> Swarm Intelligence: An Introduction

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Origins, Observations of Nature Core Concepts and Principles SI based Algorithms Ant Colony Optimization Particle Swarm Optimization New Work

What is Swarm Intelligence? Why is Swarm Intelligence Interesting?

Introduction to Swarm Intelligence

This presentation will cover the following topics:

- What is Swarm Intelligence?
- Origins of Swarm Intelligence
- Core Concepts
- Applications and SI based algorithms

Origins, Observations of Nature Core Concepts and Principles SI based Algorithms Ant Colony Optimization Particle Swarm Optimization New Work

What is Swarm Intelligence? Why is Swarm Intelligence Interesting?

What is Swarm Intelligence?

What is "Swarm Intelligence" (SI)?

- http://www.youtube.com/watch?v=jEGV4ZSP22A
- "The collective behaviour of a decentralized, self-organized system"
- What is "Decentralization"?
- What is "Self-Organization"?

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What is Swarm Intelligence? Why is Swarm Intelligence Interesting?

What is Swarm Intelligence?

What does this definition mean to us?

- System consisting of a population of "agents"
- Simple Interactions between agents
- Leading to complex high-level behaviour

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What is Swarm Intelligence? Why is Swarm Intelligence Interesting?

Why is Swarm Intelligence Interesting?

Why is SI interesting to us?

- Framework for decentralized and scalable problem solving
- Unique perspective for addressing many problems

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What is Swarm Intelligence? Why is Swarm Intelligence Interesting?

Why is Swarm Intelligence Interesting?

SI naturally lends itself to alternative computational models:

- Distributed models
- Massively parallel models
- Flexible, dynamic models
- Robotics
- etc...

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What is Swarm Intelligence? Why is Swarm Intelligence Interesting?

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Why is Swarm Intelligence Interesting?

Useful in simulating many real-life systems

- Behaviour of crowds
- Traffic simulation
- Spread of disease
- etc...

Origins

Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Origins, Observations of Nature

Where did the idea of SI originate?

- Inspired by the success of swarming creatures in nature
- In particular: ants, termites and bees



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Ant Colonies

What's so interesting about ants?

- One of the most successful species on the planet
- Colonies can range from tens, to millions, of ants
- Individual ants are extremely basic creatures
- Colony displays a complex structure and behaviour
- How do they achieve this success?

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

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Colony Behaviour

A basic look at ant colony behaviour:

- Coordinated among specialized workers
- Labour tasks include:
 - Defence
 - Food Collection
 - Brood Care
 - Nest Cleaning
 - Nest Construction

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

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Colony Behaviour

Ants achieve complex behaviours:

- Division of labour, adaptive task allocation
- Path finding and optimization
- Clustering and sorting
- Structure formation
- Recruitment for foraging and collective transport of food

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Colony Behaviour

How does the colony address these tasks?

- Ants, as individuals, are extremely basic
- No single ant could plan these complex tasks
- These tasks are easily completed by the ant colony
- How is this possible?

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Colony Behaviour

Colony behaviour:

- Labour within ant colonies is decentralized
- No central planning or control
- Local interactions between ants
- Laying of chemical pheromones
- Complex behaviour arises
- A swarm intelligence is displayed

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Ant Foraging

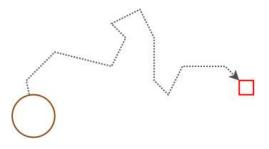
Ant Foraging:

- Ants effectively locate and exploit food sources
- Food sources are discovered by random exploration
- Ants discover efficient paths to known food sources
- Ants have no high-level knowledge of the situation
- How do ants form these efficient paths?

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Ant Foraging

- The key is pheromone
- While searching for food, ant movement is largely random



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Ant Foraging

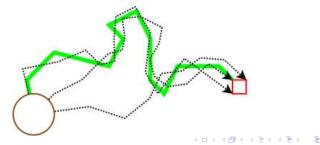
- Ants will return to the colony with food
- Ants with food will lay a trail of pheromone along their path



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Ant Foraging

- Ants are sensitive to pheromone
- The pheromone deposited attracts other ants
- Ants encountering a pheromone trail will tend to follow it
- These ants are more likely to reach the food source



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Ant Foraging

Over Time:

- More ants discover the food source
- More pheromone is deposited
- Existing trails to the food source are strengthened



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

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Trail Optimization

At the high level:

- Ants will seem to choose more optimal paths
- How is this achieved?
- Combination of:
 - Randomness of movement
 - Nature of pheromone

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Trail Optimization

Properties of pheromone:

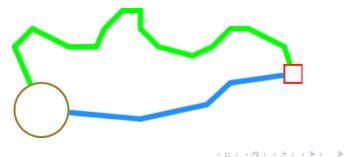
- Pheromones are chemicals subject to:
 - Evaporation
 - Diffusion
 - Other environmental effects
- Pheromone weakens over time
- Pheromone trails will dissipate and spread out

Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

Trail Optimization

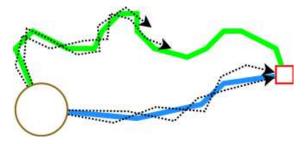
Example:

- A food source has been discovered by two ants
- One ant happens to take a more efficient path



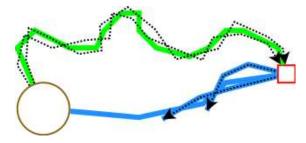
Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

- Each trail initially attracts a roughly equal number of ants
- Ants on the more efficient path arrive earlier



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

- Ants return, depositing additional pheromone
- Pheromone trail is strengthened on return



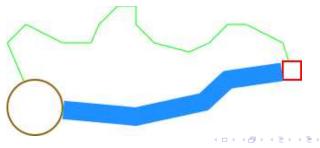
Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

- Ants following the more efficient trail have shorter trips
- Trips are completed with a higher frequency
- Higher frequency leads to stronger pheromone



Origins Ant Colonies Example: Ant Foraging Behaviour Trail Optimization

- Ants will favour the stronger pheromone trail
- Less efficient trail slowly dissipates
- The colony has chosen the more efficient path
- No knowledge of the global situation!



Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

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Core Concepts and Principles

What differentiates Swarm Intelligence from other Population-based methods?

• We must understand the core components:

- Decentralization
- Self-Organization
- Emergent Behaviour

Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

Decentralization and Self-Organization

Decentralization:

- Population of roughly homogeneous agents
- Control is fully distributed among the population
- No central "brain" controlling the agents
- Each agent has roughly the same level of influence

Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

Decentralization and Self-Organization

Self-Organization:

- Agents each act according to their own behaviour
- Agents communicate and interact
- Communications can include:
 - Direct contact
 - Local exchange of information
 - Local broadcasts
 - Stigmergy
 - etc...

Global behaviour arises from the interactions of the agents

Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

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Emergent Behaviour

"Emergent Behaviour" is the heart of SI

- A High-level behaviour of a population based system
- Must arise from the local interactions within the population
- Self-organization of a decentralized population
- Two categories: Weak and Strong

Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

Emergent Behaviour

Weak emergent behaviour of a population:

• can be reduced to the behaviour of a single individual

Strong emergent behaviour of a population:

• can not be reduced to the behaviour of a single individual

Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

Emergent Behaviour

Weak Emergent Behaviour:

- Extremely common
- Can be easily predicted by looking at a single individual
- Often simple to engineer
- For example, if individuals simply "move forward", the population will, as a whole, move forward

Core Concepts and Principles Decentralization Self-Organization Emergent Behaviour

Emergent Behaviour

Strong Emergent Behaviour:

- Heart of SI and very interesting phenomena itself
- Hard to predict from the behaviour of an individual
- May seem to "transcend" the capabilities of the individual
- "The whole is greater than the sum of its parts"
- It is often quite difficult to engineer
- For example, path optimization of foraging ants

SI and Artificial Life SI for Problem Solving

SI and Artificial Life

SI and Artificial Life:

- SI was first explored in the field of artificial life
- Simulations of swarming creatures
- "Boids" algorithm
- Motivation: learning more about emergent behaviours

SI and Artificial Life SI for Problem Solving

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SI based Algorithms

SI for problem solving:

- Relatively new field
- Active field of research
- SI algorithms have been used to address many problems
- Most commonly, optimization problems

Ant Colony Optimization

How Does Ant Colony Optimization Work? Generic Ant Colony Optimization Algorithm Example: Ant Colony Optimization for Travelling Salesman Example Application: ACO for Classification

Ant Colony Optimization

Ant Colony Optimization (ACO):

- Meta-heuristic method for combinatorial optimization
- One of the first SI algorithms for optimization
- Modelled after the foraging behaviour of ants
- ACO finds good paths through graphs
- Applicable to a wide variety of problems

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How ACO works

How does ACO work?

- ACO simulates the way ants communicate via pheromone
- Iteratively generates paths through graphs
- Pheromone "deposited" on graph edges
- Pheromone levels effect edge choices
- Good paths will emerge over time

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How ACO works

Generic ACO Process:

- Generic ACO consists of a two phase loop
 - Edge selection phase
 - Pheromone update phase
- Loop iterates until reaching some termination criteria

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Generic Ant Colony Optimization

Generic edge selection phase:

- Population of ants placed into the graph
- Ants move randomly through the graph
- Movement influenced by edge weights and pheromone
- Phase ends when all ants have created some kind of path

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Generic Ant Colony Optimization

Generic ant movement:

- For current node x with set of neighbours Y
- Choose edge $xy, y \in Y$ with probability p_{xy}

$$p_{xy} = \frac{(\tau_{xy})(\eta_{xy})}{\sum_{y_i \in Y} (\tau_{xy_i})(\eta_{xy_i})}$$

- η_{xy} Contribution of edge weight
- τ_{xy} Contribution of pheromone

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Generic Ant Colony Optimization

Generic pheromone update phase:

• Existing pheromone levels are reduced via "evaporation"

•
$$\tau_{xy} = (1 - \rho)\tau_{xy}$$

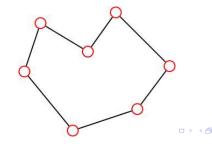
- ρ Evaporation coefficient parameter
- Ants return along the path taken through the graph
- At each edge, ants deposit pheromone
- Pheromone deposited according to: $\Delta \tau^k$
 - Path of each ant is evaluated using heuristic
 - $\Delta \tau^k \propto$ heuristic path value of ant k

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Ant Colony Optimization for Travelling Salesman

Travelling Salesman Problem (TSP):

- Given a set of cities
- Visit each city exactly once
- Return to the origin
- Find the tour with shortest total length



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Ant Colony Optimization for Travelling Salesman

Travelling Salesman Problem (TSP):

- NP-Hard
- Modelled as a complete graph
- Each node represents a city
- Edges have weight equal to the distance between cities
- ACO is applied to find good solutions in polynomial time

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Ant Colony Optimization for Travelling Salesman

ACO for TSP:

- Convert edge distance values into attractiveness value η
- For each pair of cities *x*, *y*:

•
$$\eta_{xy} = P/d_{xy}$$

- P Initial attractiveness parameter
- *d_{xy}* Distance between cities *x* and *y*
- Each ant will form a valid tour during edge selection
- Pheromone deposited according to tour values

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Ant Colony Optimization for Travelling Salesman

Edge selection for TSP:

- Each ant randomly assigned some city as their origin
- Ants travel through the graph visiting all cities
- Ants blacklist cities they have previously visited
- Blacklisted cities do not contribute to p_{xy} values
- After visiting all cities, ants return to their origin

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Ant Colony Optimization for Travelling Salesman

Selecting the next city in the tour:

- Current city x
- Set of unvisited cities Y
- Move to city $y \in Y$ with probability p_{xy}

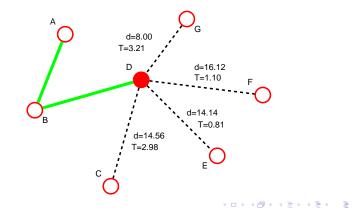
$$p_{xy} = \frac{(\tau_{xy})(n_{xy})}{\sum_{y_i \in Y} (\tau_{xy_i})(n_{xy_i})}$$

• If Y is empty, move to origin then stop

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Ant Colony Optimization for Travelling Salesman

For example, consider the following situation:



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Ant Colony Optimization for Travelling Salesman

Х	d	η	au	p
Α				
В				
С	14.56		2.98	
D				
Е	14.14		0.81	
F	16.12		1.10	
G	8.00		3.21	

Calculate η for each move:

•
$$\eta_{xy} = P/d_{xy}$$

• P = 100 for example

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Ant Colony Optimization for Travelling Salesman

Х	d	η	τ	p
Α				
В				
С	14.56	6.87	2.98	
D				
Е	14.14	7.07	0.81	
F	16.12	6.20	1.10	
G	8.00	12.5	3.21	

Calculate p for each move:

•
$$p_{xy} = \frac{(\tau_{xy})(\eta_{xy})}{\sum_{y_i \in Y} (\tau_{xy_i})(\eta_{xy_i})}$$

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Ant Colony Optimization for Travelling Salesman

Х	d	η	au	р
Α				0
В				0
С	14.56	6.87	2.98	0.28
D				0
Е	14.14	7.07	0.81	0.08
F	16.12	6.20	1.10	0.09
G	8.00	12.5	3.21	0.55

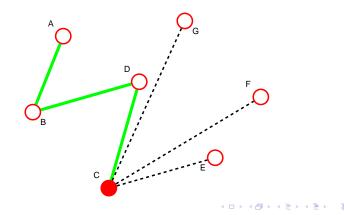
Choose the next move randomly according to *p*:

C is chosen

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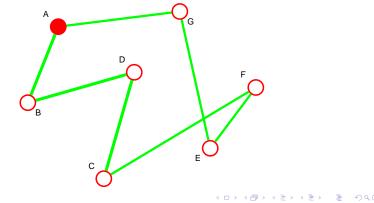
Move to C and repeat:



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Ant Colony Optimization for Travelling Salesman

When all cities have been visited, a valid tour has been created



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Ant Colony Optimization for Travelling Salesman

Pheromone Update Phase:

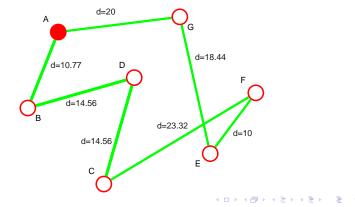
- Each ant calculates the cost of their tour
- Ants travel along their tours depositing pheromone
- For each ant k:
 - $\Delta \tau^k = Q/L_k$
 - L_k Value of ant k's tour
 - Q Pheromone attractiveness parameter
- For each edge xy:

•
$$\tau_{xy} = (1 - \rho)\tau_{xy} + \sum_k \Delta \tau^k$$

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Ant Colony Optimization for Travelling Salesman

Consider this tour:



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Ant Colony Optimization for Travelling Salesman

Pheromone deposit is calculated:

$$L = d_{AB} + d_{BD} + d_{DC} + d_{CF} + d_{FE} + d_{EG} + d_{GA}$$

= 10.77 + 14.56 + 14.56 + 23.32 + 10 + 18.44 + 20
= 111.65

Q = 100 for example

$$\Delta \tau = Q/L$$
$$= 100/111.65$$
$$= 0.89$$

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Ant Colony Optimization for Travelling Salesman

Algorithm:

- For each edge xy:
 - Initialize $\eta_{xy} = P/d_{xy}$
 - Initialize $\tau_{xy} = 0$
- Run simulation loop until reaching termination criteria
 - Edge Selection
 - Pheromone Update
- Return best tour found as output

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Ant Colony Optimization for Travelling Salesman

Behaviour in early iterations:

- Little to no pheromone
- Ants generate tours in a greedy way
- Closest cities chosen with high probability
- High variety in TSP tours generated

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Ant Colony Optimization for Travelling Salesman

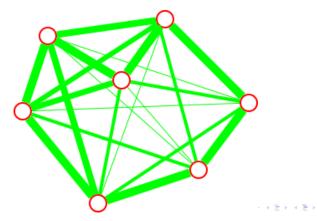
Behaviour in later iterations:

- Pheromone levels build up on popular edges
- Edges used by "good" tours will have more pheromone
- Pheromone levels begin to have greater influence
- Ants generate similar tours using these "good" edges

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Ant Colony Optimization for Travelling Salesman

Early iterations:

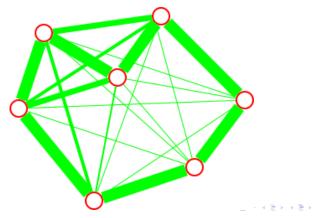


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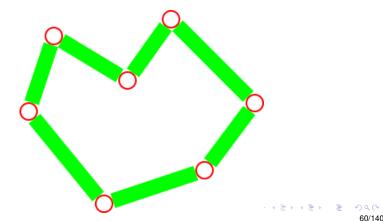
Later iterations:



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Ant Colony Optimization for Travelling Salesman

Convergence:



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ACO for Classification

- ACO finds applications in a wide variety of fields
- For example: data mining
- Rule-based classification

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Rule Based Classification

Given an object with a set of attributes:

- Assign a predefined class to the object
 - Based on a set of rules
 - Find a rule matching the attributes
 - Assign a class using this rule

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Rule Based Classification

Classification Rule:

- A rule assigns a class with the form:
 - IF < conditions > THEN < class >
 - IF A and B THEN 0
 - IF (A and C) or D THEN 1
 - etc...
- A condition has the form:
 - Attribute, Operator, Value
 - Colour = Blue
 - Width < 2</p>
 - etc...

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ACO for Rule Based Classification

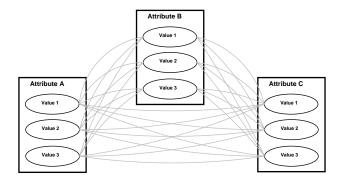
ACO can discover rules from a data set:

- These rules are of the form:
 - IF < condition AND condition AND ... > THEN < class >
- These conditions are restricted to "categorical" attributes
 - Attribute = Value

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Rules as Paths

Rules can be interpreted as paths through a graph:



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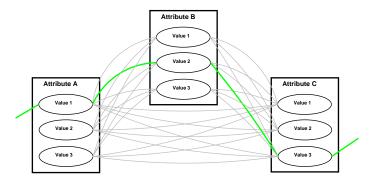
Rules as Paths

- Vertices represent conditions:
 - Attribute-value pair
 - Attribute = Value"
- Edges represent "AND" relations between conditions

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Rules as Paths

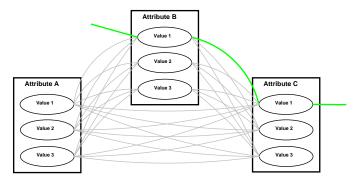
IF A=1 AND B=2 AND C=3:



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Rules as Paths

IF B=1 AND C=1:



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Applying ACO

To apply ACO to this graph representation, we require:

- Initial edge weights
- Heuristic for depositing pheromone

Ant Colony Optimization How Does Ant Colony Optimization Work? Generic Ant Colony Optimization Algorithm Example: Ant Colony Optimization for Travelling Salesman Example Application: ACO for Classification

Initial Edge Weights

Edge weights are assigned using the training set:

- Edges leading to an Attribute-Value pair are assigned weightings based on that Attribute-Value pair
- Weights are determined according to the normalized Shannon Entropy of that Attribute-Value pair within the training set

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Initial Edge Weights

Shannon Entropy:

$$H(W|A_a = V_{av}) = -\sum_{w \in W} (P(w|A_a = V_{av}) * \log_2 P(w|A_a = V_{av}))$$

- W: Set of possible classes
- A_a : Attribute $a \in A$
- V_{av} : Value $v \in V_a$

Represents the information gained by observing a given Attribute-Value pair according to the training set

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Edge Weights

For edges leading to value $v \in V_a$ of attribute $a \in A$:

$$\eta = \frac{\log_2 |W| - H(W|A_a = V_{av})}{\sum_{i \in A} \sum_{j \in V_i} \left(\log_2 |W| - H(W|A_i = V_{ij})\right)}$$

A normalized and inverted Shannon Entropy

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Pheromone Heuristic

New rules are evaluated using the "quality" measure:

$$Q = \frac{TP}{TP + FN} * \frac{TN}{FR + TN}$$

- TP : True Positives
- TN : True Negatives

- FP : False Positives
- FN : False Negatives

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ACO Rule Generation Algorithm

Until termination:

- Initialize edge weights using the uncovered training set
- Until convergence:
 - Generate a new rule as a path
 - Deposit and evaporate pheromone
- Add the best-found rule to the final set of rules
- Discard training cases covered by the new rule

Output: A list of classification rules

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Convergence and Termination

Convergence occurs when either:

- The same rule is generated a specified number of times
- The maximum number of ants per iteration is reached

Termination occurs when:

• The number of uncovered cases reaches a threshold

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ACO has successfully been applied to generate a set of classification rules from a training set. These rules can now be applied to perform classification.

Particle Swarm Optimization Real-valued Black-box Optimization How Particle Swarm Optimization Works Effects of Parameters Algorithm Swarm Behaviour Benefits of Particle Swarm Optimization Example Application: Broadcast Tower Coverage

Particle Swarm Optimization

Particle Swarm Optimization (PSO):

- SI algorithm for real-valued, black-box optimization
- Discovered accidentally
- Originally a simulation of "social flocking" behaviour
- Population made of "particles" in the solution space
- Collision free "bird flocking" behaviour

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Real-valued Black-box Optimization

Real-valued optimization problems:

- Find the optimal input to some objective function
- Each parameter is a real number

Solution space:

- Parameters define a "solution space"
- Each parameter corresponds to a dimension
- A point in this space represents a function input

Black-box optimization problems:

- Objective function provided as a "black-box"
- Nothing is known about the function
- Must learn about the function through evaluations

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How Particle Swarm Optimization Works

Particles:

- Particles exist as points in the solution space
- These points represent input values to objective function
- Assigned values by evaluating the objective function
- "Fly" through solution space
- Communicate via broadcast

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How Particle Swarm Optimization Works

Each particle is simply made up of:

- Position X
- Velocity \vec{V}
- Personal Best Point $\vec{P_i}$

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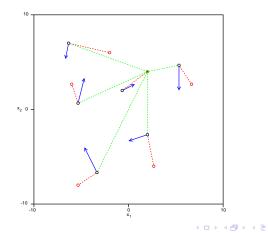
How Particle Swarm Optimization Works

Particle behaviour:

- Particles move according to their velocity
- Velocity is updated through accelerations
- Inertial weighting is applied to prevent explosive speeds
- Acceleration towards the particle's best found point
- Acceleration towards the swarm's best found point

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How Particle Swarm Optimization Works



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How Particle Swarm Optimization Works

Acceleration towards personal best:

- Self influence
- Influence of the particle's own knowledge

Acceleration towards global best:

- Social influence
- Influence of the swarm's collective knowledge
- Global best points are communicated via broadcast

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How Particle Swarm Optimization Works

Accelerations:

- Randomly weighted according to parameters
 - ϕ_p Personal influence parameter
 - ϕ_g Social influence parameter
- Separate random weighting per dimension
 - More "explorative"
- Constant deceleration is applied
 - ω Inertial weighting parameter
 - Allows stronger accelerations without explosive speeds
 - Promotes convergence

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Effects of Parameters

Low personal influence, high social influence:

- Faster convergence
- More susceptible to local optima
- Exploitation > Exploration

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Effects of Parameters

High personal influence, low social influence:

- Slower convergence
- Less susceptible to local optima
- Exploitation < Exploration

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Effects of Parameters

NO personal influence, high social influence:

- Social only swarm
- All particles immediately converge to the best found point
- Behaviour degrades to simple repeated local search

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Effects of Parameters

High personal influence, NO social influence:

- "Self only" swarm
- Each particle acts completely independently
- Behaviour degrades to multiple local search
- No "swarm intelligence" present

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Effects of Parameters

Parameter values:

- Matter of exploration vs. exploitation
- Exploration required for more "difficult" problems
- Exploitation required for convergence and efficiency

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Effects of Parameters

Parameters:

- Typically, both ϕ_p and ϕ_g are set to 2
- ω set to around 0.7
- Must be tweaked for each problem to get best results
- This tweaking is often unintuitive
- Requires knowledge of the solution space

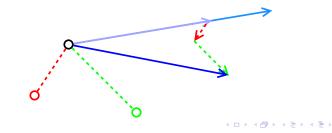
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Particle Swarm Optimization Algorithm

Velocity and position update equations:

• For each dimension *d*:

$$V_d = \omega V_d + U[0, \phi_P](P_{i_d} - X_d) + U[0, \phi_g](P_{g_d} - X_d)$$
$$X_d = X_d + V_d$$



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Example Particle Update

Consider a particle with:

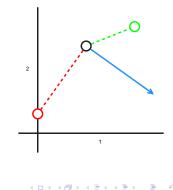
- *X* = [5,9]
- *V* = [7, -5]

And global best found point:

• *P*_g = [10, 11]

With PSO Parameters:

ω = 0.7



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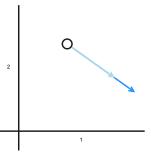
Example Particle Update

Inertial weighting is applied:

$$V_1 = \omega V_1$$

= 0.7 * 7
= 4.9
$$V_2 = \omega V_2$$

= 0.7 * -5
= -3.5



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Example Particle Update

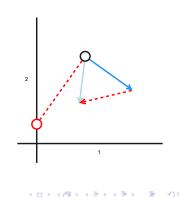
Random acceleration towards P:

$$V_1 = V_1 + U[0, \phi_p](P_1 - X_1)$$

= 4.9 + U[0, 2](0 - 5)
= 4.9 + (1.1 * -5)
= -0.6

$$V_2 = V_2 + U[0, \phi_p](P_2 - X_2)$$

= -3.5 + U[0, 2](2 - 9)
= -3.5 + (0.2 * -7)
= -4.9



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Example Particle Update

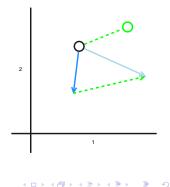
Random acceleration towards P_g :

$$V_1 = V_1 + U[0, \phi_g](P_1 - X_1)$$

= -0.6 + U[0, 2](10 - 5)
= 4.9 + (0.4 * 5)
= 6.9

$$V_2 = V_2 + U[0, \phi_g](P_2 - X_2)$$

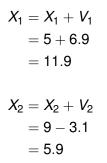
= -4.9 + U[0,2](11 - 9)
= -4.9 + (0.9 * 2)
= -3.1

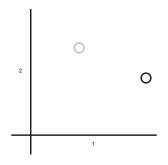


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Example Particle Update

Update position:





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Particle Swarm Optimization Algorithm

Algorithm:

- Initialize particles:
 - Random position
 - Random velocity
 - Evaluate initial positions
- While termination criteria not met:
 - Update P_g via communication
 - For each particle *i*:
 - Update velocity
 - Update position
 - Evaluate new position
 - Update P_i

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Swarm Behaviour

Behaviour in early stages:

- Particles will fly through the solution space
- Overshoot the global and personal best points
- Arc and loop around these points
- Coarse-grained search
- Swarm finds "good" areas
- Particles slow over time, swarm begins to converge

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Swarm Behaviour

Behaviour in later stages:

- Stagnation of global best point leads to convergence
- Particles gather around this point, slowing over time
- Fine-grained search of the "good" area
- Swarm finds the best point within the "good" area

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Benefits of Particle Swarm Optimization

Benefits of PSO:

- Very simple to implement
- No costly computations
- Easily extendable to problems of any dimension
- Effective on difficult, noisy problems
- Can be applied to any black-box real-valued function
- Can even be used in meta-optimization
- PSO finding optimal parameters for PSO on some problem

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Example Application

PSO can be applied to solve a problem if:

- A solution to the problem can be represented as a number of real-valued parameters
- A solution's quality can be represented by a single value
- A function is provided which evaluates any given solution

As an example, consider the problem of maximizing the coverage of a number of broadcast towers.

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Simple Broadcast Coverage Problem

Given a set number of broadcast towers:

- Assign each tower an x, y coordinate
- Assign each an amount of power

In order to:

- Maximize coverage
- Minimize power costs

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Simple Broadcast Coverage Problem

In order to apply PSO we must:

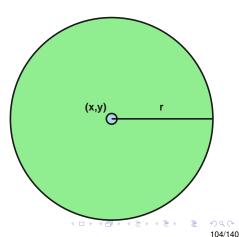
- Form a real-valued solution space
- Represent the problem as a function which:
 - Assigns values to points in the solution space
 - Evaluates the quality of a given solution point

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Tower Representation

Each tower has 3 parameters

- x coordinate
- y coordinate
- power r



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Solution Space

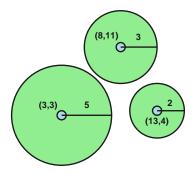
Multiple towers can be respresented:

- [Tower₁, Tower₂, ..., Tower_n]
- $[x_1, y_1, r_1, x_2, y_2, r_2, ..., x_n, y_n, r_n]$
- A solution space with 3*n* dimensions
- A particle's position in this space describes:
 - The positions and power values of *n* towers
 - A candidate solution to the tower coverage problem

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Example Point

For example, X = [3, 3, 5, 8, 11, 3, 13, 4, 2] corresponds to:



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Evaluating a Solution

PSO requires a function to evaluate these solutions:

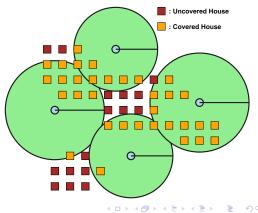
- Total coverage of the towers
- Penalize for power costs

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Coverage

For simplicity:

- Houses within broadcast range
- Each house is worth some set value
- For example:
 - 10 per house



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Power Cost

For simplicity, the cost of a tower is:

- A flat initial cost, for example 100
 - If *r* <= 0, the tower is considered unused
 - No initial cost in this case
- Power cost scaling exponentially with r

• For example: r²

Cost of *n* towers =
$$\sum_{i=0}^{n} \begin{cases} 0, & r_i <= 0\\ 100 + r_i^2, & r_i > 0 \end{cases}$$

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Final Evaluation Function

The final evaluation function is then:

$$egin{aligned} f(...) &= \textit{HouseCoverage} - \textit{PowerCosts} \ &= 10*|\textit{Covered}| - \sum_{i=0}^n egin{cases} 0, & r_i <= 0 \ 100+r_i^2, & r_i > 0 \end{aligned}$$

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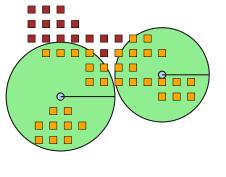
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Example

f(7, 7, 7, 21, 10, 6)

$$=10 * |Covered| -\sum_{i=0}^{n} \begin{cases} 0, & r_{i} <= \\ 100 + r_{i}^{2}, & r_{i} > 0 \end{cases} \\=10 * 34 - (7^{2} + 100) - (6^{2} + 100) \\=55 \end{cases}$$



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Example

$$f(13, 10, 13, 21, 11, 0)$$

$$=10 * |Covered|$$

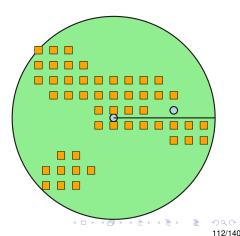
$$-\sum_{i=0}^{n} \begin{cases} 0, & r_i <= 0\\ 100 + r_i^2, & r_i > 0 \end{cases}$$

$$=10 * 49$$

$$-(13^2 + 100)$$

$$-(0)$$

$$=121$$



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Applying PSO

Applying PSO:

- Plug in the evaluation function
- Provide appropriate parameter ranges
- PSO will search for the optimal solution:
 - According to the provided evaluation function
 - Accuracy of this function is essential
 - PSO will exploit errors in this function

Thank You

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Questions?

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Introduction

Bare-Bones PSO Abstracting the BBPSO Algorithm Particle Field Optimization Further Developing PFO Final PFO Algorithm

New Work

My research:

- Particle Field Optimization (PFO)
- Based on the PSO algorithm
- Abstraction of the "Bare-Bones" PSO model

Exploring:

- New high-level concept
- New behaviour
- New avenues for development

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Bare-Bones PSO

Bare-Bones Particle Swarm (BBPSO):

- Abstraction of the core PSO
- Simplifies the particle update process
- Removal of velocity and acceleration
- Retains roughly the same behaviour

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Bare-Bones PSO

From PSO to BBPSO:

- Observations of a single particle during swarm stagnation
- Each dimension shows a distinct bell-curve histogram
- Can a similar histogram be achieved in a simpler way?

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Bare-Bones PSO

New method of position update:

- Update particles according to Gaussian distribution
- Distribution constructed to mimic histogram bell-curve
- Velocity and accelerations discarded entirely
- Particle movement abstracted to a random sampling

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Bare-Bones PSO

BBPSO particle update:

• For each particle i:

•
$$P_m = \frac{P_i + P_g}{2}$$

For each dimension d:

•
$$X_{i_d} = \mathcal{N}(P_{m_d}, |P_{i_d} - P_{g_d}|)$$

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Bare-Bones PSO

Result of BBPSO:

- Roughly the same high-level behaviour
- Roughly the same level of performance
- Particles no longer "fly" through the space
- Much simpler particle behaviour
- More predictable, easier to analyze

Introduction Bare-Bones PSO Abstracting the BBPSO Algorithm Particle Field Optimization Further Developing PFO Final PFO Algorithm

Abstracting the BBPSO Algorithm

Abstracting the BBPSO:

- It is possible to further abstract the BBPSO
- Recall the components of the canonical PSO particle:
 - Position
 - Velocity
 - Personal best found point
 - Communicated knowledge of global best
- Each component is required to update the particle

Introduction Bare-Bones PSO Abstracting the BBPSO Algorithm Particle Field Optimization Further Developing PFO Final PFO Algorithm

Abstracting the BBPSO Algorithm

Abstracting the BBPSO:

- The BBPSO algorithm removes the velocity component
- Position is updated by random sampling
- Sampled distribution is independent of current position
- Communication of global bests depend on personal bests
- Current position is used only to update the personal best

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Abstracting the BBPSO Algorithm

Particles without positions:

- Particles can be updated without storing a position
- Sample the random distribution
- Evaluate new point
- Update the best found point if needed
- Discard the new point

Introduction Bare-Bones PSO Abstracting the BBPSO Algorithm Particle Field Optimization Further Developing PFO Final PFO Algorithm

Abstracting the BBPSO Algorithm

Effects of removing particle position:

- Identical behaviour to BBPSO
- Different concepts
- Particles no longer exist as explicit points
- Each particle defined by its best found point
- Particle's construct and sample a random distribution
- Probability of that particle existing at a given point

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New Model

Moving forward with this concept:

- Individuals are no longer candidate solutions
- Each represents a probability field
- Simple Gaussian distributions
- No longer "Particles"
- Instead, "Particle Fields"

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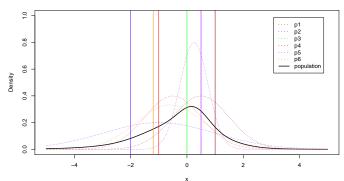
New Model

At the population level:

- Population forms a complex probability field
- Sum of simple individual fields
- Probability field of all possible particle locations

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New Model



Population Probability Field

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New Model

Population probability field:

- Probability field updated as individuals are updated
- Shows how PSO explores the solution space
- Demonstrates how PSO "learns"
- Similarities to a limited Bayesian learning process

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New Model

Generating candidate solutions:

- Solutions have been separated from particles
- Maintain a population of candidate solutions
- Solutions generated by sampling complex population distribution
- For each candidate solution:
 - Randomly select a particle field individual
 - Generate position from that individual's distribution

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New Model

Updating the particle field individuals:

- Each solution chooses an individual during generation
- Individual's are updated using associated solutions
- Similar to the standard PSO method
- Adapted to handle any number of associated solutions

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New Model

Moving forward again:

- Still roughly the same behaviour as the BBPSO
- Slightly more random
- Biggest difference is the high-level concept
- New concept provides new avenues for development

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New Model

Modifying the population distribution:

- Now possible to modify the population probability field
- Consider complex population distribution
- Sum of simple individual distributions
- Apply simple weighting scheme
- Drastic change to population distribution
- Focus search to better areas?

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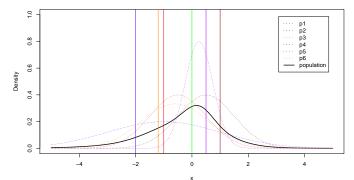
Weighting Schemes

Effects of weighting schemes:

- Introduce new behaviour
- Changes the population probability field
- Changes how the swarm "learns"
- Incorporate different information into the search

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Effects of Weighting

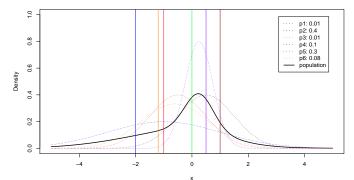


Population Probability Field

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Effects of Weighting



Weighted Population Probability Field

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Relative Population Sizes

Modifying relative population sizes:

- Model now consists of two separated populations
- Possible to modify population sizes independently
- Relative sizes effects the high level behaviour
- More particle field individuals:
 - May be more exploratory
- Less particle field individuals:
 - Faster convergence

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Final PFO Algorithm

Final PFO Algorithm:

- Combining all these changes we have a distinct algorithm
- New behaviour and perspective
- New avenues for future development

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PFO Simulation Step

For each candidate solution to be generated:

- Sample complex distribution defined by PF population
- Randomly choose a particle field individual
- According to weighting values
- Sample that individual's simple distribution

For each PF individual:

- Choose best associated solution
- Update personal best point if needed
- Calculate new weighting value

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Results

Preliminary experimental results:

- Weighting scheme for individuals:
 - Average value of candidate solutions generated by each
 - Better information than just the best found?
- Tests done with different ratios of population sizes
- Compared to BBPSO
- Better performance on all test problems

Thank You

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Questions?

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