddTitle}_{\texttt{TitleControl}}.\\ & \texttt{create}_{\texttt{Title}}.\texttt{TitleAdded}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{User}}).\\ & \texttt{addItem}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{ItemControl}}.\texttt{addItem}_{\texttt{ItemControl}}.\texttt{create}_{\texttt{Item}}.\\ & \texttt{displayItemId}_{\texttt{LibrarianTerminal}}.\texttt{displayItemId}_{\texttt{User}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\\ & \texttt{destroy}_{\texttt{ItemControl}}.\texttt{destroy}_{\texttt{TitleControl}}.\\ \end{split}$$

Regular expression in sum-of-products form:

```
requestTitleInfo_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.
getItem_Title.displayTitleInfo_LibrarianTerminal.displayTitleInfo_User.
displayItemInfo_User .addItem_LibrarianTerminal.create_TtemControl.addItem_TtemControl.
create_Ttem.displayItemId_LibrarianTerminal.displayItemId_User.exit_LibrarianTerminal.
destroy_TtemControl.destroy_TitleControl
+
requestTitleInfo_LibrarianTerminal.create_TitleControl.requestTitleInfo_TitleControl.
titleNotExist_LibrarianTerminal.create_TitleControl.requestAddTitle_TitleControl.
create_Title.titleAdded_LibrarianTerminal.titleAdded_User.addItem_LibrarianTerminal.
destroy_TitleControl.addItem_Terminal.create_TitleControl.requestAddTitle_TitleControl.
titleNotExist_LibrarianTerminal.create_TitleControl.requestAddTitle_TitleControl.
create_Title.titleAdded_LibrarianTerminal.titleAdded_User.addItem_LibrarianTerminal.
create_Title.addItem_Terminal.create_TitleControl.destroy_TitleControl.
```

Test Requirements for Interaction Diagrams

Initial conditions:

```
Term1: self.titleControl.title->exists(t:Title|t.isbn=isbn)
Term2: not self.titleControl.title->exists(t:Title|t.isbn=isbn)
```

Scenario Sequences:

```
Product term 1 sequence:
```

```
requestTitleInfo<sub>LibrarianTerminal</sub>.create<sub>TitleControl</sub>.
requestTitleInfo<sub>TitleControl</sub>.getItem<sub>Title</sub>.displayTitleInfo<sub>LibrarianTerminal</sub>.
displayTitleInfo<sub>User</sub>.displayItemInfo<sub>User</sub>*.addItem<sub>LibrarianTerminal</sub>.
create<sub>ItemControl</sub>.addItem<sub>ItemControl</sub>.create<sub>Item</sub>.displayItemId<sub>LibrarianTerminal</sub>.
displayItemId<sub>User</sub>.exit<sub>LibrarianTerminal</sub>.destroy<sub>ItemControl</sub>.destroy<sub>TitleControl</sub>
```

Product term 2 sequence:

```
\label{eq:constraint} \begin{split} & \text{requestTitleInfo}_{\text{LibrarianTerminal}}. \text{create}_{\text{TitleControl}}, \\ & \text{requestTitleInfo}_{\text{TitleControl}}. \text{titleNotExist}_{\text{LibrarianTerminal}}. \\ & \text{titleNotExist}_{\text{User}}, \text{requestAddTitle}_{\text{LibrarianTerminal}}. \\ & \text{create}_{\text{TitleControl}}. \text{create}_{\text{Title}}. \\ & \text{titleAdded}_{\text{User}}). \\ & \text{addItem}_{\text{LibrarianTerminal}}. \\ & \text{create}_{\text{ItemControl}}. \\ & \text{displayItemId}_{\text{LibrarianTerminal}}. \\ & \text{displayItemId}_{\text{User}}. \\ & \text{exit}_{\text{LibrarianTerminal}}. \\ & \text{destroy}_{\text{TitleControl}}. \\ \end{split}
```

Oracles for test sequences

```
Title.allInstances->select(isbn=title.isbn).item->size =
Title.allInstances->select(isbn=title.isbn).
item->size@pre+1
```

Decision Table

Variants	Condition Section	Action Section					
(use case G)		Messa	State				
	А	Ι	II	III	IV	Change	
g1	Yes	No	Yes	No	Yes	Yes	
g ₂	No	Yes	No	Yes	Yes	Yes	

Initial Conditions: Context of OCL expressions is LibrarianTerminal

A: self.titleControl.title->exists(t:Title|t.isbn=isbn)

Message to Actor User:

I: titleNotExist
II: displayTitleInfo.displayItemInfo*
III: titleAdded

IV: displayItemId

State Change:

Title.allInstances->select(isbn=title.isbn).item->size =Title.allInstances->select(isbn=title.isbn). item->size@pre+1

APPENDIX F: DECISION TABLES FOR USE CASE ADD TITLE

Regular expression:

```
\label{eq:control} \begin{split} \text{requestAddTitle}_{\text{LibrarianTerminal}}.\text{create}_{\text{TitleControl}}.\text{requestAddTitle}_{\text{TitleControl}}.\\ (\text{create}_{\text{Title}}.\text{TitleAdded}_{\text{LibrarianTerminal}}.\text{titleAdded}_{\text{User}}+\text{titleExist}_{\text{LibrarianTerminal}}. \end{split}
\texttt{titleExist}_{\texttt{User}}).\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{destroy}_{\texttt{TitleControl}}
```

Regular expression in sum-of-products form:

```
\texttt{requestAddTitle}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{TitleControl}}.\texttt{requestAddTitle}_{\texttt{TitleControl}}.\texttt{create}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{exit}_{\texttt{LibrarianTerminal}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdded}_{\texttt{user}}.\texttt{titleAdde
  destroy_TitleControl
  +
\begin{array}{l} \texttt{requestAddTitle}_{\texttt{LibrarianTerminal}}.\texttt{create}_{\texttt{TitleControl}}.\texttt{requestAddTitle}_{\texttt{TitleControl}}.\texttt{titleExist}_{\texttt{LibrarianTerminal}}.\texttt{destroy}_{\texttt{TitleControl}}.\texttt{} \end{array}
```

Test Requirements for Interaction Diagrams

Initial conditions:

```
Term1: not self.titleControl.title->exists(t:Title|t.isbn=isbn)
Term2: self.titleControl.title->exists(t:Title|t.isbn=isbn)
```

Scenario Sequences:

Product term 1 sequence:

```
\label{eq:create} requestAddTitle_{\tt LibrarianTerminal}.create_{\tt TitleControl}.requestAddTitle_{\tt TitleControl}.create_{\tt Title}.TitleAdded_{\tt LibrarianTerminal}.titleAdded_{\tt User}.exit_{\tt LibrarianTerminal}.
destroy
```

Product term 2 sequence:

```
\label{eq:control} request Add \end{title}_{\tt LibrarianTerminal}. \end{title}_{\tt TitleControl}. \end{title} request \end{title}_{\tt LibrarianTerminal}. \end{title} \end{title}_{\tt LibrarianTerminal}. \end{title} \end{title} \end{title}_{\tt LibrarianTerminal}. \end{title} \end{title} \end{title} \end{title}_{\tt LibrarianTerminal}. \end{title} \end{title}
```

Oracles for test sequences

```
Title.allInstances->size=Title.allInstances->size@pre+1
```

Decision Table

Variants (use case I)	Condition Section	Action Section				
		Messages to A	State			
	А	Ι	II	Change		
i ₁	Yes	No	Yes	Yes		
i ₂	No	Yes	No	No		

Initial Conditions: Context of OCL Expressions is LibrarianTerminal

A: not self.titleControl.title->exists(t:Title|t.isbn=isbn)

Message to Actor Librarian:

- I: titleExist
- II: titleAdded

State Change:

title.allinstances->size=title.allinstances->size@pre+1

APPENDIX G: DECISION TABLES FOR USE CASE REMOVE ITEM

Regular expression:

```
\label{eq:constraint} \begin{split} requestTitleInfo_{\texttt{LibrarianTerminal}}.create_{\texttt{TitleControl}}.requestTitleInfo_{\texttt{TitleControl}}.\\ (getItem_{\texttt{Title}}.displayTitleInfo_{\texttt{LibrarianTerminal}}.displayTitleInfo_{\texttt{User}}.\\ displayItemInfo_{\texttt{User}}^*.removeItem_{\texttt{LibrarianTerminal}}.create_{\texttt{ItemControl}}.\\ removeItem_{\texttt{ItemControl}}.(destroy_{\texttt{Item}}+\texttt{loanORreservationExist}_{\texttt{LibrarianTerminal}})+\\ titleNotExist_{\texttt{LibrarianTerminal}}.titleNotExist_{\texttt{User}}).exit_{\texttt{LibrarianTerminal}}.destroy_{\texttt{TitleControl}}.\\ destroy_{\texttt{ItemControl}}.\\ \end{split}
```

Regular expression in sum-of-products form:

```
requestTitleInfo_LibrarianTerminal .create_TitleControl .requestTitleInfo_TitleControl .
getItem_Title .displayTitleInfo_LibrarianTerminal .displayTitleInfo_User .
displayItemInfo_User .removeItem_LibrarianTerminal .create_ItemControl .
removeItem_TtemControl .destroy_Item .exit_LibrarianTerminal .destroy_TitleControl .
destroy_ItemControl .
+
requestTitleInfo_LibrarianTerminal .create_TitleControl .requestTitleInfo_TitleControl .
getItem_Title .displayTitleInfo_LibrarianTerminal .displayTitleInfo_User .
displayItemInfo_User .removeItem_LibrarianTerminal .create_ItemControl .
destroy_TitleControl .loanORreservationExist_LibrarianTerminal .exit_LibrarianTerminal .
destroy_TitleControl .loanORreservationExist_LibrarianTerminal .exit_LibrarianTerminal .
destroy_TitleInfo_LibrarianTerminal .create_ItemControl .
destroy_TitleControl .destroy_ItemControl .
+
requestTitleInfo_LibrarianTerminal .create_ItemControl .cequestTitleInfo_TitleControl .
destroy_TitleControl .destroy_ItemControl .
destroy_TitleControl .destroy_ItemControl .requestTitleInfo_TitleControl .
destroy_TitleControl .destroy_ItemControl .create_ItemControl .requestTitleInfo_TitleControl .
destroy_TitleControl .destroy_ItemControl .create_ItemControl .cexit_LibrarianTerminal .destroy_TitleControl .destroy_ItemControl .destroy_ItemControl .cexit_LibrarianTerminal .destroy_TitleControl .destroy_ItemControl .destroy_ItemControl .cexit_LibrarianTerminal .destroy_TitleControl .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .cexit_LibrarianTerminal .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .cexit_LibrarianTerminal .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .cexit_LibrarianTerminal .destroy_ItemControl .destroy_ItemControl .destroy_ItemControl .cexit .
```

Test Requirements for Interaction Diagrams

Initial conditions:

```
Term1: self.titleControl.title->exists(t:Title|t.isbn=isbn) and
Not self.itemControl.loancopy->select
(itemId=loancopy.itemId).loancopyStauts=onloan
Term2: self.titleControl.title->exists(t:Title|t.isbn=isbn) and
self.itemControl.loancopy->select
```

(itemId=loancopy.itemId).loancopyStauts=onloan

*Term3: n*ot self.titleControl.title->exists (t:Title|t.isbn=isbn)

Scenario Sequences:

```
Product term 1 sequence:
```

```
requestTitleInfo<sub>LibrarianTerminal</sub>.create<sub>TitleControl</sub>.
requestTitleInfo<sub>TitleControl</sub>.getItem<sub>Title</sub>.displayTitleInfo<sub>LibrarianTerminal</sub>.
displayTitleInfo<sub>User</sub>.displayItemInfo<sub>User</sub>.removeItem<sub>LibrarianTerminal</sub>.
create<sub>ItemControl</sub>.removeItem<sub>ItemControl</sub>.destroy<sub>Item</sub>.exit<sub>LibrarianTerminal</sub>.
destroy<sub>TitleControl</sub>.destroy<sub>ItemControl</sub>
```

Product term 2 sequence:

```
requestTitleInfo<sub>LibrarianTerminal</sub>.create<sub>TitleControl</sub>.
requestTitleInfo<sub>TitleControl</sub>.getItem<sub>Title</sub>.displayTitleInfo<sub>LibrarianTerminal</sub>.
displayTitleInfo<sub>User</sub>.displayItemInfo<sub>User</sub>.removeItem<sub>LibrarianTerminal</sub>.
create<sub>ItemControl</sub>.removeItem<sub>ItemControl</sub>.loanORreservationExist<sub>LibrarianTerminal</sub>.
.exit<sub>LibrarianTerminal</sub>.destroy<sub>TitleControl</sub>.destroy<sub>ItemControl</sub>
```

```
Product term 3 sequence:
    requestTitleInfo_LibrarianTerminal.create_TitleControl.
    requestTitleInfo_TitleControl.titleNotExist_LibrarianTerminal.
    titleNotExist_User.exit_LibrarianTerminal.destroy_TitleControl.destroy_ItemControl
```

Oracles for test sequences

```
Title.allInstances->select(isbn=title.isbn).item
= Title.allInstances->select(isbn=title.isbn).item@pre-
set{item}
```

Decision Table

Variants	Condition Section			Action Section			
(use case H)				Messages to Actor			State
	А	В	С	Ι	II	III	Change
h ₁	Yes	No	No	No	Yes	No	Yes
h ₂	No	Yes	No	No	Yes	Yes	No
h ₃	No	No	Yes	Yes	No	No	No

Initial Conditions: Context of OCL Expressions is LibrarianTerminal

```
A: self.titleControl.title->exists(t:Title|t.isbn=isbn)
    and
    not self.itemControl.loancopy->select
```

(itemId=loancopy.itemId).loancopyStatus =onloan

- B: self.titleControl.title->exists(t:Title|t.isbn=isbn)
 and
 self.itemControl.loancopy->select
 (itemId=loancopy.itemId).loancopyStatus = onloan
- C: not self.titleControl.title->exists(t:Title|t.isbn=isbn)

Message to Actor Librarian:

- I: titleNotExist
- $II: \ \texttt{displayTitleInfo.displayItemInfo*}$
- III: loanORreservationExist

State Changes:

Title.allInstances->select(isbn=title.isbn).item

= Title.allInstances->select(isbn=title.isbn).item@pre-set{item}

APPENDIX H: ALGORITHMS

In this appendix, we describe several methods and provide some algorithms for the production of complete use case sequences to be tested from the activity diagram describing use case sequential dependencies and test scale information. More specifically, we focus on the combination of instantiated use case sequences. We remind Figure 9 in Figure 17 because algorithms make use of classes and relationships this figure specifies.



Figure 17 - Classes in the systemTestingRequirements package

Remember that (from Figure 17) class SystemTestingRequirements initializes:

- Composition allParamUCSeq (all the parameterized use case sequences) with class ParamUCSeq (parameterized use case sequence) from the activity diagram;
- Composition allOriginalInstUCSeq (all the original instantiated use case sequences) with class InstUCSeq (instantiated use case sequence) from the test scale information;

- Composition completeUCSeq (the complete use case sequences to be tested). This is done by method MergeInstUCSeq (described below¹⁸).

Method MergeInstUCSeq is a method of class SystemTestingRequirements. This method uses the original sequence of instantiated use case sequences (composition alloriginalInstUCSeq in Figure 17), and merges them taking into account their possible common elements. Each time two sequences are interleaved, only a given percentage of all the possible interleavings is produced (parameter num). This method uses method GenerateInterleavings described below. The result is a set of complete use case sequences (composition completeUCSeq in Figure 17).

```
Procedure MergeInstUCSeq(int percentage)
```

```
begin
 // current is the current sequence of instantiated use case sequences
 // with which one of the original sequence is merged, producing the
 // next sequence of instantiated use case sequences.
 SequenceOfInstUCSeq current = null, next = null;
 // i (resp. j) is used to go through the original (resp. the current)
 // sequence.
 int i, j;
 // must remove the redundant sequences TBD
 if (allOriginalInstUCSeq->size = 0) then
 begin
  return null;
 end
 if (allOriginalInstUCSeq->size = 1) then
 begin
   return allOriginalInstUCSeq.at(1);
 end
 // We merge the two first original sequences and produce the first
 // value for variable current.
 current = GenerateInterleavings(allOriginalInstUCSeq.at(1),
 allOriginalInstUCSeq.at(2), percentage);
 // We then merge each of the remaining original sequence one by one.
 for (i = 3; i <= allOriginalInstUCSeq->size; i++) do
 begin
  // We merge original sequence I to all the sequences in current.
```

```
for (j = 1; j <= current->size; j++) do
```

¹⁸ Note that three methods of class SystemTestingRequirements are described, though only one is shown in Figure 17 because of the size of their signature.

```
begin
    next.append( GenerateInterleavings(current.at(j),
    allOriginalInstUCSeq.at(i), percentage));
end
    // next become the new current sequence.
    current = next;
    next = null;
end
this->completeUCSeq = current;
end // of procedure MergeInstUCSeq
```

Private method GenerateInterleavings of class SystemTestingRequirements generates a given percentage (parameter percentage) of all the possible interleavings of two instantiated use case sequences (parameters S1 and S2). It first calls then produces the interleavings (given IdentifyCommonElements(S1, S2). all in the PISubSequences (information returned percentage) by IndentifyCommonElements), and merges all these interleavings with the common elements. It returns a sequence of all the interleavings produced.

```
Function GenerateInterleavings(InstUCSeq S1, InstUCSeq S2, int
percentage): SequenceOfInstrUCSeq
```

Private method IdentifyCommonElements of class SystemTestingRequirements identifies the common elements between two instantiated use case sequences (parameters S1 and S2) that must be merged. It identifies the common elements as well as the sub sequences, between the common elements, that differ. This method returns a sequence of object of class PISubSequences. In each of these objects, there is a common element and the following two subsequences.

```
Function IdentifyCommonElements(InstUCSeq S1, InstUCSeq S2):
Sequence(PISubSequences)
begin
    // i and j are used to go through sequences S1 and S2.
    // k and l indicate the position of the last common element.
    int i, j, k, l;
    PISubSequences pi;
    for (i = 1, l = 1, k = 1; I <= S1->size; i++) do
    begin
    // if we've reached the end of S2, it's not necessary to continue.
```

```
if (1 = S2->size) then
 begin
   break;
 endif
 for (j = 1; j <= S2->size; j++) do
 begin
   // Do we have a common element?
   if (S1->at(i) = S2->at(j)) then
   begin
    pi = new PISubSequences();
    // initializes all the attributes of pi to null
    pi.setCommonElem( S1->at(i) );
    if (k < i) then
    begin
      pi.setSeqOne( S1.subsequence(k, i-1) );
    end
    if (l < j) then
    begin
      pi.setSeqTwo( S2.subsequence(l, j-1) );
    end
    k = i + 1;
    l = j + 1;
    IdentifyCommonElements.append(pi);
    break;
   endif
 end
end
// Is there anything else to consider in the two sequences S1 and S2?
if ( (i != S1->size + 1) || (j != S2->size + 1) ) then
begin
 pi = new PISubSequences();
 pi.setCommonElem( null );
 if (k < S1->size + 1) then
 begin
   pi.setSeqOne( S1.subsequence(k, S1->size) );
 end
 if (1 < S2->size + 1) then
 begin
   pi.setSeqTwo( S2.subsequence(1, S2->size) );
 end
 IdentifyCommonElements.append(pi);
end
return IdentifyCommonElements;
```

end // of function IdentifyCommonElements